



# Compensation of insertion device induced emittance variations in ultralow emittance storage rings

**Fernando Sannibale**

IPAC 18

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U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science



# Content

- Problem definition.
- Possible compensation schemes:
  - Use a variable gap wiggler to generate emittance.
  - Use of a “dispersion bump” inside a wiggler with gap at a fixed position.
  - Compensation by small variation of the beam momentum.
  - Using intra-beam scattering (IBS).
- Final Considerations.

# The MBA Lattice Revolution



Tens of pm emittances, orders of magnitude brightness increase, approaching fully photon coherence in the transverse plane!

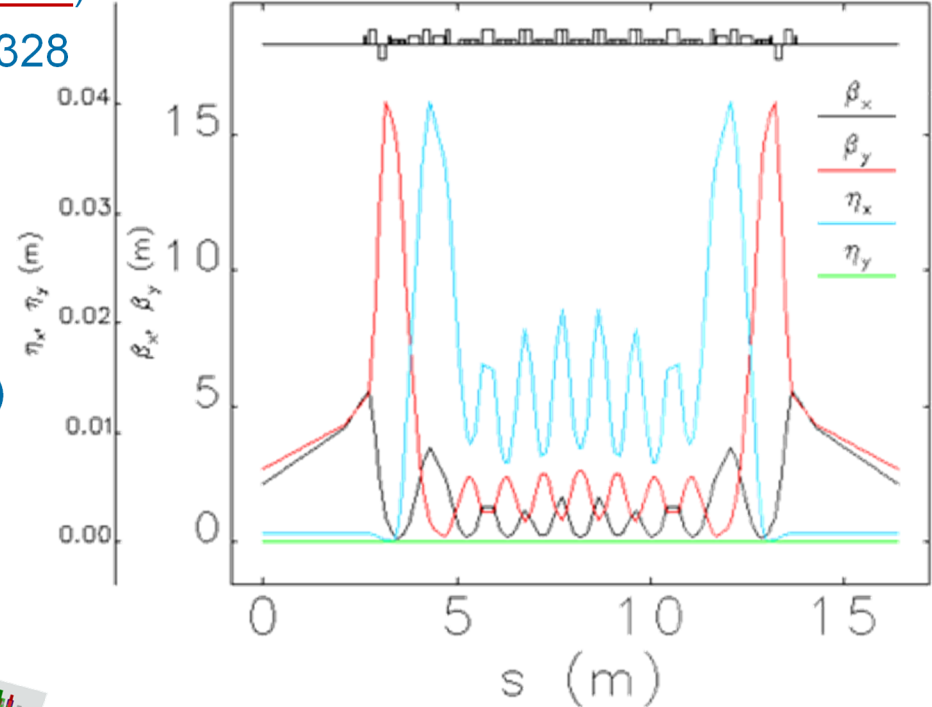
# Ultra-Low Emittance MBA Lattices



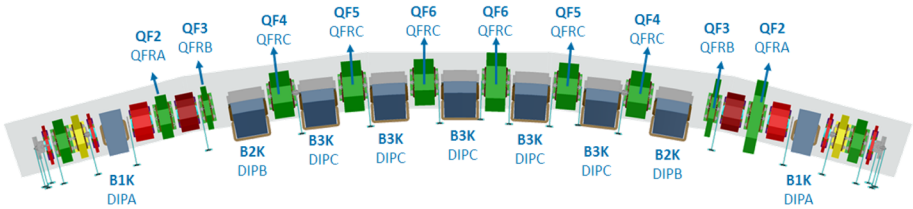
# Ultra-Low Emittance MBA Lattices

Example: ALS-U 9BA Lattice v18\_127 (obsolete)

- 1.15 nC/bunch - 2 GeV - L = 196.5 m - h = 328
- Dipole:  $\rho = 8.6 \text{ m}$  ;  $k_1 = -7 \text{ m}^{-2}$ ;  $\theta = 3.33 \text{ deg}$
- $\varepsilon_0 = 109 \text{ pm}$  (no IBS) – 12 super-periods
- Full coupling:
- $\varepsilon_x = \varepsilon_y = 81.32 \text{ pm}$  (with IBS and harm. cav.)
- $\sigma_z = 14.56 \text{ mm}$  (with IBS and harm. cavities)
- $\delta_0 = 0.0828\%$  -  $U_0 = 181.9 \text{ keV}$  (no IDs)
- $\alpha_c = 2.68 \cdot 10^{-4}$  -  $j_x = 1.865$



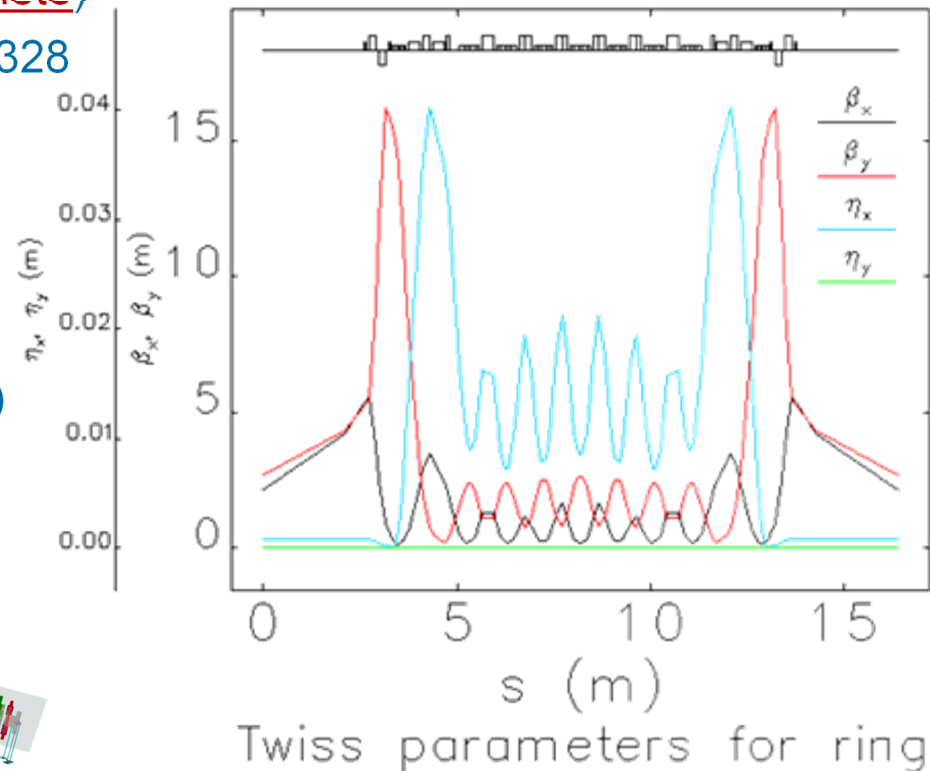
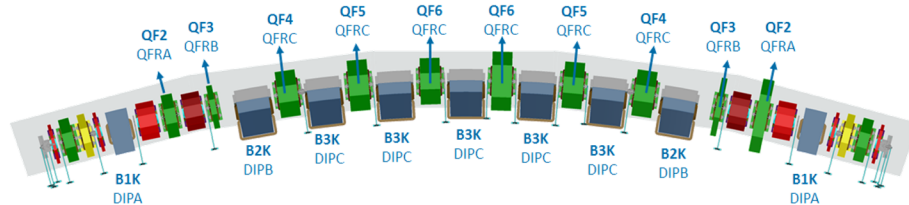
Twiss parameters for ring



