

# Transverse and Longitudinal Bunch-By-Bunch Feedback for Storage Rings

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JASRI / SPring-8

# Outline

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Topics are Focused on feedback for Electron Rings  
(For Hardon Rings, a report later in this session)

FIR filter Coefficients Calculation Method

Front-End with **RF Direct Sampling**

Transverse Feedback for **Hybrid Filling**

**Instability of Feedback** at High Gain

**Instability Free Feedback** with Beam Position data at Multiple Locations

**Single-Loop Two Dimensional** Transverse Feedback

**Two Tunes Control** of Longitudinal Feedback

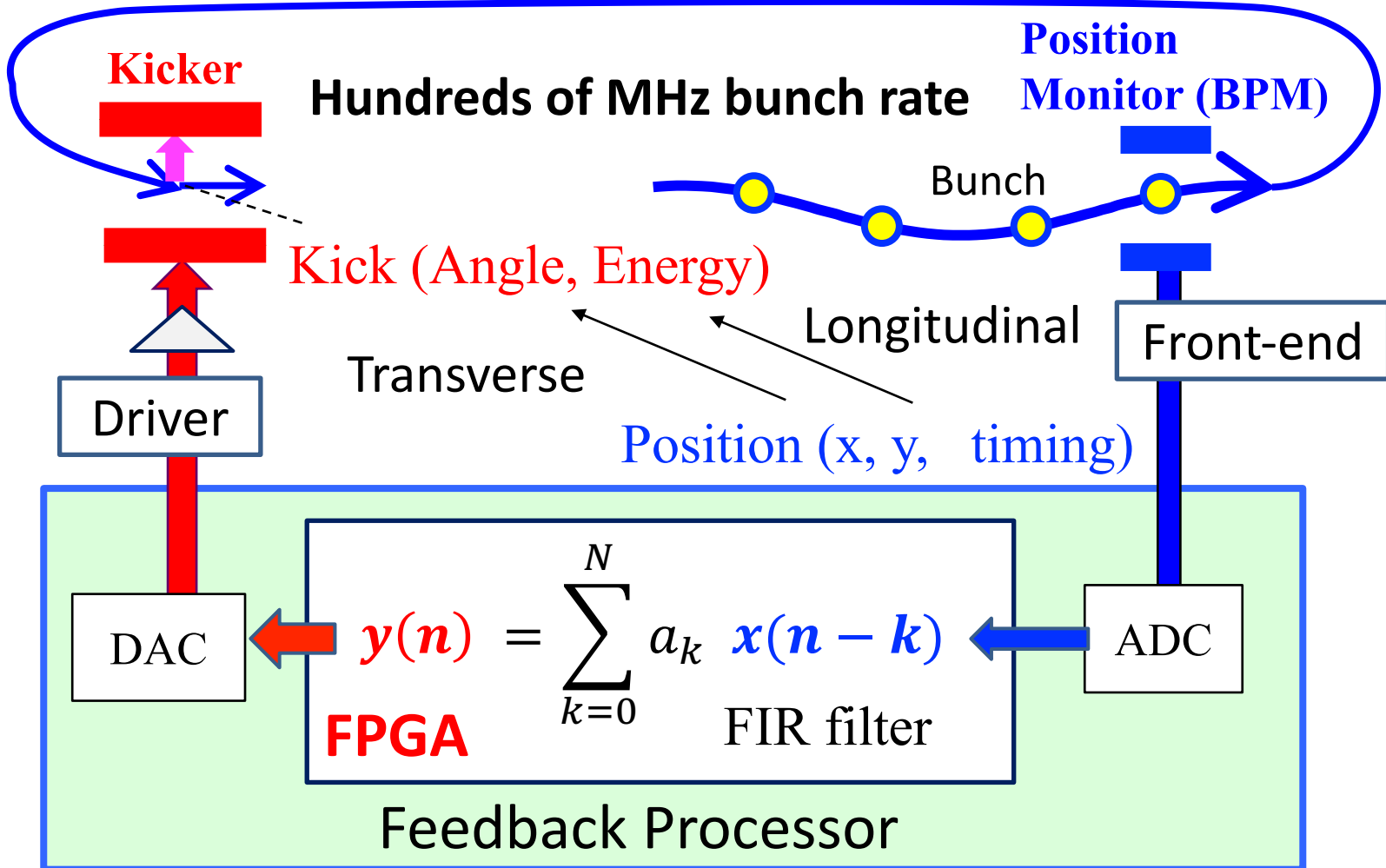
for Dipole and Quadrupole Oscillation ( $D\Phi FNE$ )

Space Saving High Efficiency **Longitudinal Kicker**

beam excitation by **BPM Noise** and **High Resolution BPM**

# Transverse and Longitudinal Digital Feedback

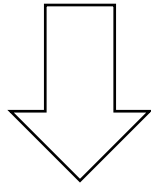
Devices for Damping of Betatron or Synchrotron Oscillations  
for Suppression of beam instabilities  
Fast damping of excited oscillation (mostly at injection)



# FPGA

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DSP (PEP-II, Elettra/SLS, .. )  
Custom LSI (KEK)



FPGA (Field Programmable Gate Array)

Hardware

Very Fast for simple processes

Field Programmable

we can easily change its logic

Reduction of Cost, Size

Simple architecture

# Examples of FPGA based Digital Feedback Processors

## Old SPring-8

### Feedback Processor\*

(First FPGA Based Processor  
~500MS/s ?)



