



MAX-PLANCK-INSTITUT  
FÜR PHYSIK



# A method for obtaining 3D charge density distribution of a self-modulated proton bunch

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on behalf of the AWAKE Collaboration

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# Conventional accelerators

- Synchrotron radiation in circular machines  $\sim \frac{1}{m^4}$  – limitation for light particle colliders
  - Modern RF cavities: limit on accelerating gradient  $\sim$  **100 MeV/m** (electric breakdown)
- ⇓
- Increase acceleration length to increase particle energy

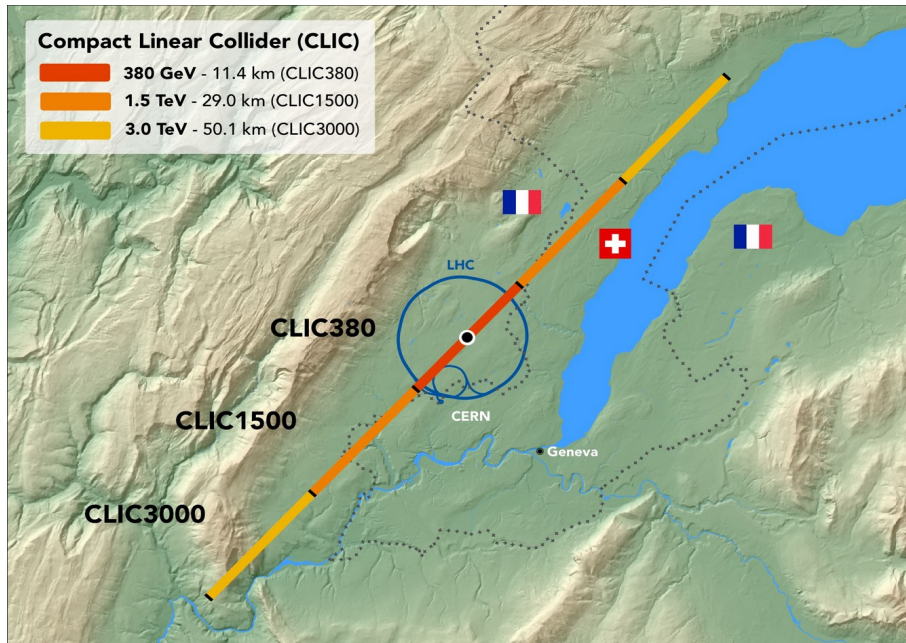


Image: CLIC – possible future linear collider at CERN.

© CERN



Image: Stanford Linear Accelerator (SLAC), USA;  
building covering the beam tube is  $\sim 3.2$  km long!  
© Wikipedia

# Why PWFA?

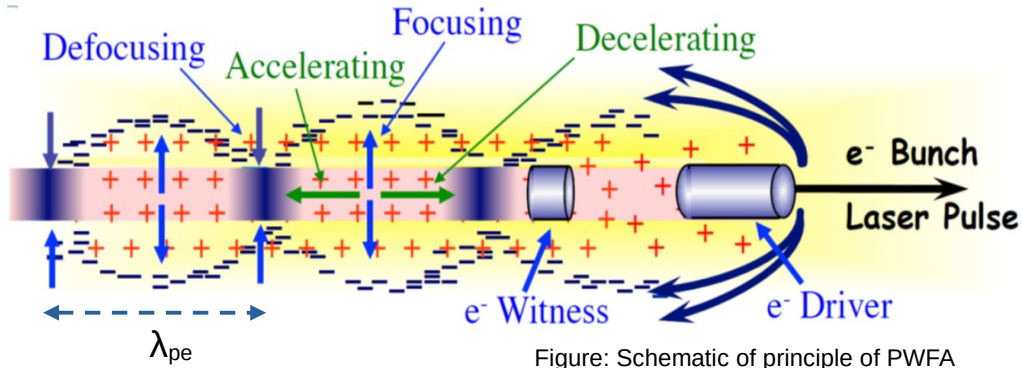


Figure: Schematic of principle of PWFA  
© P. Muggli, MPP Munich, Germany

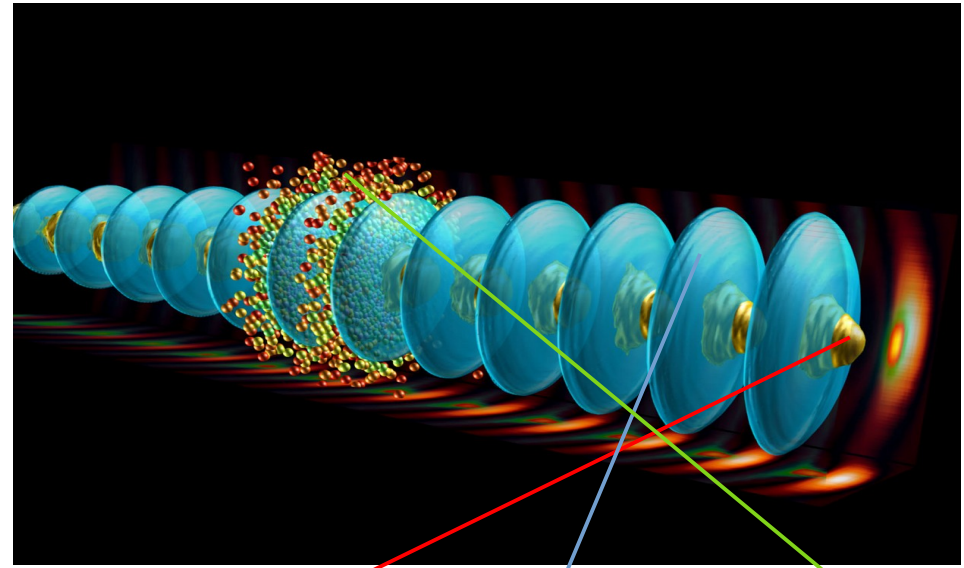


Image: drive bunch creates a plasma wave, which accelerates witness bunch  
© J. Vieira, IST Lisbon, Portugal

## Plasma-based acceleration (PWFA):

- Particle bunch or laser pulse propagates through plasma →
- Plasma electrons oscillation →
- Transverse and longitudinal electric and magnetic fields – wakefields
- Linear theory: wakefields – sinusoidal oscillations at  $\omega_{pe}$

$$\text{Electric fields up to } E_{WB} = \frac{m_e c \omega_{pe}}{e}, \quad \omega_{pe} = \sqrt{\frac{n_{pe} e^2}{\epsilon_0 m_e}}$$

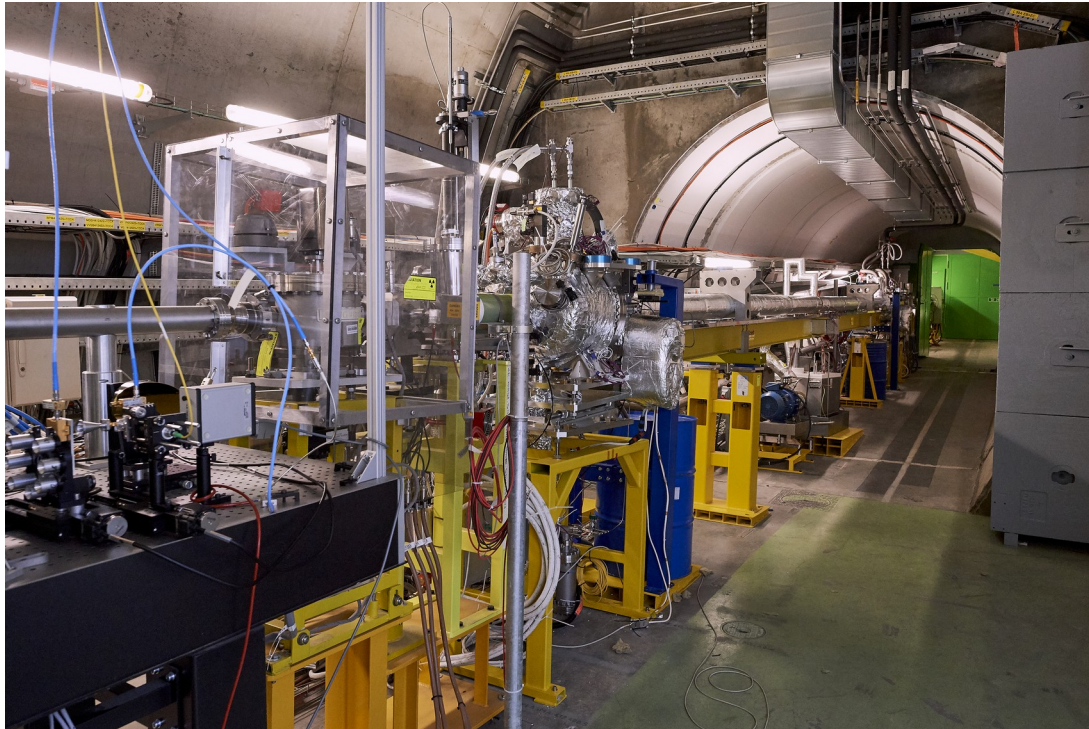
↓

$$\text{Accelerating gradient limit [eV/m]} \sim 96 \sqrt{n_{pe} [\text{cm}^{-3}]}$$