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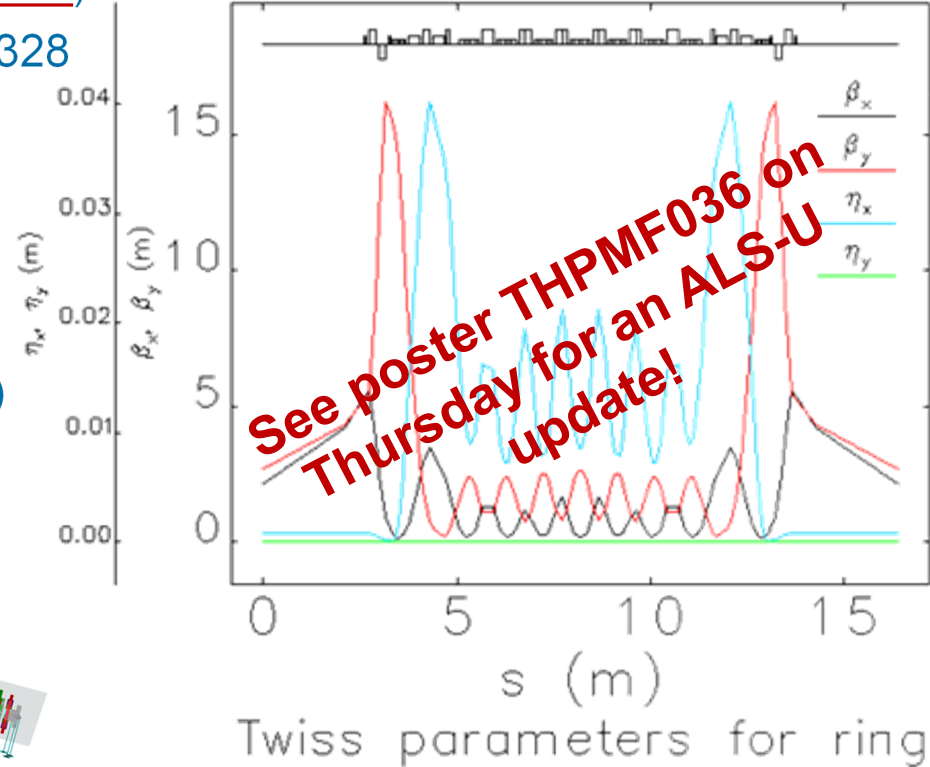
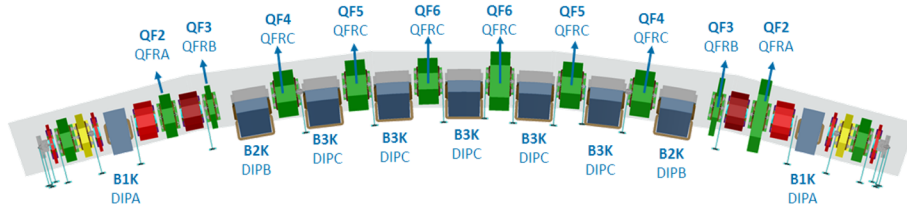
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In this situation, the IDs' contribution significantly contributes to radiation damping and hence **in defining the ring natural emittance**.

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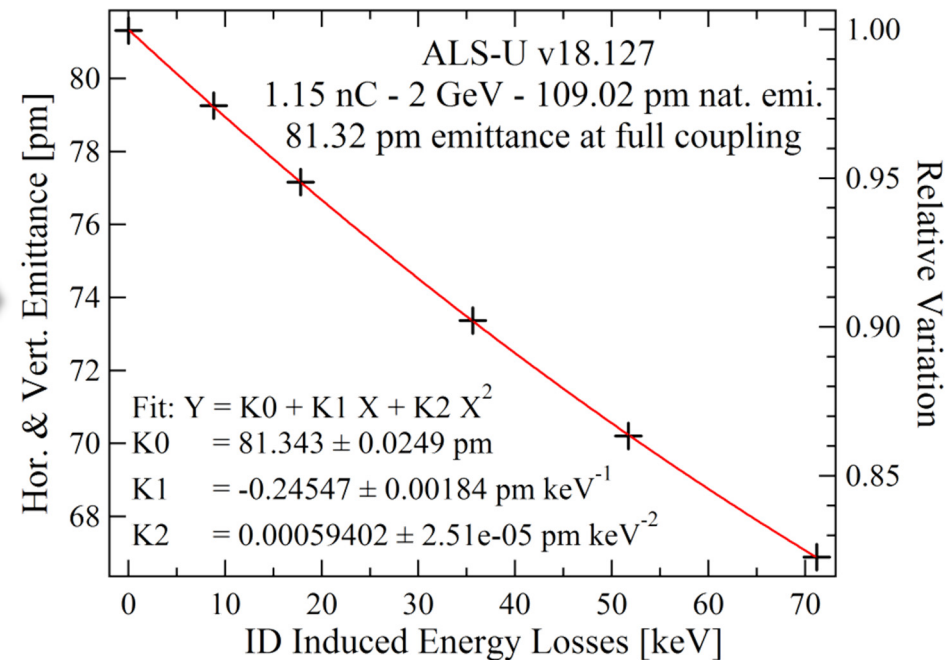
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# Significant Emittance Dependence on IDs



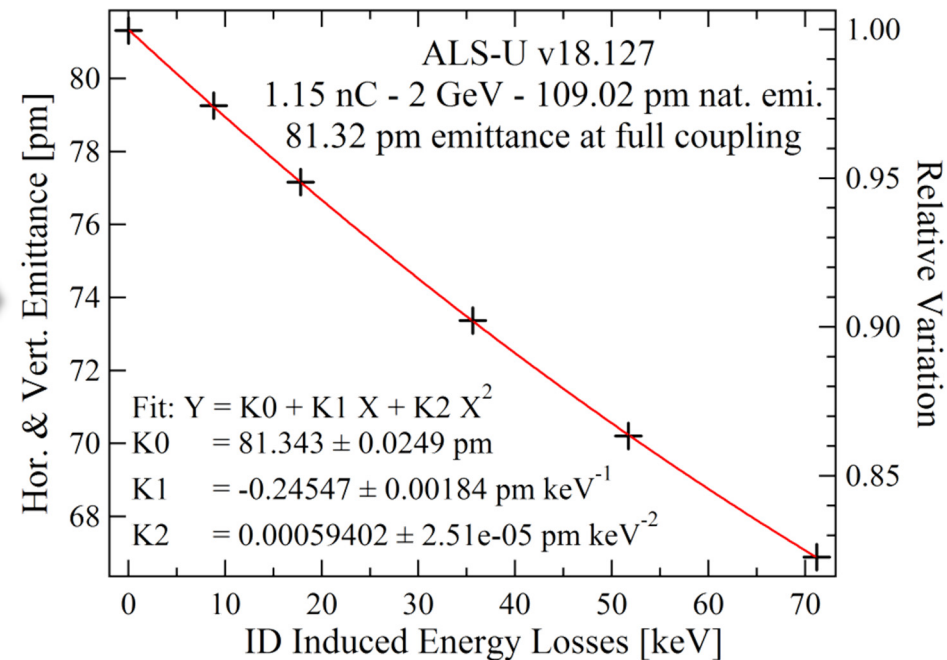
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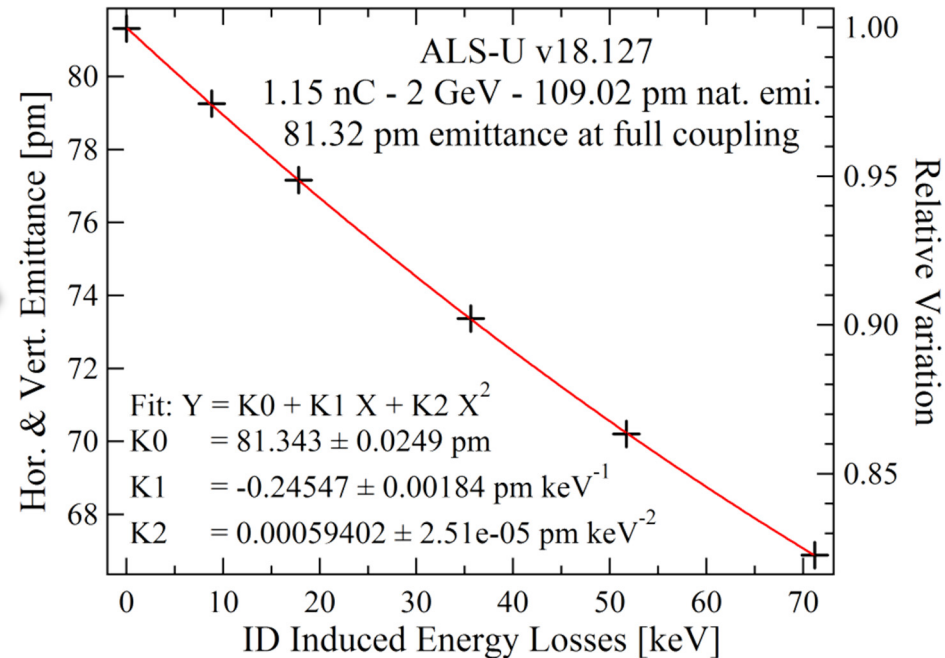
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How large are ID induced energy losses in a real ring?

# Example of ID Induced Energy Losses in a Ring

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## ALS Insertion Devices

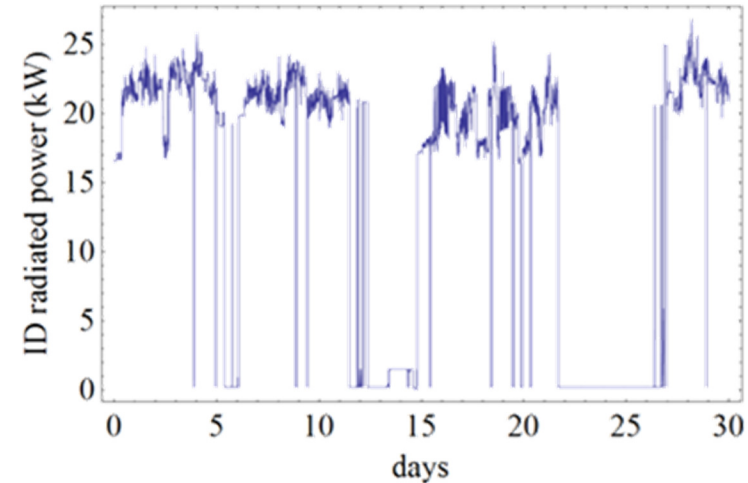
Name	Alias	BL	New?	$\lambda_u$ (mm)	BX <sub>max</sub> (T)	BX <sub>min</sub> (T)	BY <sub>max</sub> (T)	BY <sub>min</sub> (T)	No. periods
EPU50		4.0.2	No	50	0.58	0.1	0.8	0.1	37
QEPU90	MERLIN	4.0.3	No	90	0.78	0.06	1.18	0.06	20.5
U114		5.0.1	No	114	1.94	0.03	0	0	29
EPU38	COSMIC	7.0.1	No	38	0.89	0.11	0.67	0.11	44.5
EPU70	MAESTRO	7.0.2	No	70	1.18	0.07	0	0	26.5
U50		8.0.1	No	50	0.85	0.1	0	0	80
U100		9.0.1	No	100	0.98	0.05	0	0	43
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EPU50		11.0.1	No	50	0.85	0.1	0.57	0.1	36.5
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ALS data, Start 1 Nov 2017



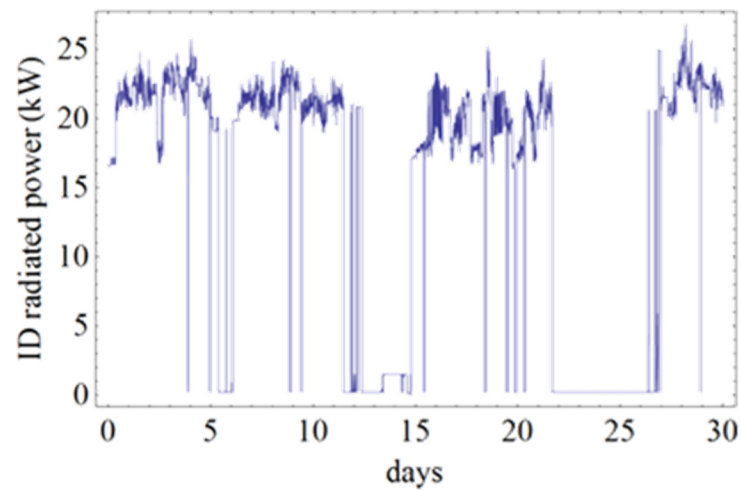
Random ID gaps variation generates random beam radiated power variations.

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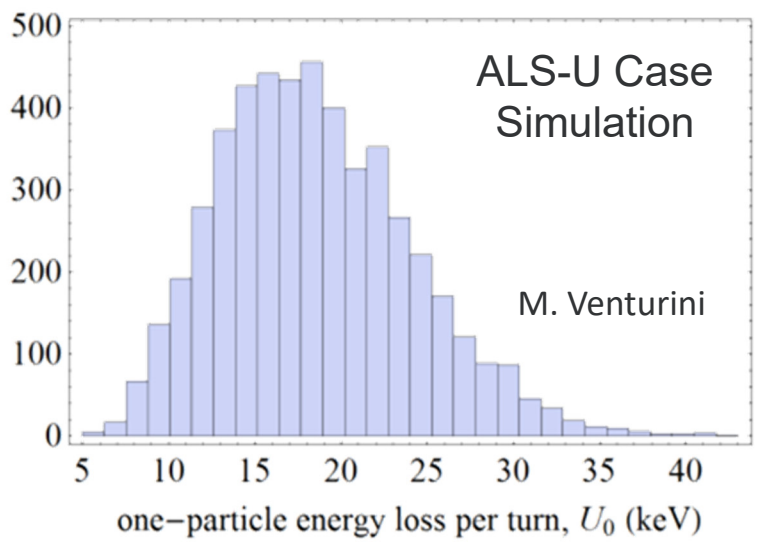
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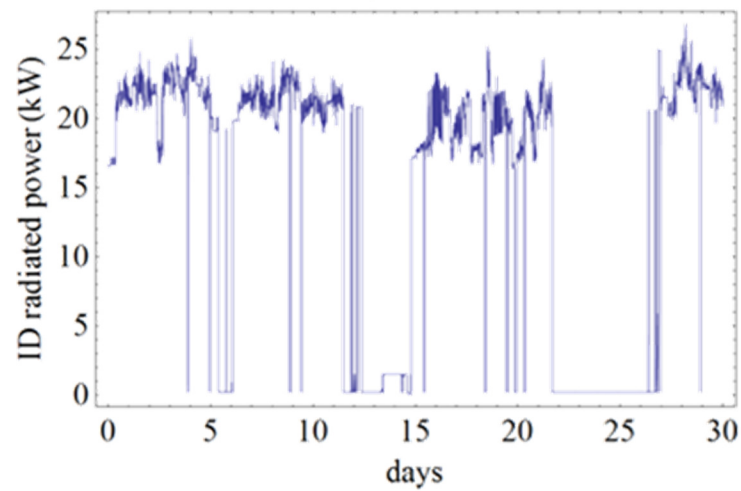


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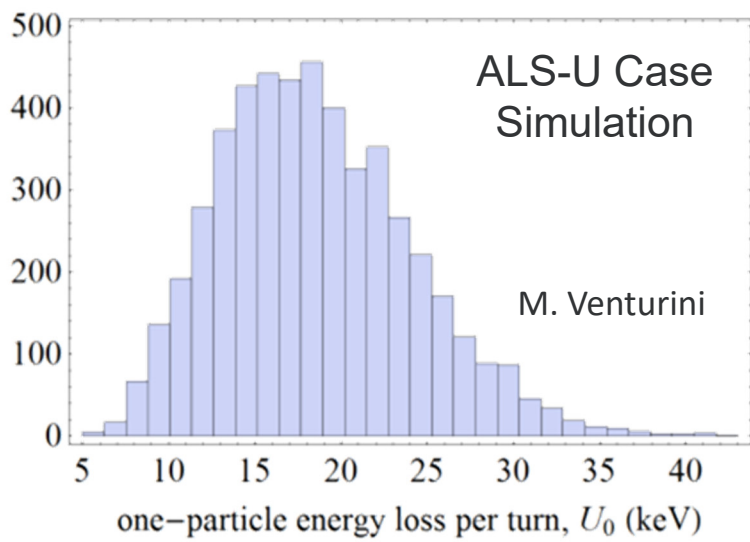
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$$\langle U_0 \rangle = 18.5 \text{ keV}, \sigma_{U_0} = 5.6 \text{ keV}$$