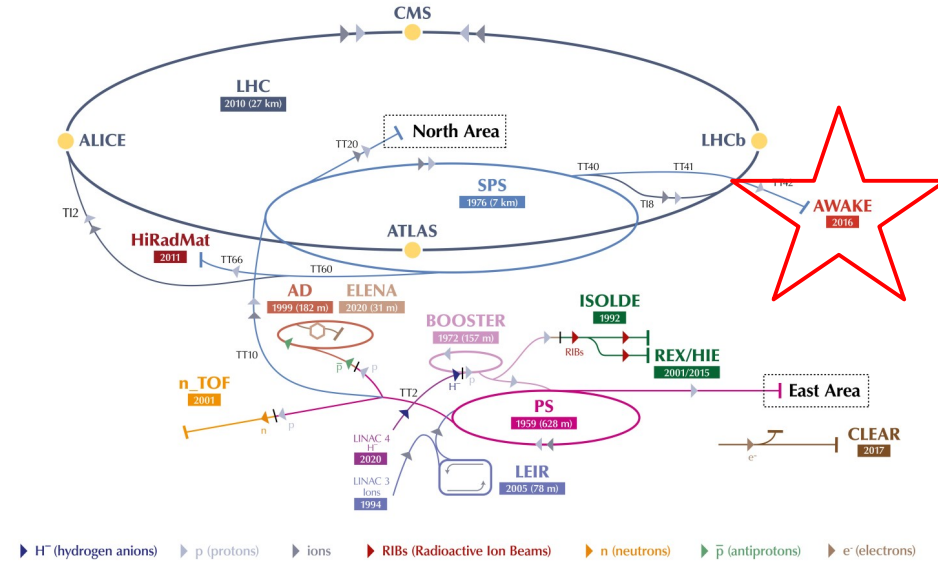
$$\text{when } n_{pe} = 10^{18} \text{ cm}^{-3} \Rightarrow \text{gradient} \sim \mathbf{100 \text{ GeV/m}}$$

# AWAKE experiment

- AWAKE – Advanced Wakefield Experiment
- CERN-based R&D project – collaboration of ~20 institutes  
→ proton driven PWFA studies
- Final goal → quality-preserving high-energy electron beam accelerator



The CERN accelerator complex  
*Complexe des accélérateurs du CERN*



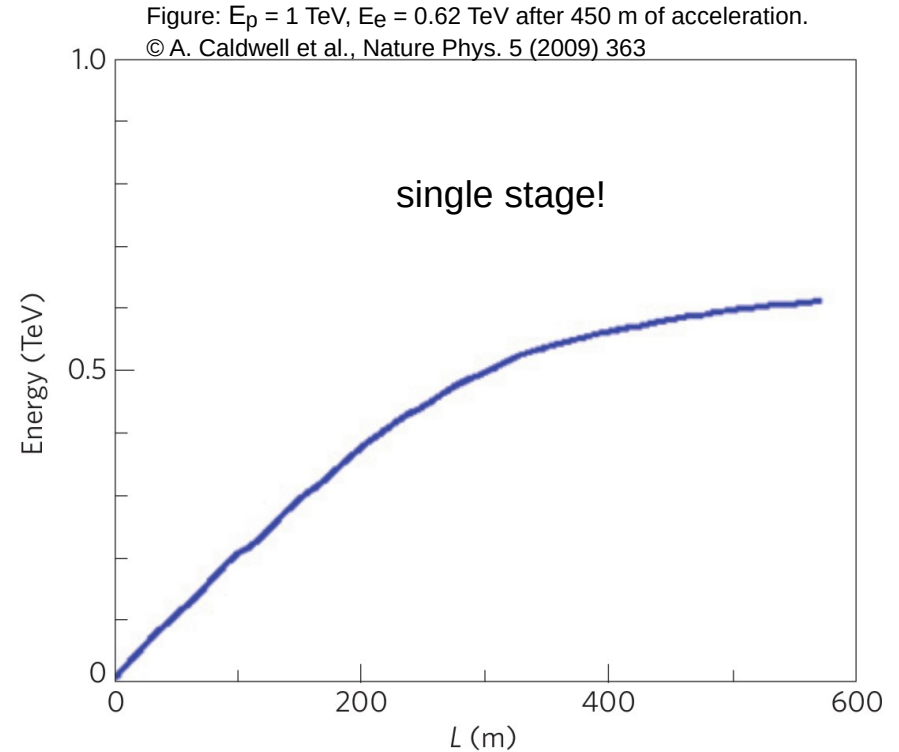
LHC - Large Hadron Collider // SPS - Super Proton Synchrotron // PS - Proton Synchrotron // AD - Antiproton Decelerator // CLEAR - CERN Linear Electron Accelerator for Research // AWAKE - Advanced WAKEfield Experiment // ISOLDE - Isotope Separator OnLine // REX/HIE - Radioactive EXperiment/High Intensity and Energy ISOLDE // LEIR - Low Energy Ion Ring // LINAC - LiNear ACcelerator // n\_TOF - Neutrons Time Of Flight // HiRadMat - High-Radiation to Materials

# Proton drive bunch

- Energy gain of witness bunch  $\leq$  energy loss of drive bunch
- $p^+$  bunch  $\rightarrow$  higher energies than laser pulses or  $e^-$  bunches:
  - SPS  $p^+$  bunch (used in AWAKE)  $\rightarrow \sim 19$  kJ
  - SLAC  $e^-$  bunch  $\rightarrow \sim 91$  J
  - 1 PW, 100 fs laser pulse  $\rightarrow < 100$  J
- $p^+$  bunch  $\rightarrow$  drive wakefields over long distance  $\rightarrow$  no need for staging

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- Theory: resonantly drive high-amplitude wakefields  $\rightarrow$  **bunch length  $\sigma_z \sim \lambda_{pe}$** ; SPS  $p^+$  bunch:  $\sigma_z \sim 12$  cm  $\gg \lambda_{pe}$



- Long  $p^+$  bunch in plasma  $\rightarrow$  **self-modulation instability (SMI)**  
 $\rightarrow$  train of micro-bunches

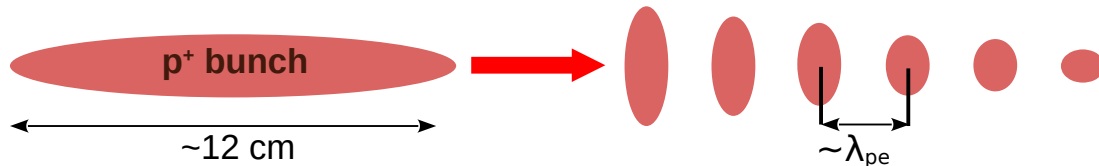
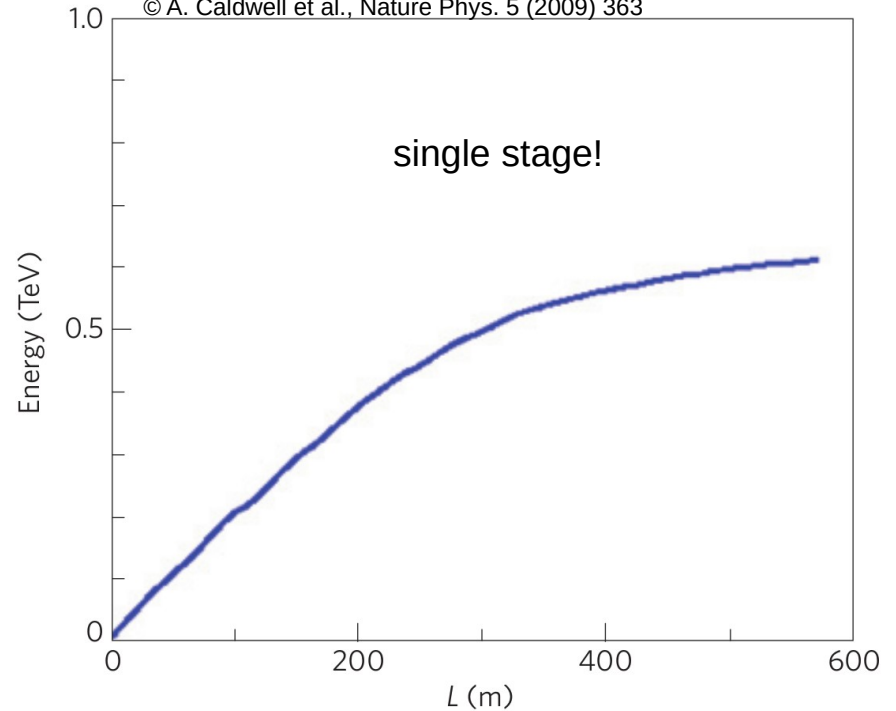


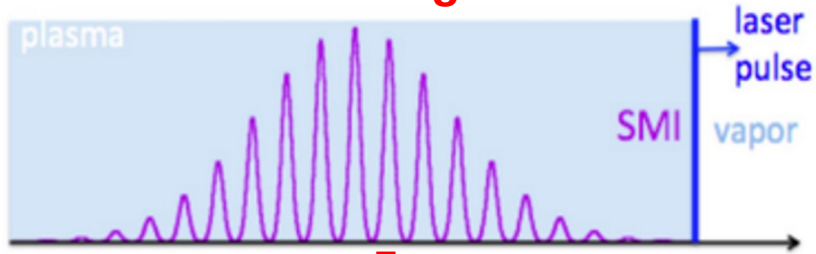
Figure:  $E_p = 1$  TeV,  $E_e = 0.62$  TeV after 450 m of acceleration.