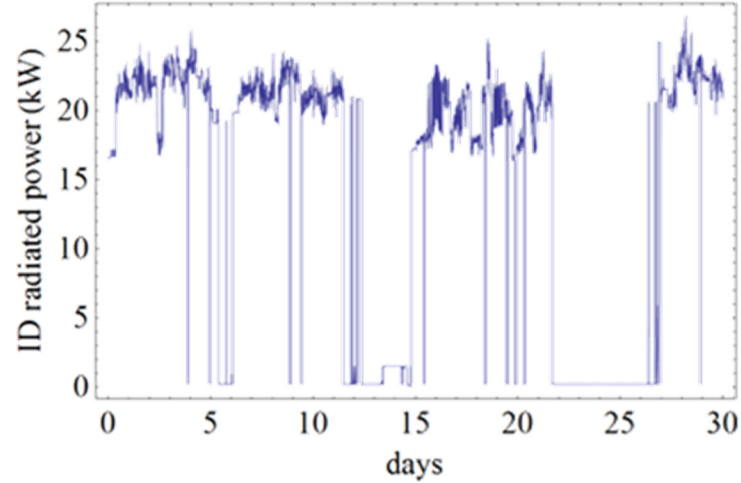
$$\Delta\epsilon/\epsilon \sim 7 \% \quad (4 \text{ sigma})$$

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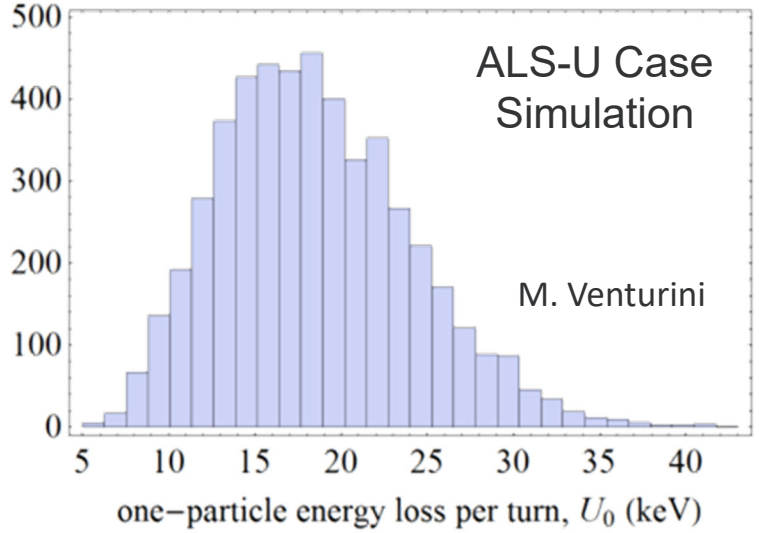
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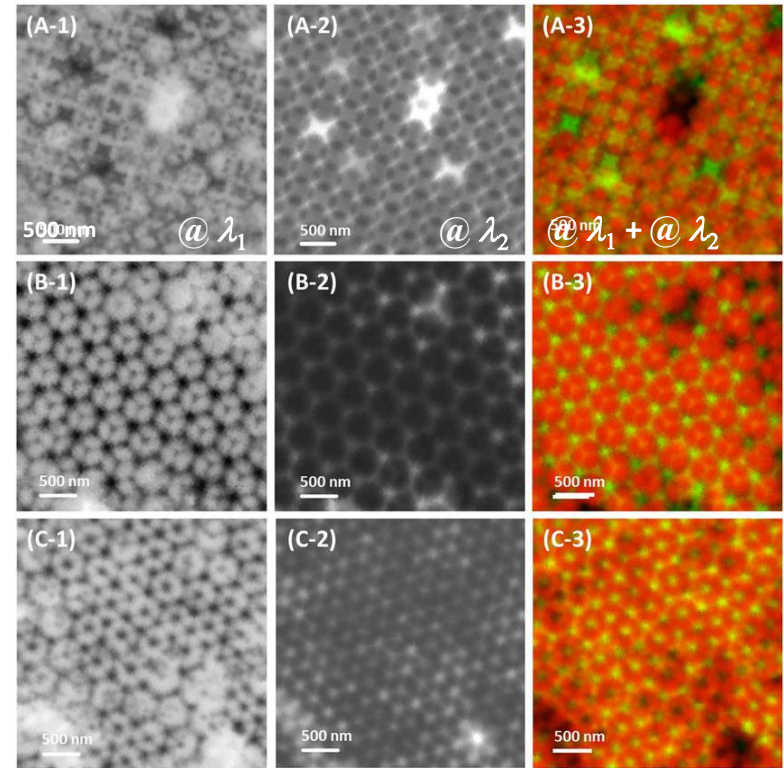
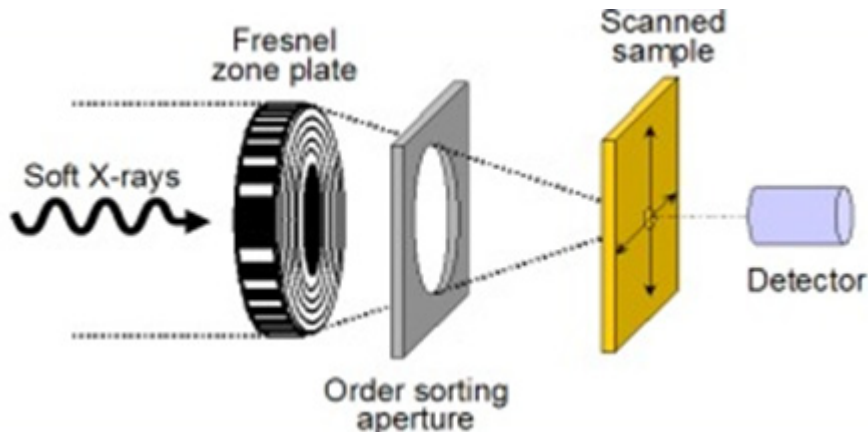
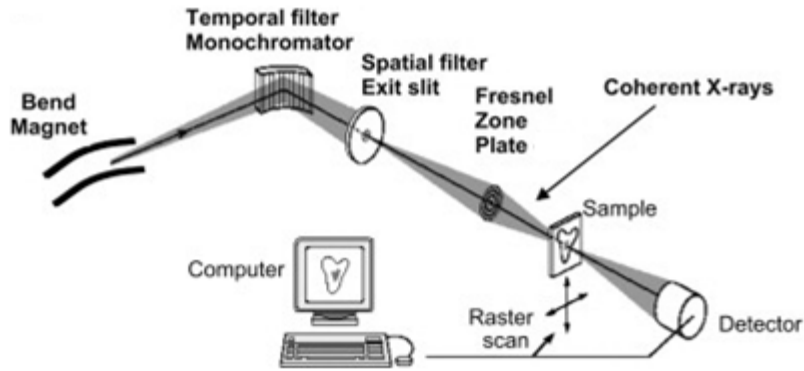


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How important such an emittance variation to experiments?



# STXM- Scanning Transmission X-Ray Microscopy



**Colloid Crystal STXM Image.** H. W. Nho, T. H. Yoon, (2017). Scientific Rep. 7. 10.1038/s41598-017-12831-4.

X-ray microscopy/spectroscopy technique very sensitive to beam size and hence to emittance variations.