© A. Caldwell et al., Nature Phys. 5 (2009) 363

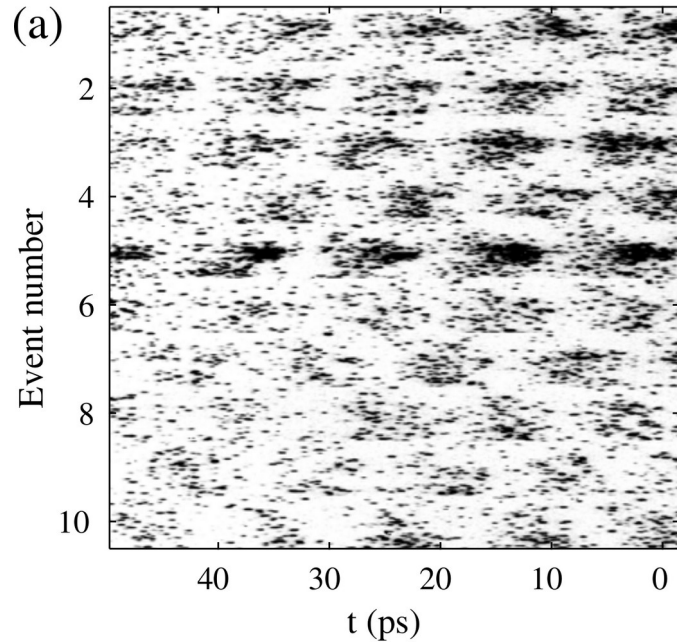


# Self-modulation: instability $\rightarrow$ seeded

**No seeding**

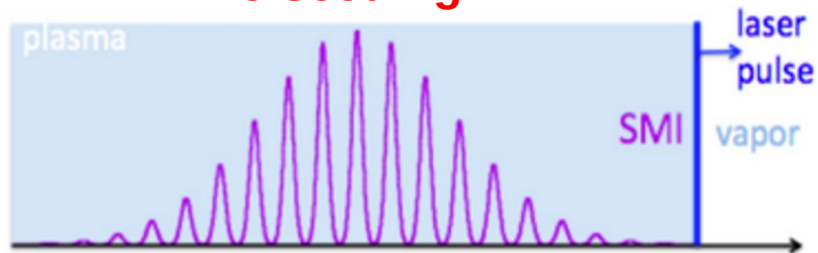


F. Batsch et al., Phys. Rev. Lett. 126, 164802 (2021)

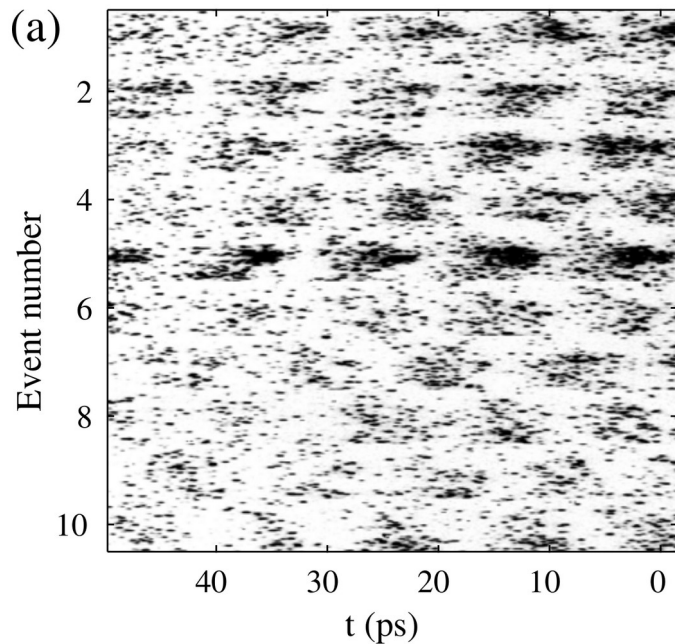


# Self-modulation: instability $\rightarrow$ seeded

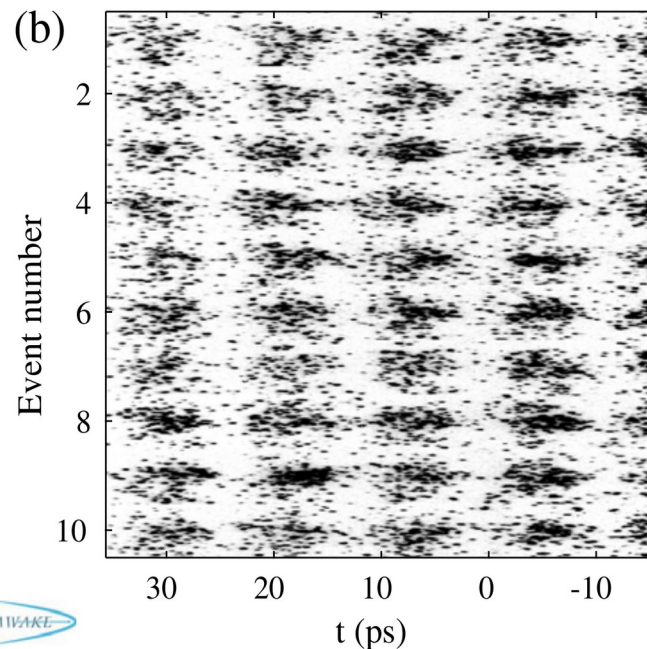
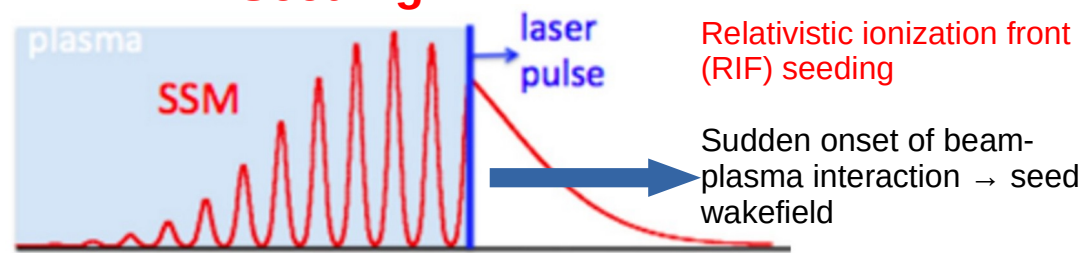
No seeding



F. Batsch et al., Phys. Rev. Lett. 126, 164802 (2021)



Seeding

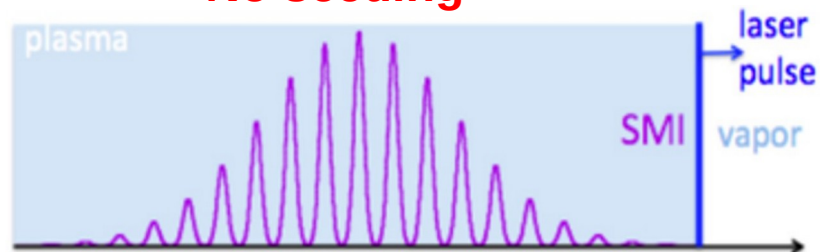


Reproducible outcome!

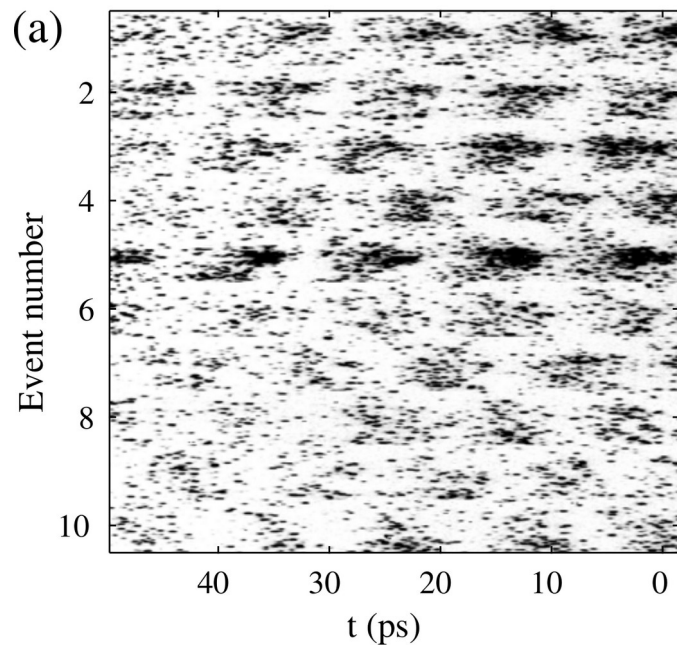
$$\Delta t / \tau_{pe} \sim 6 \%,$$
$$\tau_{pe} = 2\pi / \omega_{pe}$$

# Self-modulation: instability $\rightarrow$ seeded

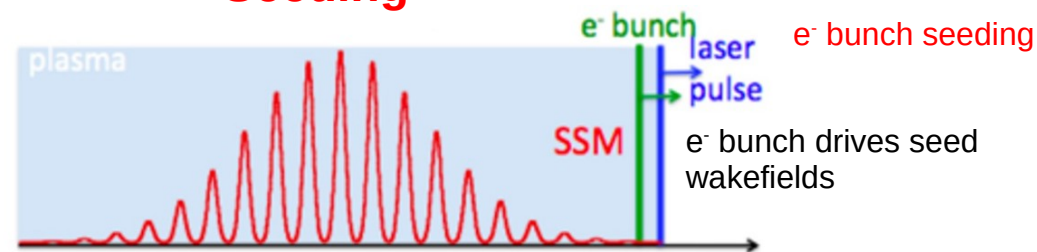
**No seeding**



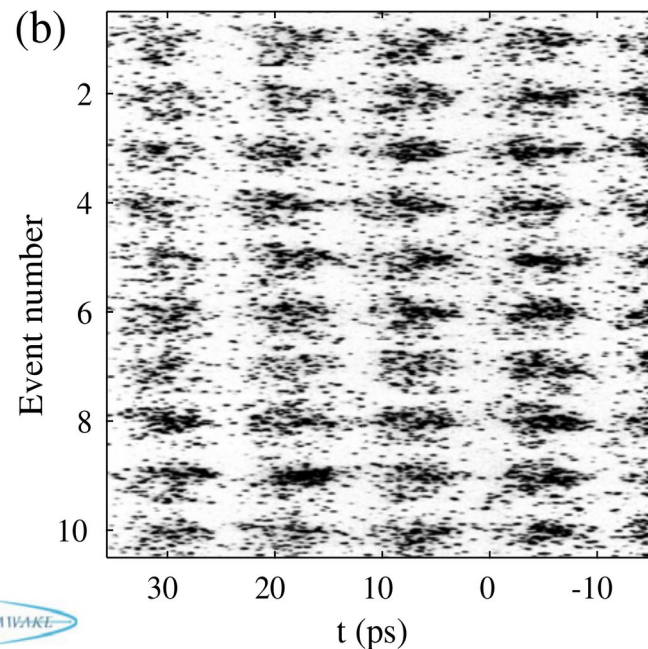
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**Seeding**



L. Verra et al., accepted for publication to Phys. Rev. Lett. (2022)

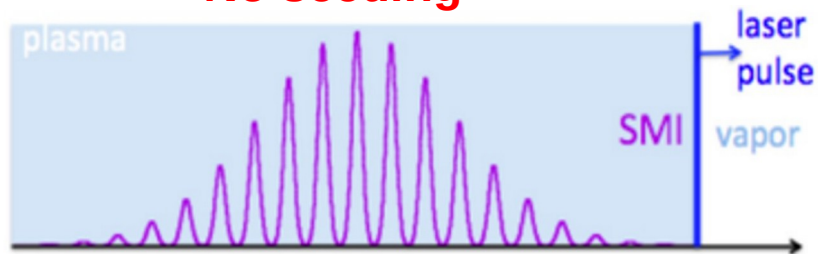


→ Reproducible outcome!

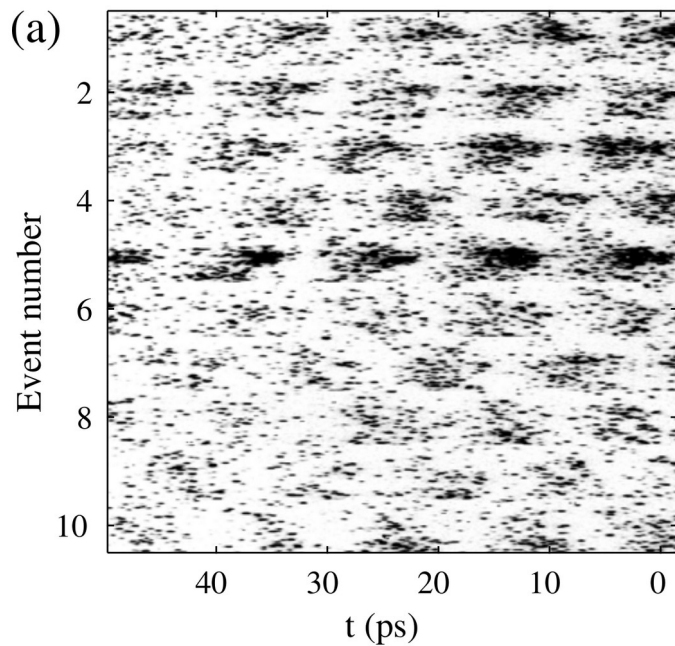
$$\Delta t / \tau_{pe} \sim 6 \%,$$
$$\tau_{pe} = 2\pi / \omega_{pe}$$

# Self-modulation: instability $\rightarrow$ seeded

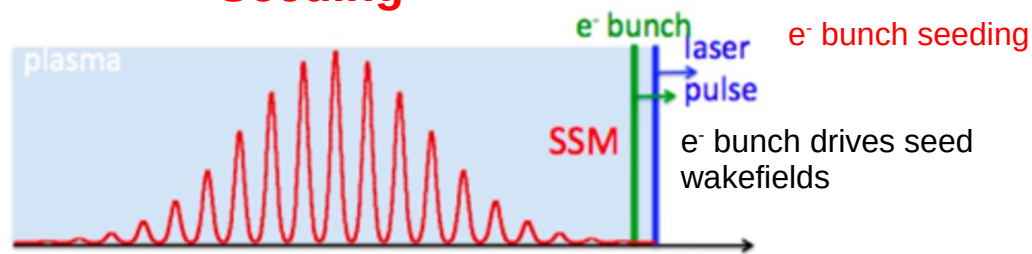
**No seeding**



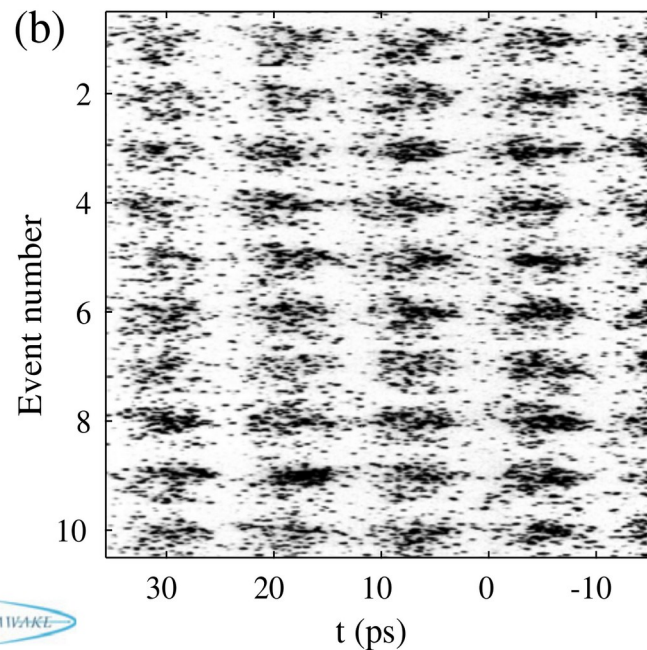
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**Seeding**



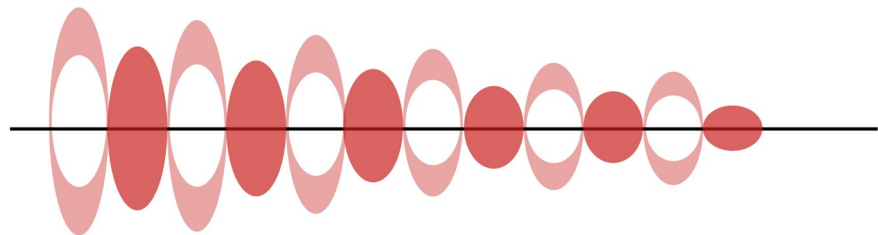
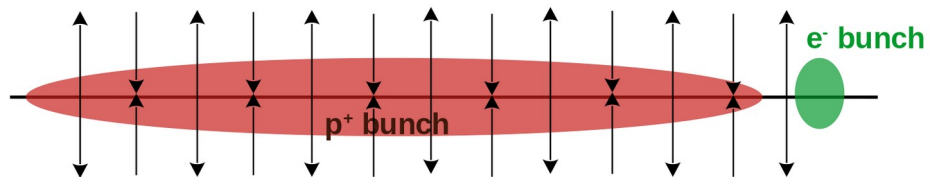
L. Verra et al., accepted for publication to Phys. Rev. Lett. (2022)



**Reproducible outcome!**

$$\Delta t / \tau_{pe} \sim 6 \%,$$
$$\tau_{pe} = 2\pi / \omega_{pe}$$

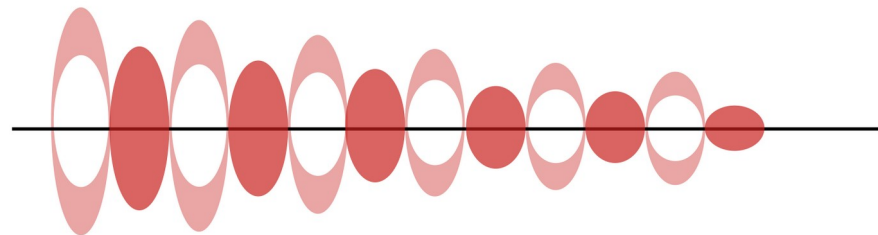
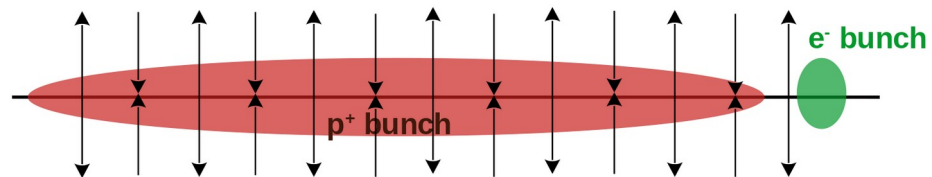
# eSSM vs eSSM+Hosing



e<sup>-</sup> and p<sup>+</sup> bunches aligned  
force on p<sup>+</sup> bunch centroid = 0  
force on p<sup>+</sup> bunch slice → focusing/defocusing

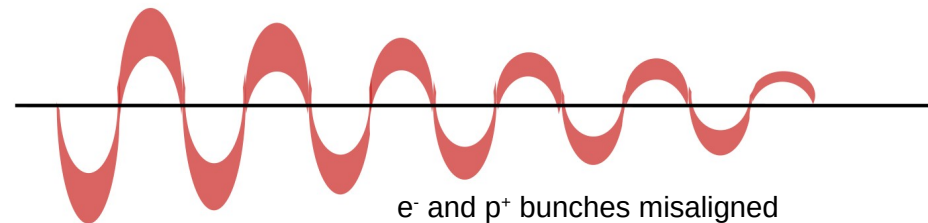
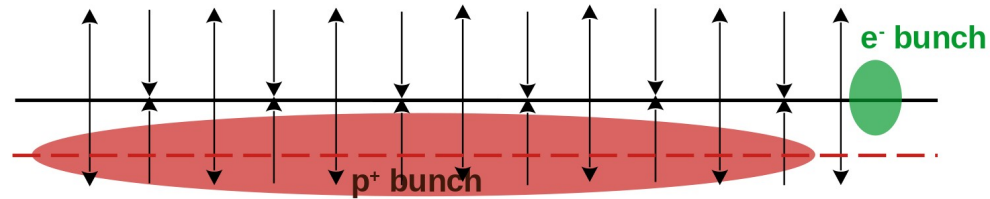
↓  
eSSM

# eSSM vs eSSM+Hosing



$e^-$  and  $p^+$  bunches aligned  
force on  $p^+$  bunch centroid = 0  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing

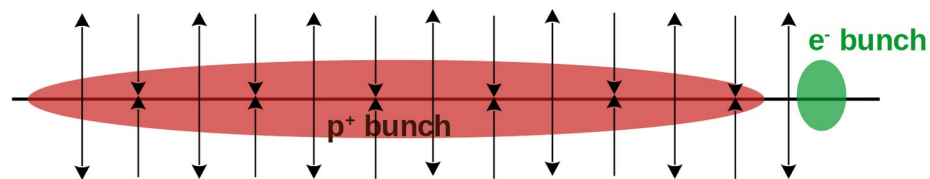
**↓**  
eSSM



$e^-$  and  $p^+$  bunches misaligned  
force on  $p^+$  bunch centroid  $\neq 0 \rightarrow$  hosing  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing

**↓**  
Hosing + eSSM  
 $\downarrow$        $\downarrow$   
one plane    plane  $\perp$  hosing

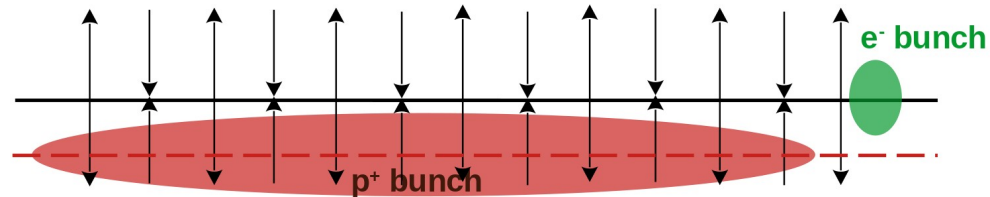
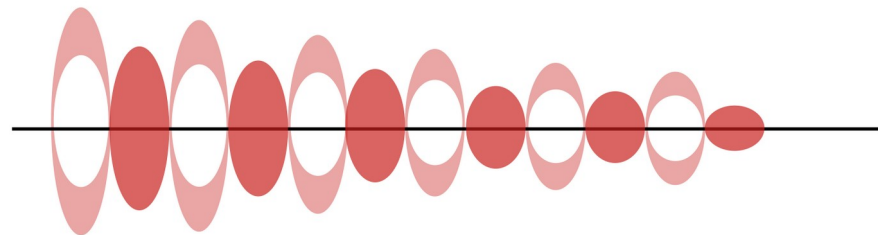
# eSSM vs eSSM+Hosing



$e^-$  and  $p^+$  bunches aligned  
force on  $p^+$  bunch centroid = 0  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing



eSSM



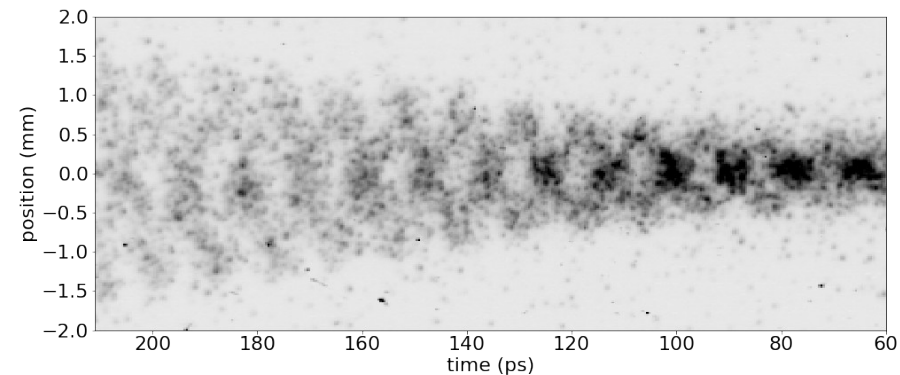
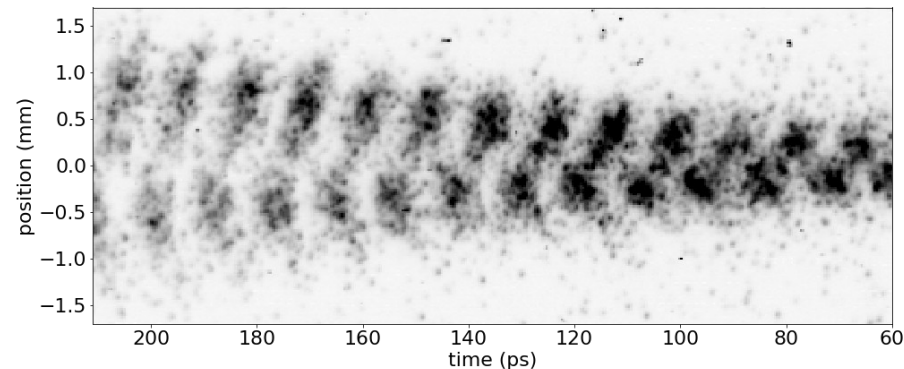
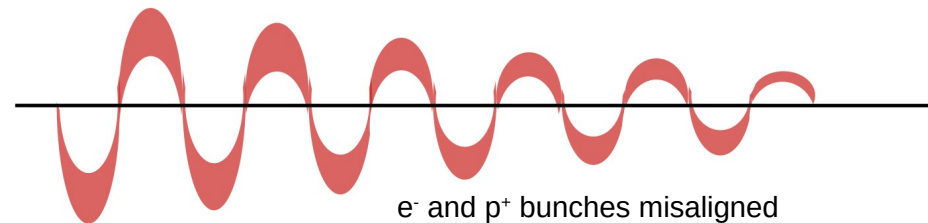
$e^-$  and  $p^+$  bunches misaligned  
force on  $p^+$  bunch centroid  $\neq 0 \rightarrow$  hosing  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing



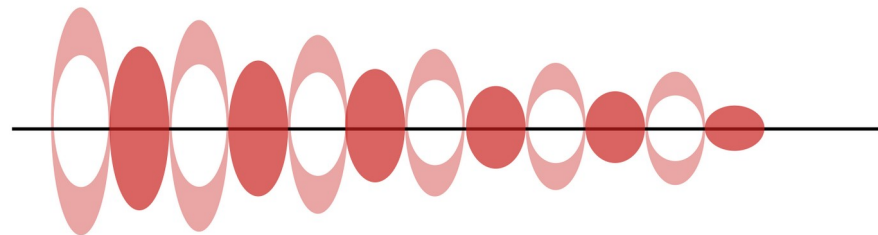
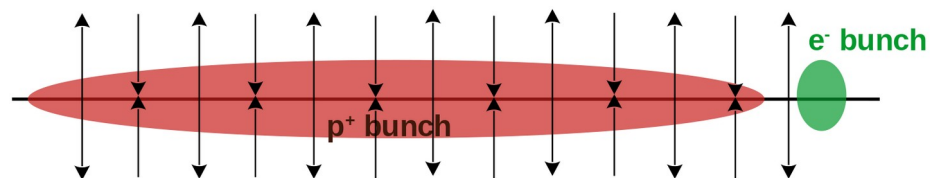
Hosing + eSSM

one plane

plane  $\perp$  hosing



# eSSM vs eSSM+Hosing



$e^-$  and  $p^+$  bunches aligned  
force on  $p^+$  bunch centroid = 0  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing



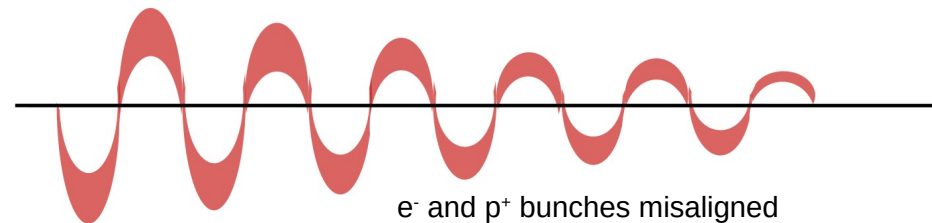
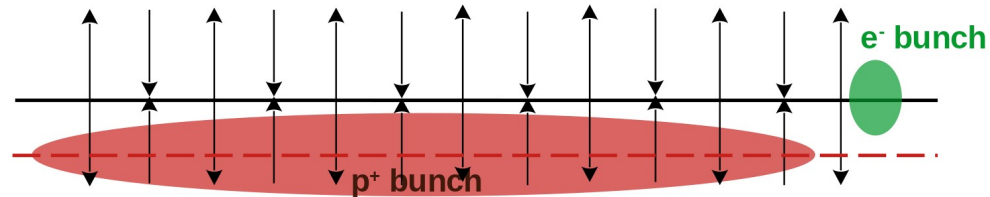
eSSM

- Hosing occurs in the plane of misalignment

- Plane of misalignment  $\neq$  main plane of observation?