# Compensation by Variable Gap Wiggler

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$$U_0 = \frac{C_\gamma}{2\pi} E^4 I_2 \quad C_\gamma = 8.846 \cdot 10^{-5} \text{ m/GeV}^3 \quad I_2 = \oint \frac{ds}{\rho^2} = \frac{B^2 L_w}{2 (B\rho)^2} \quad (\text{wiggler})$$



$$B = 2\pi \frac{mc}{e} \frac{K_w}{\lambda_w} \quad (\text{wiggler})$$

$$U_0 = \pi C_\gamma \left( \frac{m c^2}{e} \right)^4 \gamma^2 \left( \frac{K_w}{\lambda_w} \right)^2 L_w$$

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**ALS Wiggler example:**  $\lambda_w = 0.114 \text{ m}$ ;  $N_{\text{Periods}} = 29$ ;  $L_w = 3.3 \text{ m}$ ;  $K_w = 20.6$ ;  $B_w = 1.94 \text{ T}$ ;

$U_0 = 28.3 \text{ keV @ } 1.9 \text{ GeV}$  or  $31.4 \text{ keV @ } 2 \text{ GeV}$

# Compensation by Local Dispersion Bump in Fixed Gap Wiggler



F. Sannibale – IPAC18, Vancouver, BC Canada, May 2, 2018



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$$I_5 = \oint \frac{\mathcal{H}}{|\rho^3|} ds$$

$$C_q = \frac{55}{32\sqrt{3}} \frac{h}{2\pi mc} \approx 3.832 \times 10^{-13} \text{ m}$$

$$I_4 = \oint \frac{\eta_x}{\rho} \left( \frac{1}{\rho^2} + 2k_1 \right) ds \quad k_1 = \frac{e}{p} \frac{\partial B_y}{\partial x}$$

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$$\rightarrow \Delta I_{5W} \sim \frac{4}{3\pi} \frac{B_W^3}{(B\rho)^3} L_W \langle \gamma_x \rangle \eta_x^2, \quad \Delta I_{2W} = 0, \quad \Delta I_{4W} \sim 0$$

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- Potentially compatible with user operation of the wiggler at fixed gap (if wiggler users can accept horizontal beam size variations)

Cons.:

- Requires extra knobs to perform the local dispersion bump.
- Bump size significant. Possible effects on beam dynamics should be evaluated.

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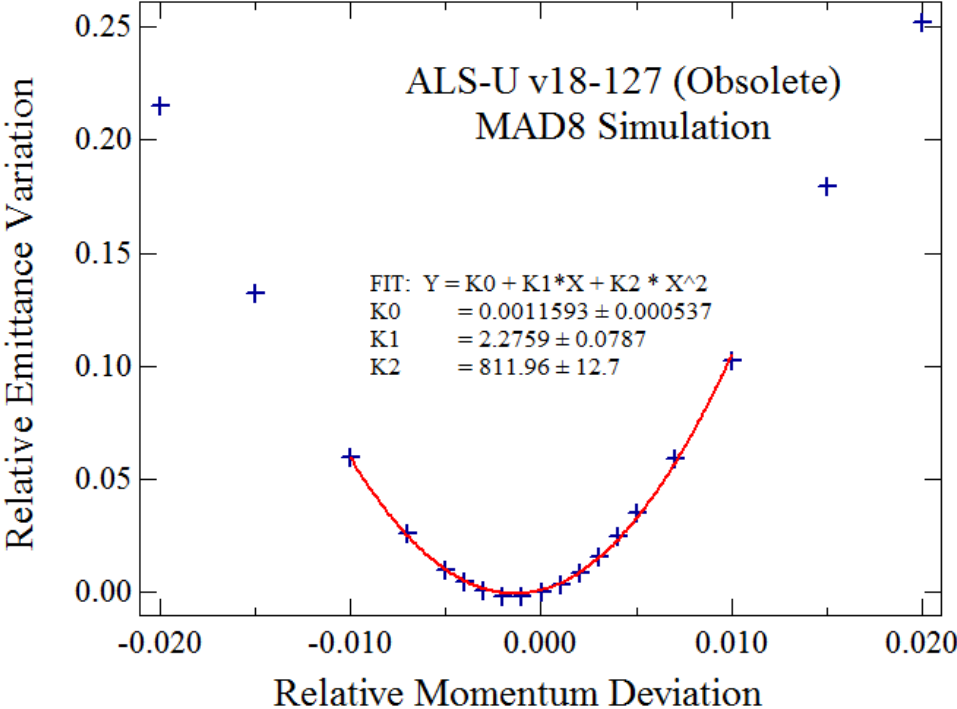
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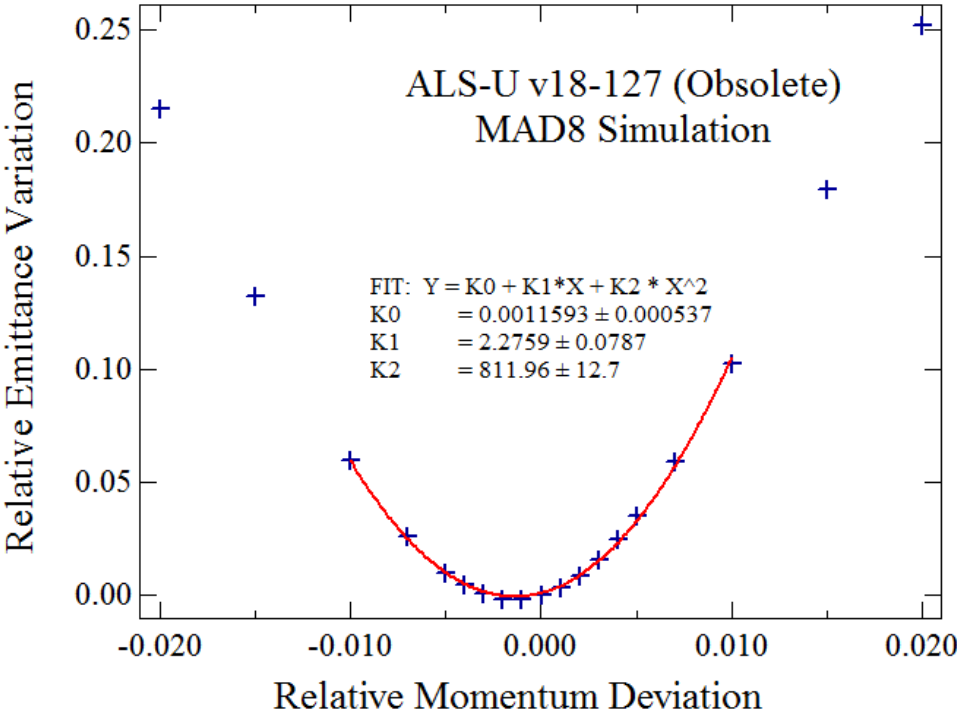
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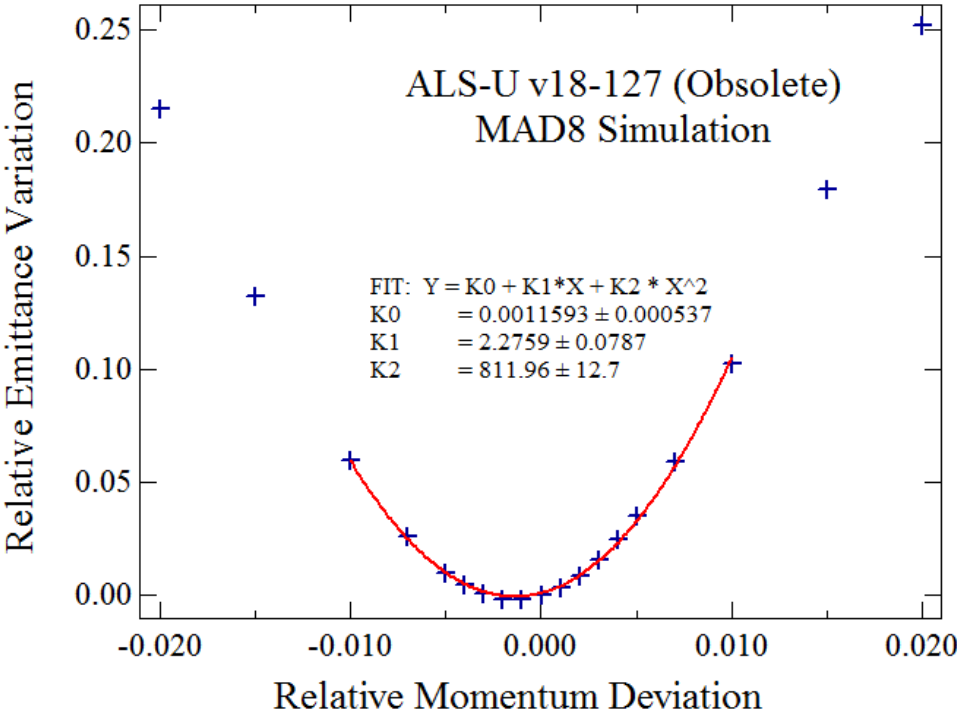
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The scheme it is not practical because it moves source points in dipoles, change the energy of the radiated photons, and can challenge the ring dynamic aperture.



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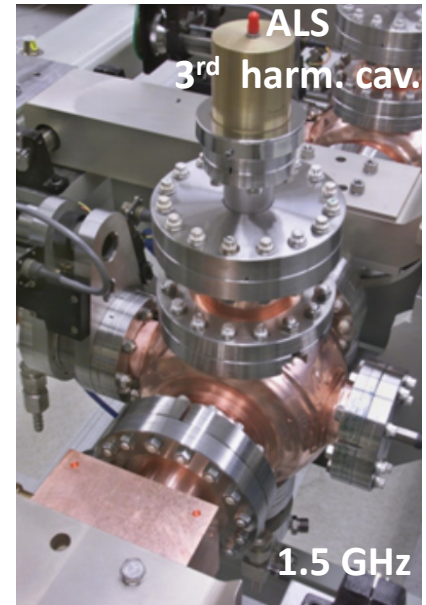
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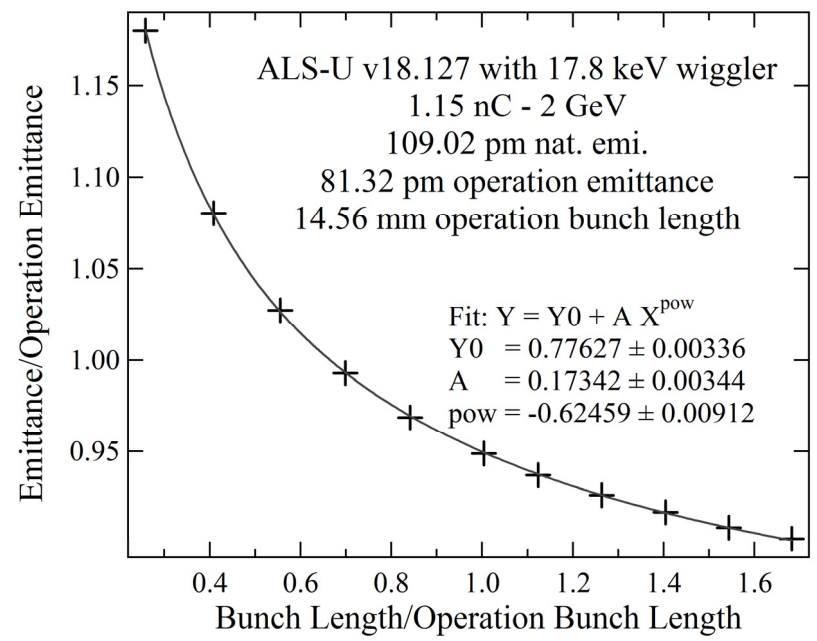
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Harmonic cavities, when present, can be used for that purpose