- Need a **method to look at two (or more) planes simultaneously**



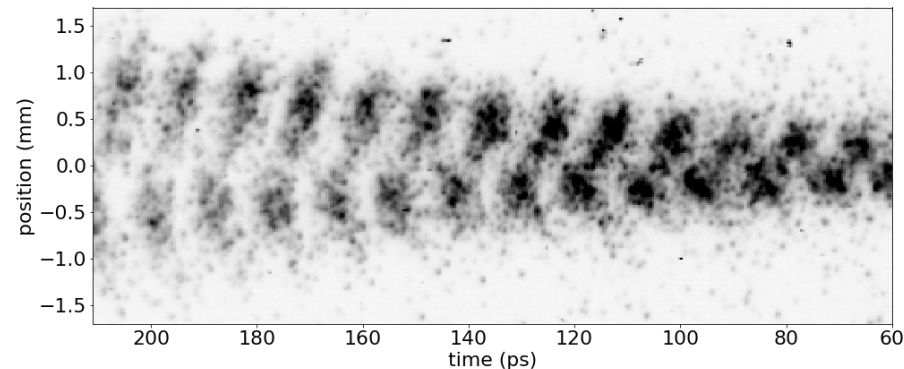
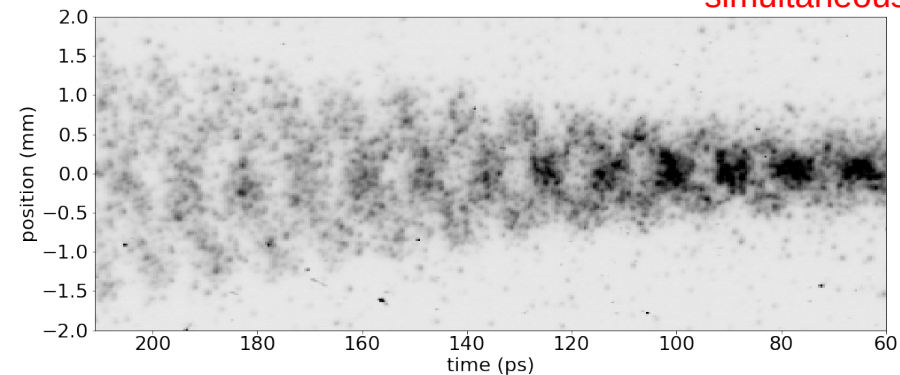
$e^-$  and  $p^+$  bunches misaligned  
force on  $p^+$  bunch centroid  $\neq 0 \rightarrow$  hosing  
force on  $p^+$  bunch slice  $\rightarrow$  focusing/defocusing



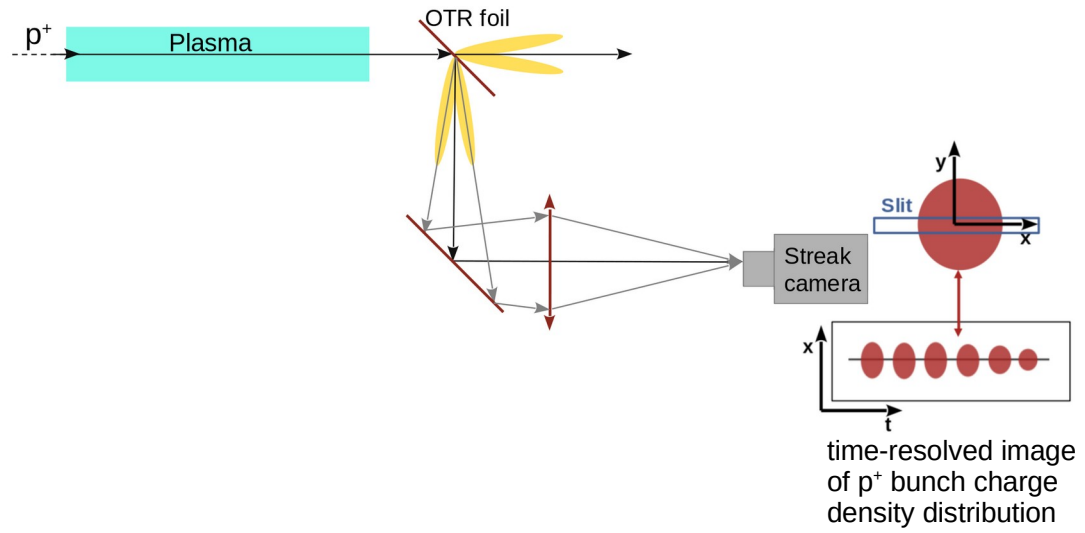
Hosing + eSSM

one plane

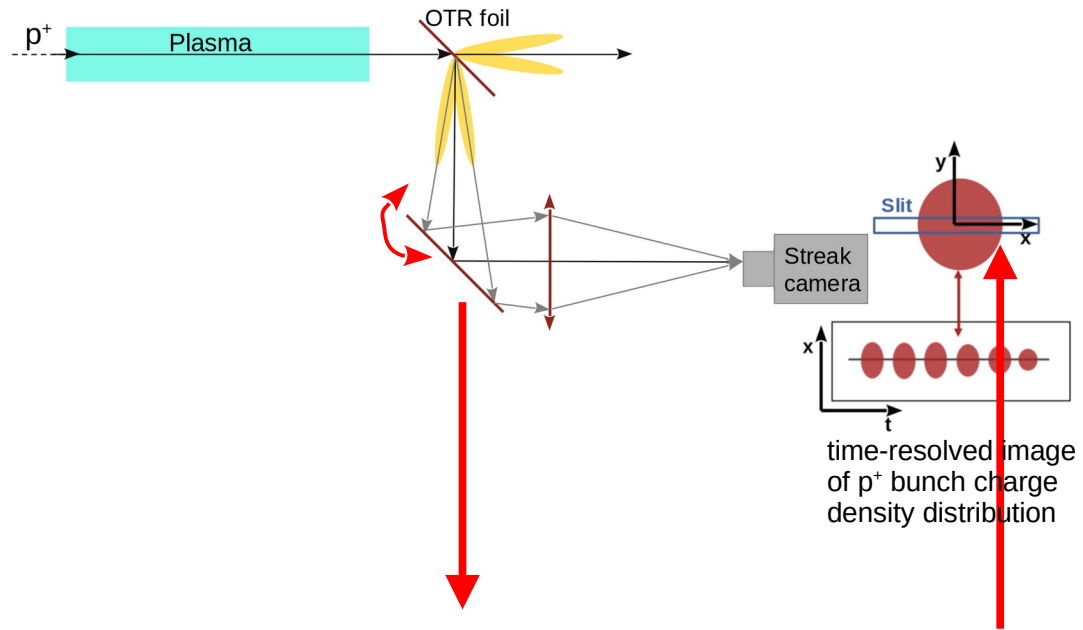
plane  $\perp$  hosing



# Method

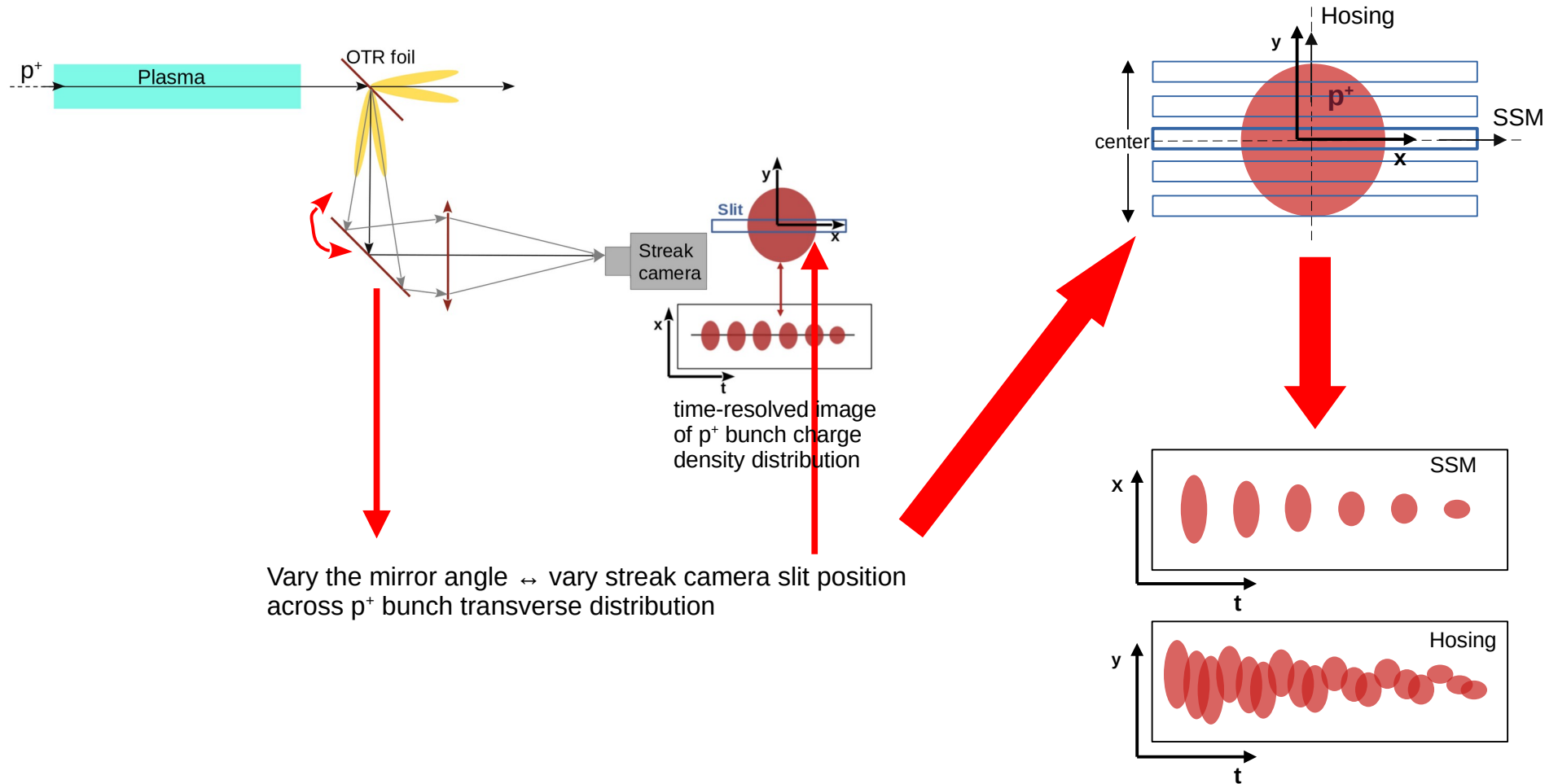


# Method



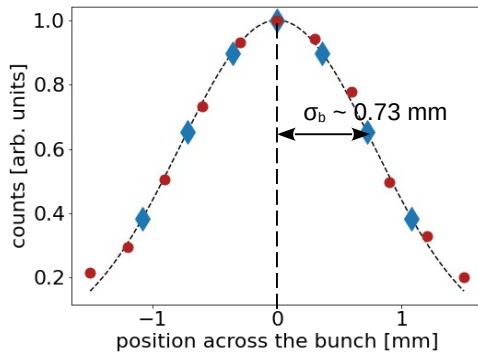
Vary the mirror angle  $\leftrightarrow$  vary streak camera slit position  
across  $p^+$  bunch transverse distribution