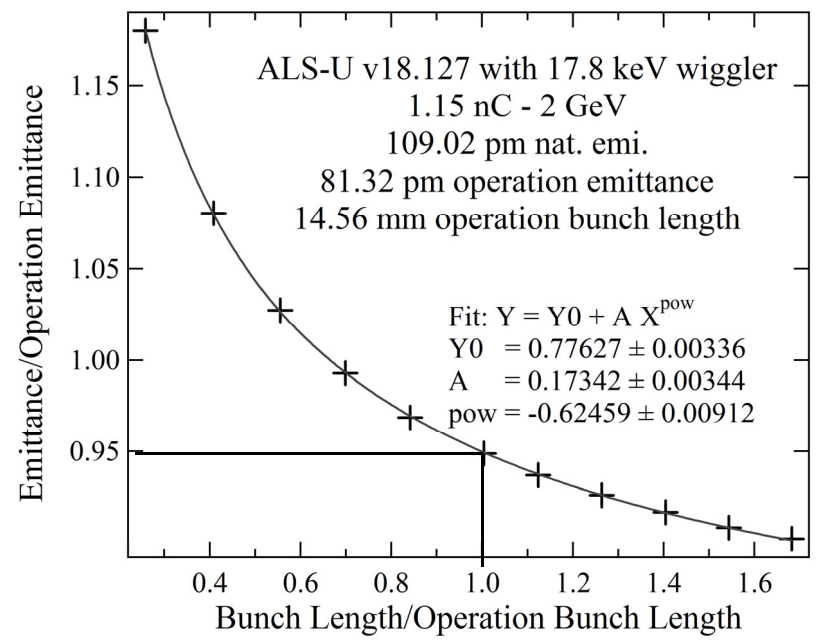
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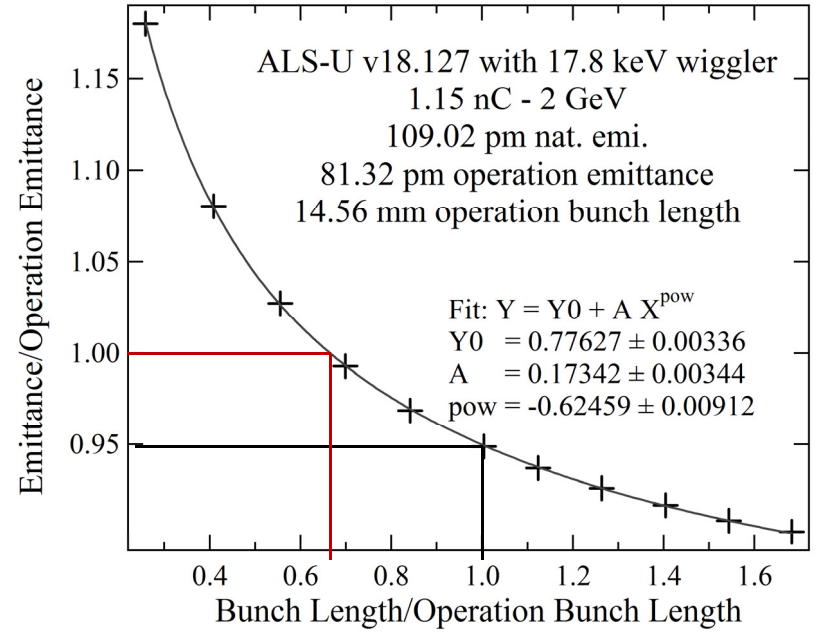
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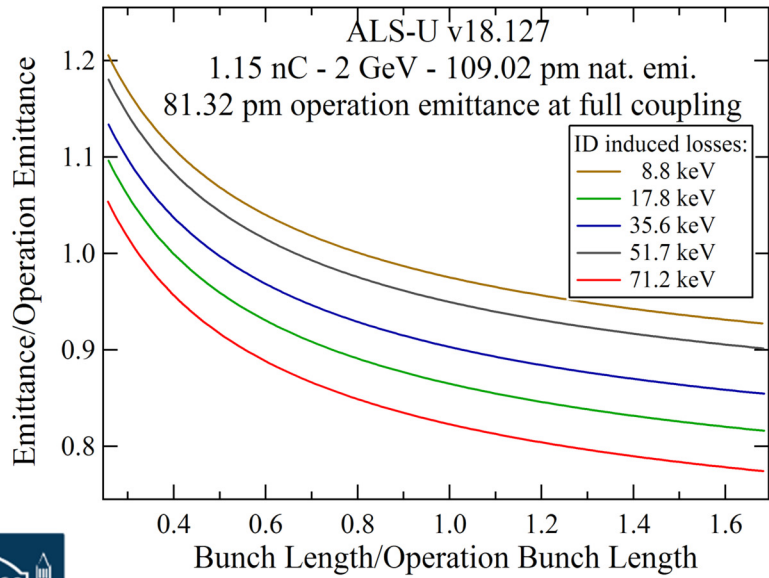
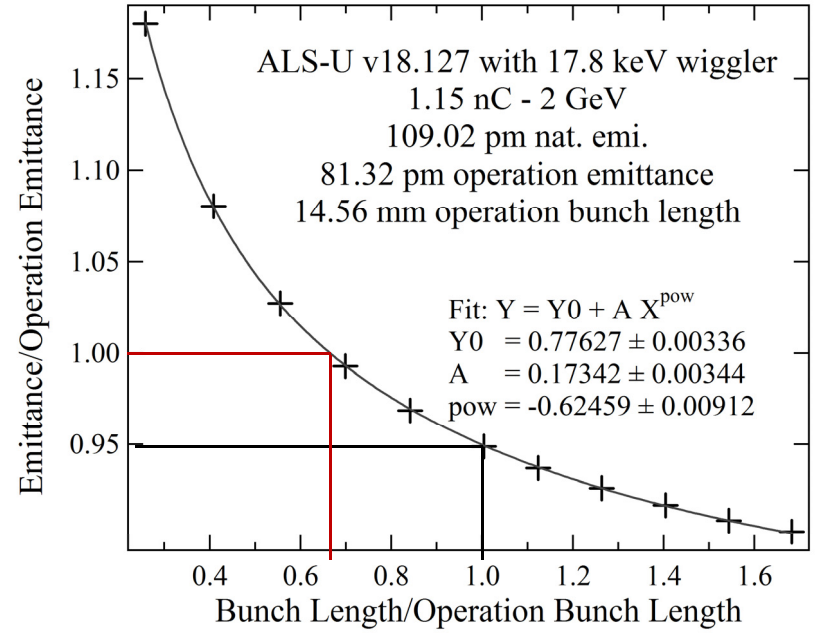
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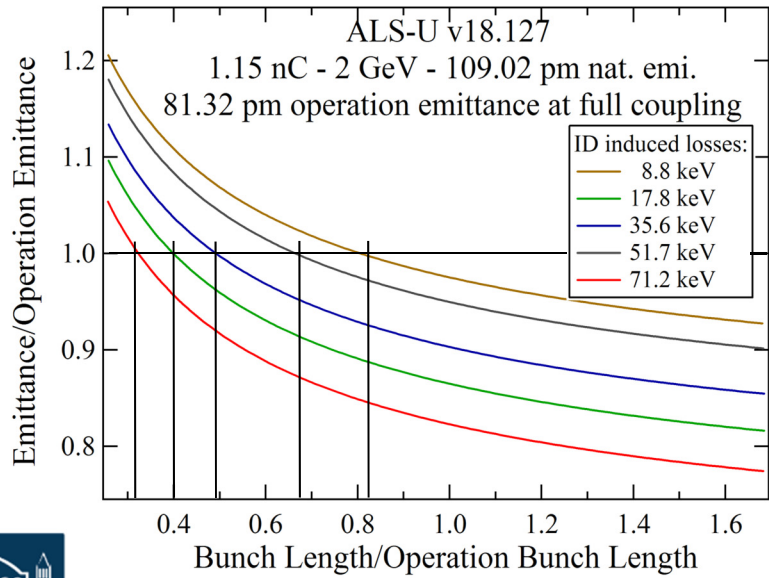
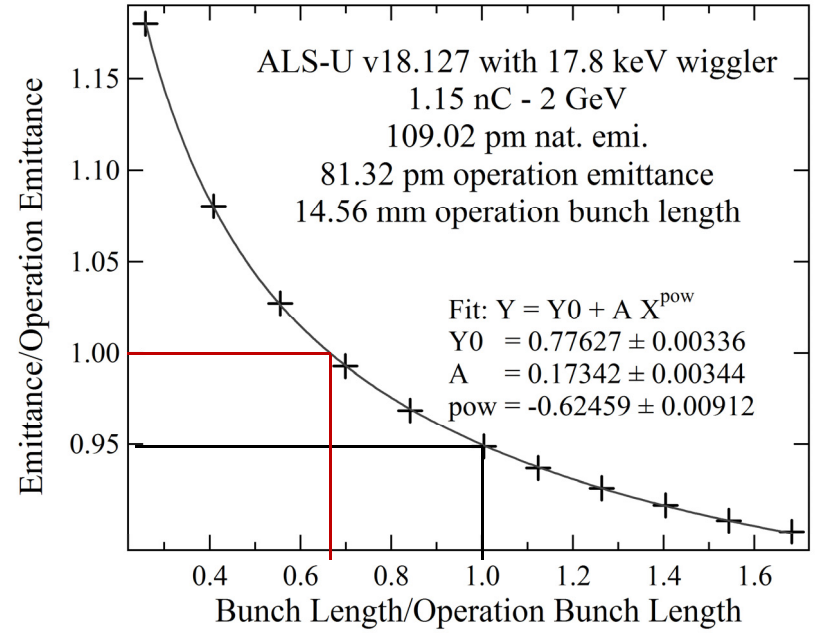
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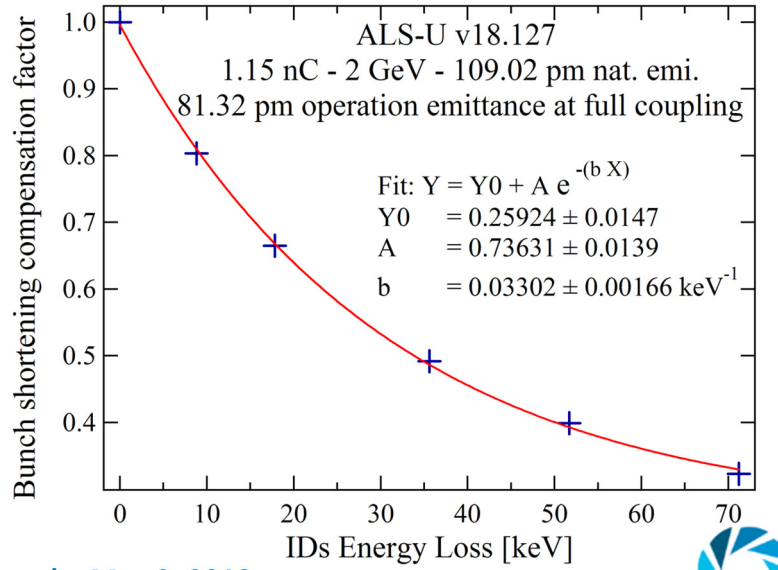
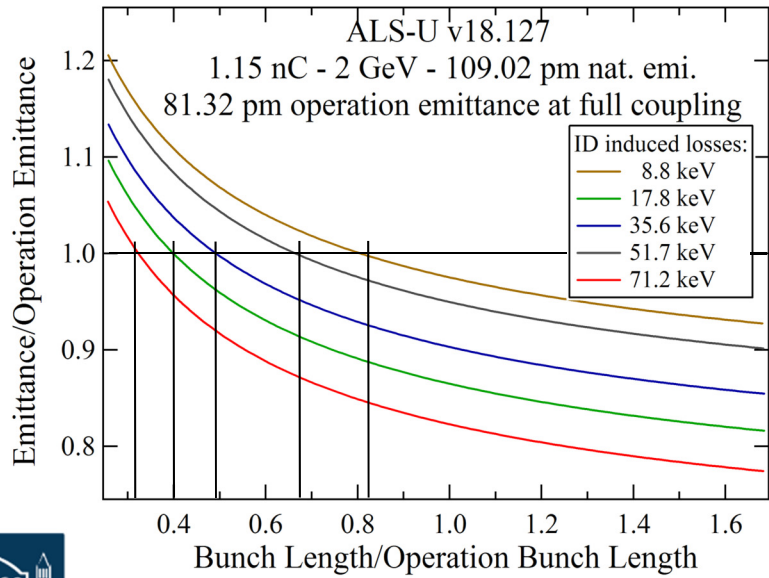
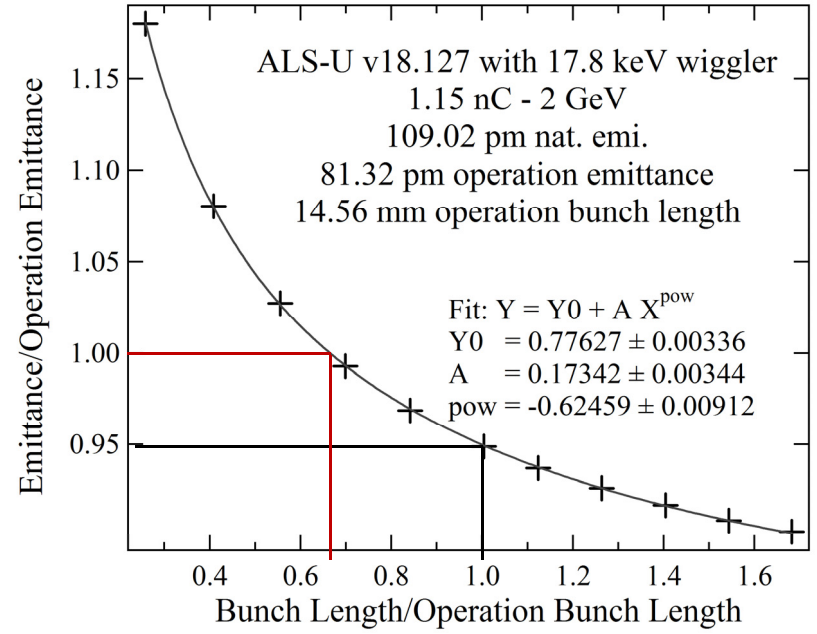
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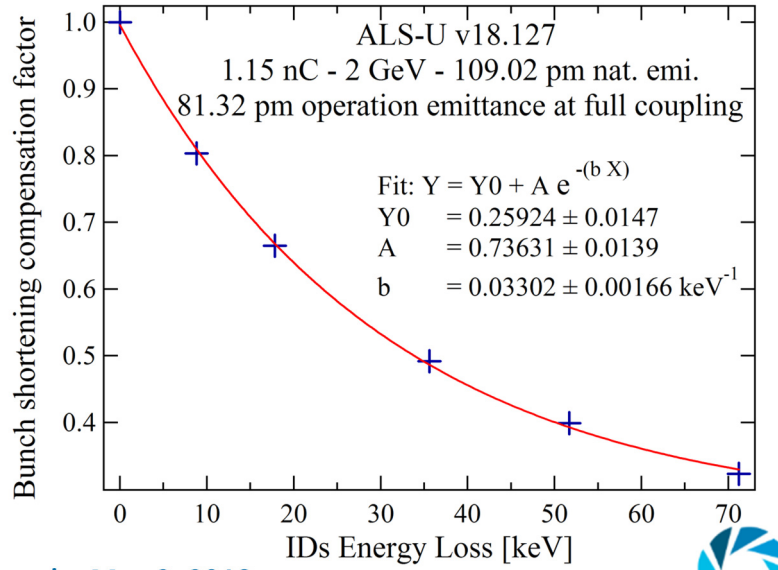
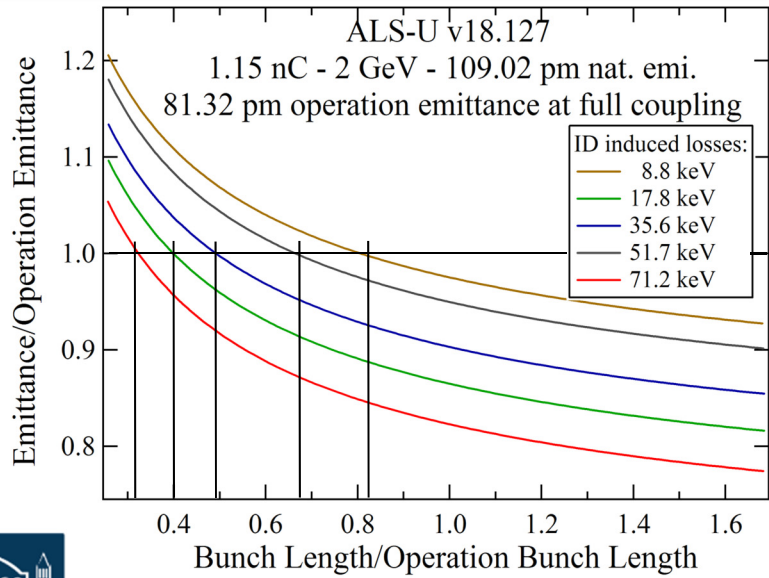
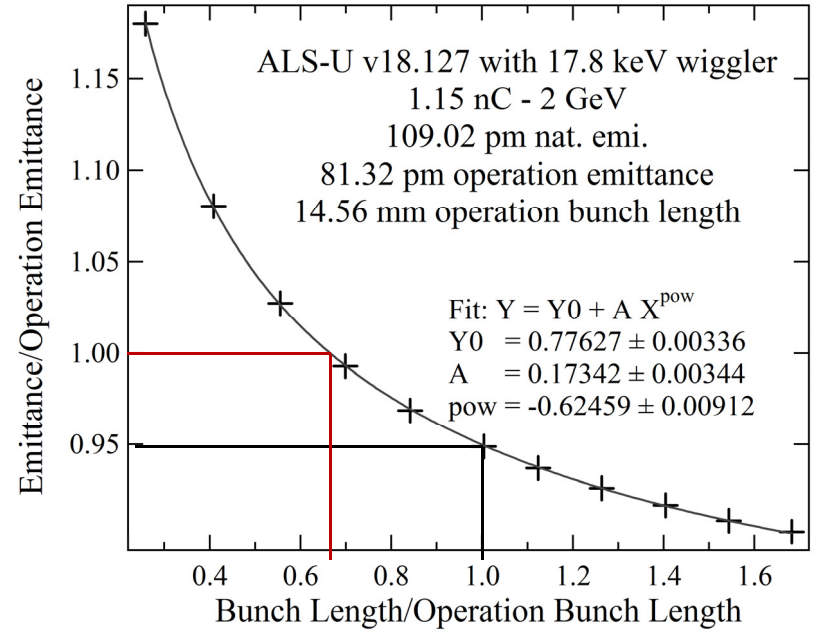
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**Example:** Wigglers tuned for  $\sim 18 \text{ keV}$  losses. Emittance decreases to  $\sim 95\%$  of the no ID value if the bunch length is not changed. To reestablish the emittance to the original value the bunch must be shortened to  $\sim 66\%$  of the no ID value (using the harmonic cavities). **Lifetime will be also reduced by the same factor!**



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  - Control by IBS requires significant bunch length shortening using harmonic cavities, affecting lifetime and stressing cavity tuning control.