# Method



# Results

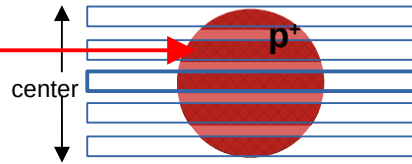
1.
  - Vary mirror angle →
  - Time-integrated  $p^+$  bunch charge density distribution as a function of position across the bunch →
  - Find central point
  - Determine positions where to take data



• – summed charge density

♦ – positions where slices of

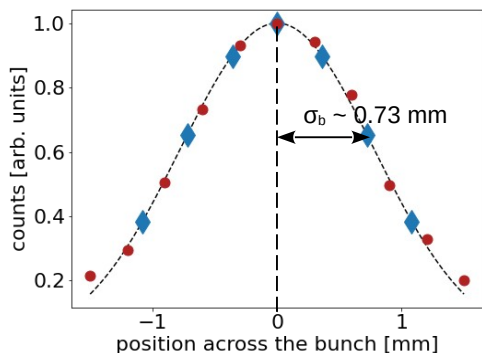
$p^+$  bunch charge density  
distribution are recorded



Step size –  $0.5\sigma_b$

# Results

- Vary mirror angle →
  - Time-integrated  $p^+$  bunch charge density distribution as a function of position across the bunch →
  - Find central point
  - Determine positions where to take data

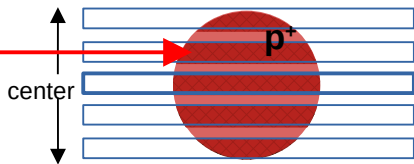


● – summed charge density

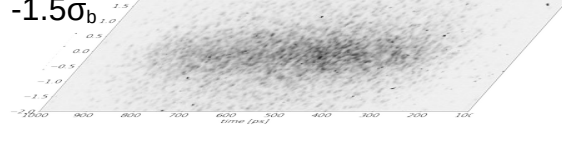
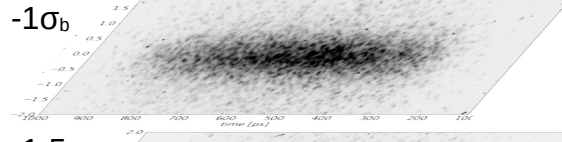
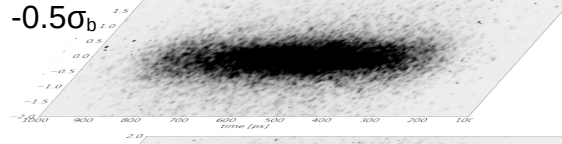
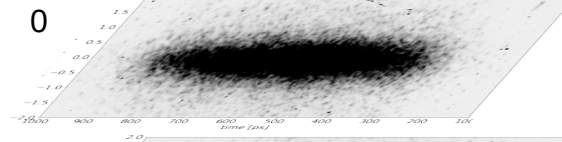
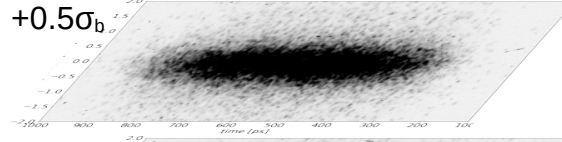
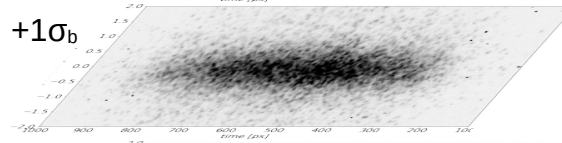
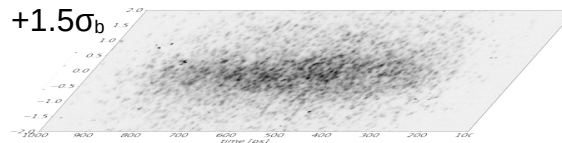
◆ – positions where slices of

$p^+$  bunch charge density distribution are recorded

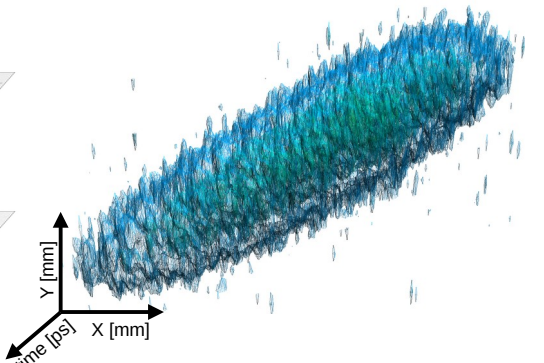
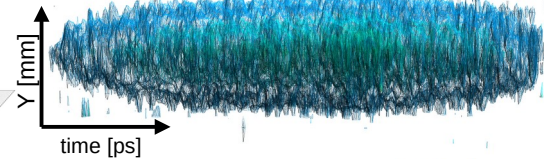
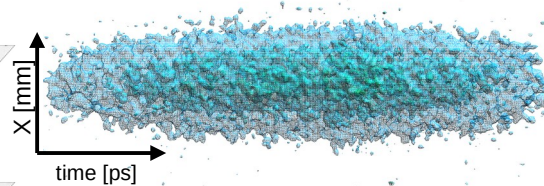
Step size –  $0.5\sigma_b$



- Do a test →
  - Incoming  $p^+$  bunch (propagating as if in vacuum)

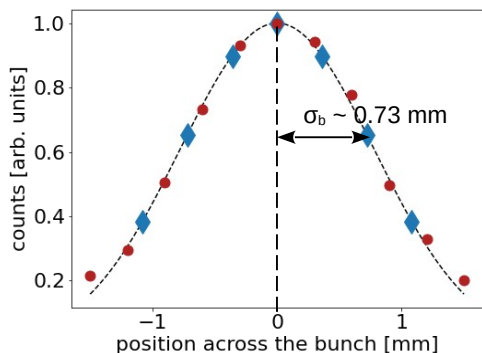


• Slices placed in linear rectangular grid → 3D distribution



# Results

- Vary mirror angle  $\rightarrow$
  - Time-integrated  $p^+$  bunch charge density distribution as a function of position across the bunch  $\rightarrow$
  - Find central point
  - Determine positions where to take data

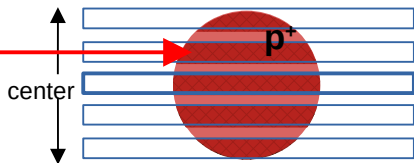


• – summed charge density

◆ – positions where slices of

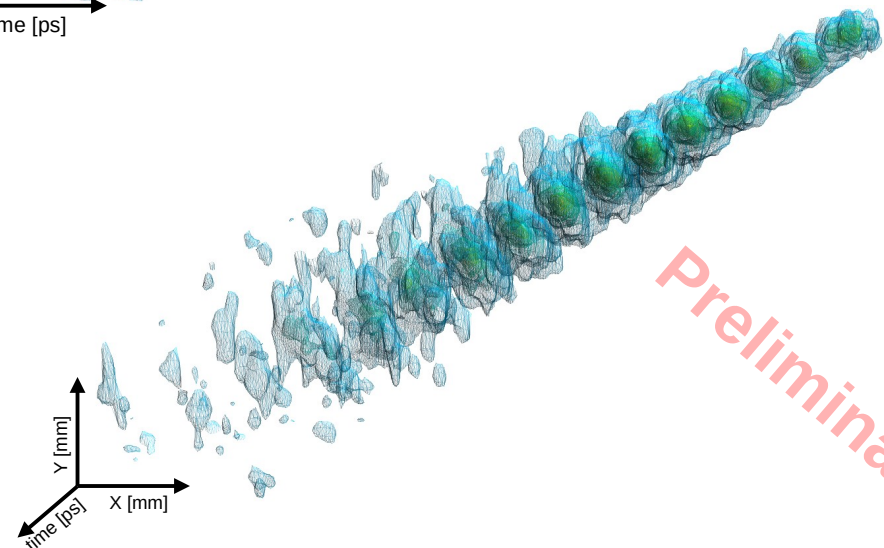
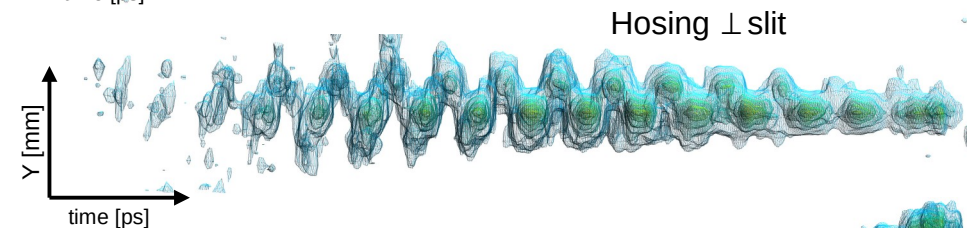
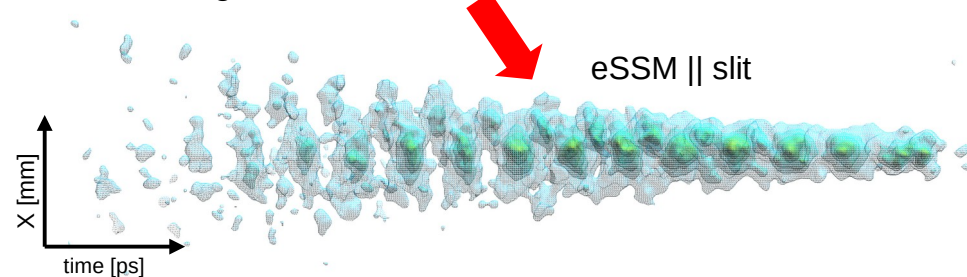
$p^+$  bunch charge density distribution are recorded

Step size –  $0.5\sigma_b$



- $p^+$  bunch in plasma  $\rightarrow$

- Misalign  $e^-$  bunch  $\perp$  slit



Preliminary

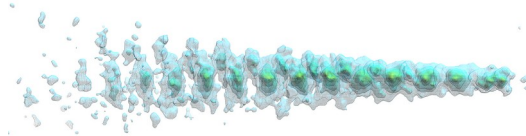
# Conclusion

- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

# Conclusion

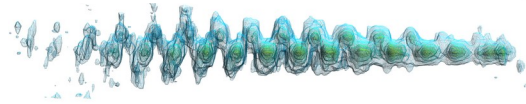
- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

- $e^-p^+$  aligned → eSSM

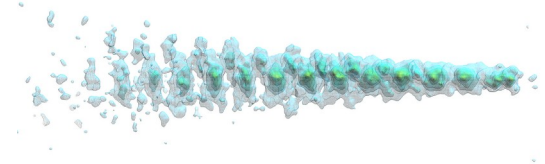


→ in all planes

- $e^-p^+$  misaligned → Hosing + eSSM



+



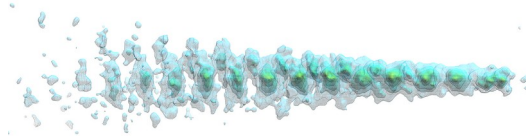
- Hosing occurs in the plane of misalignment → if not main plane of observation → can be unnoticed



# Conclusion

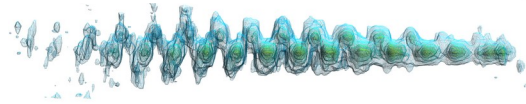
- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

- $e^-$ - $p^+$  aligned → eSSM

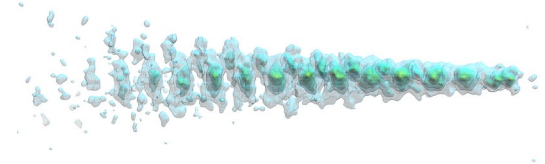


→ in all planes

- $e^-$ - $p^+$  misaligned → Hosing + eSSM



+

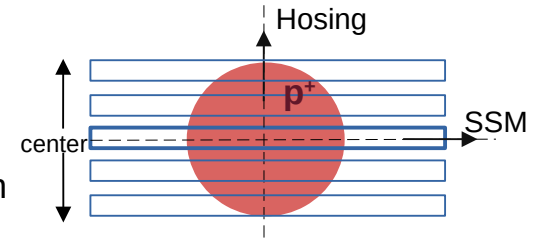


- Hosing occurs in the plane of misalignment → if not main plane of observation → can be unnoticed



- Develop a method for simultaneous observation of two (or more) planes

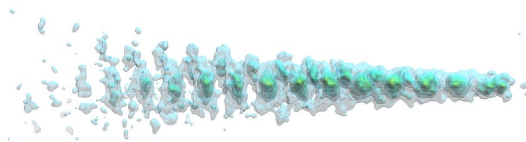
- Do a “streak camera slit scan” across the transverse  $p^+$  bunch charge density distribution



# Conclusion

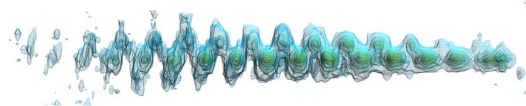
- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

- $e^-p^+$  aligned → eSSM

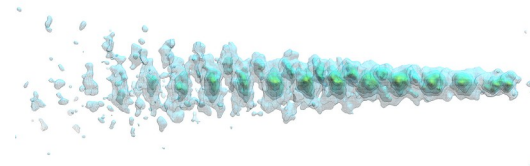


→ in all planes

- $e^-p^+$  misaligned → Hosing + eSSM



+



- Hosing occurs in the plane of misalignment → if not main plane of observation → can be unnoticed

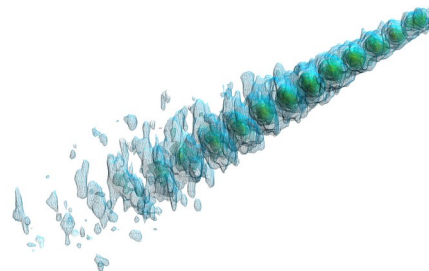
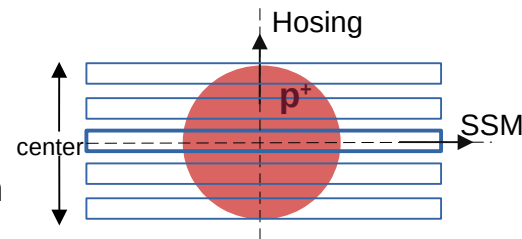


- Develop a method for simultaneous observation of two (or more) planes

- Do a “streak camera slit scan” across the transverse  $p^+$  bunch charge density distribution

- Test with the incoming  $p^+$  bunch (no plasma)

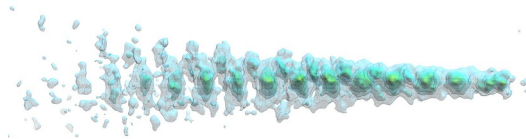
- Test with the  $p^+$  bunch in plasma: Hosing  $\perp$  slit and eSSM  $\parallel$  slit



# Conclusion

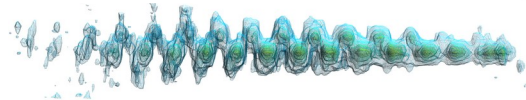
- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

- $e^-p^+$  aligned → eSSM

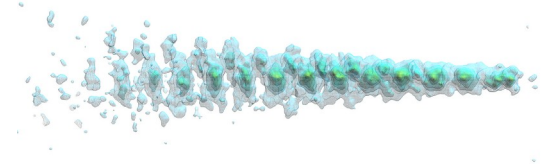


→ in all planes

- $e^-p^+$  misaligned → Hosing + eSSM



+



- Hosing occurs in the plane of misalignment → if not main plane of observation → can be unnoticed



- Develop a method for simultaneous observation of two (or more) planes

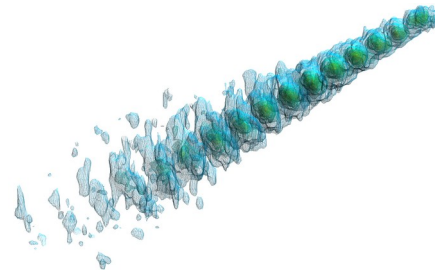
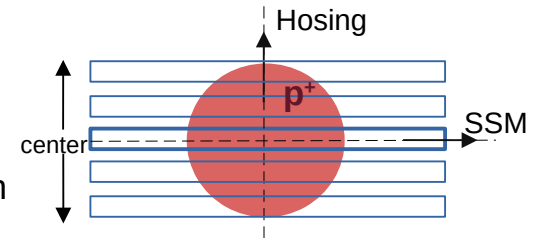
- Do a “streak camera slit scan” across the transverse  $p^+$  bunch charge density distribution

- Test with the incoming  $p^+$  bunch (no plasma)

- Test with the  $p^+$  bunch in plasma: Hosing  $\perp$  slit and eSSM  $\parallel$  slit

- Apply to future studies of simultaneous occurrence of hosing and eSSM

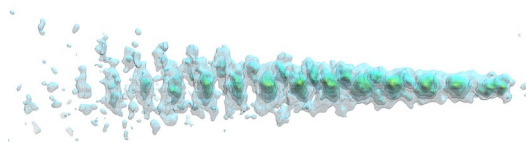
- Is eSSM-only possible?



# Conclusion

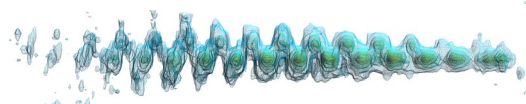
- AWAKE: seeding of self-modulation with  $e^-$  bunch → alignment-sensitive

- $e^-p^+$  aligned → eSSM

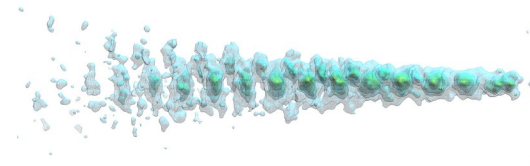


→ in all planes

- $e^-p^+$  misaligned → Hosing + eSSM



+

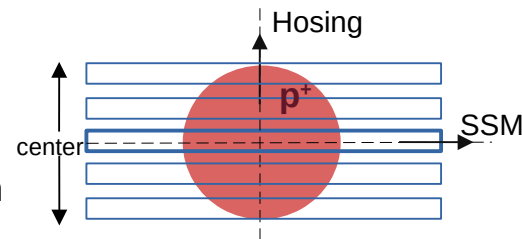


- Hosing occurs in the plane of misalignment → if not main plane of observation → can be unnoticed



- Develop a method for simultaneous observation of two (or more) planes

- Do a “streak camera slit scan” across the transverse  $p^+$  bunch charge density distribution

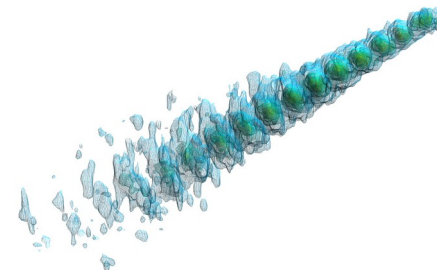


- Test with the incoming  $p^+$  bunch (no plasma)

- Test with the  $p^+$  bunch in plasma: Hosing  $\perp$  slit and eSSM  $\parallel$  slit

- Apply to future studies of simultaneous occurrence of hosing and eSSM

- Is eSSM-only possible?



**Thank you for your attention!**