Photon Factory, New SUBARU, Aichi-SR, TLS, HLS, SSRF, SOLEIL, PLS, PLS-II, KEK-PS (proton, intra-bunch), S-LSR(coasting ion), HIMAC(electron beam cooled ion)

## iGp12, Dimtel, Inc.



(based on SLAC / KEK / INFN-LNF design collaboration)

ALS, DAΦNE, Indus-2, SPEAR3, ANKA DELTA, LNLs, SuperKEKB, PEPC-II, Duke SR-FEL, MLS, TLS, BESSY II, ELSA, NSLS-II, TPS, CesrTA, HLS, Photon Factory, J-PARC, ..

## LIBERA Bunch-by-bunch,

i-tech

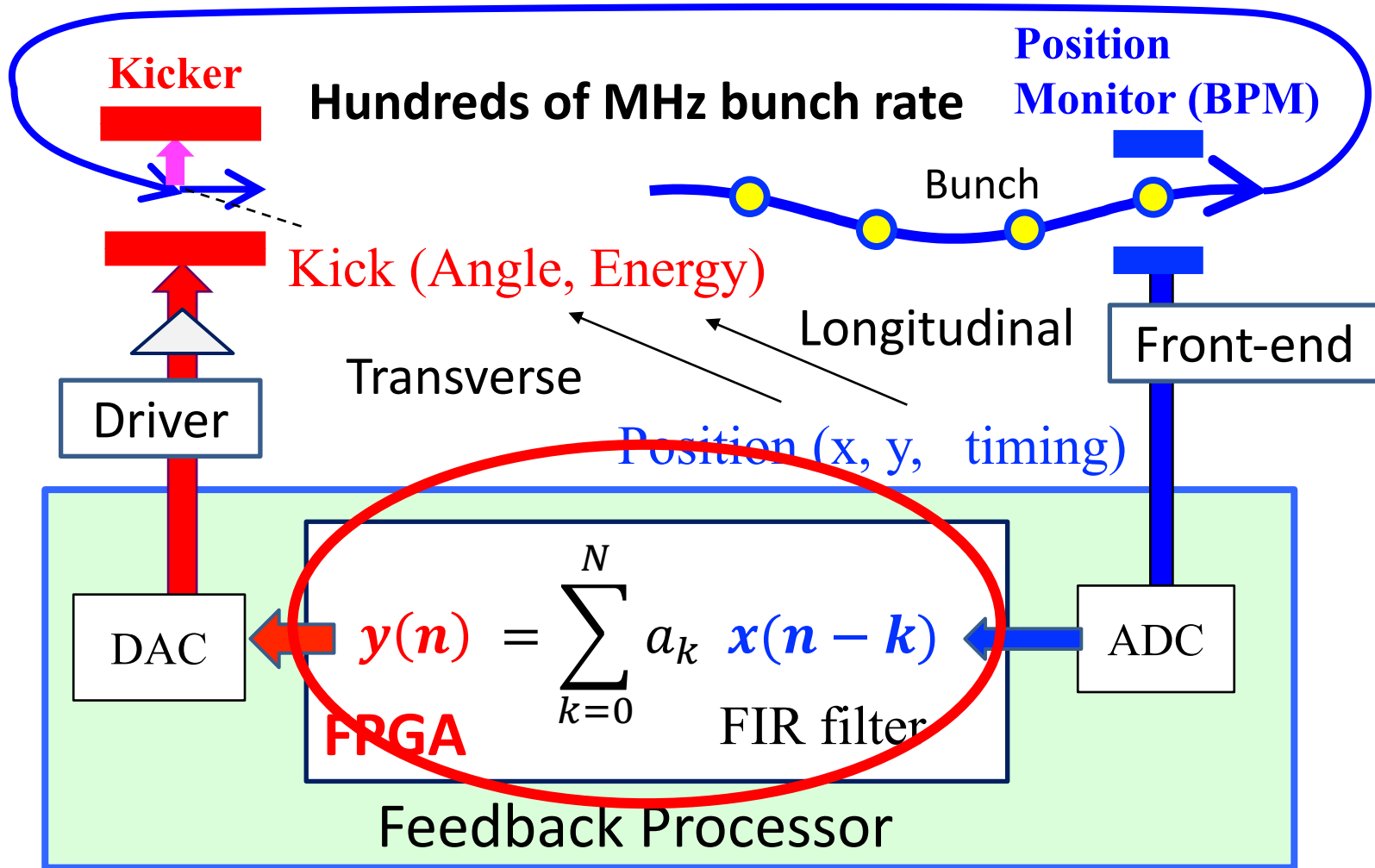


ESRF, ASP, ALBA, ANKA, CLS, Diamond, LNLs, NSRRC

\* T. Nakamura, K. Kobayashi, et al., EPAC'04, ICALEPSC'05 ( First FPGA based for hundreds MS/s)

# FIR Filter

Devices for Damping of Betatron or Synchrotron Oscillations  
for Suppression of beam instabilities  
Fast damping of excited oscillation (mostly at injection)



# Function of FIR filter

**Feedback Kick**

$$y(n) = \sum_{k=0}^N a_k x(n-k)$$

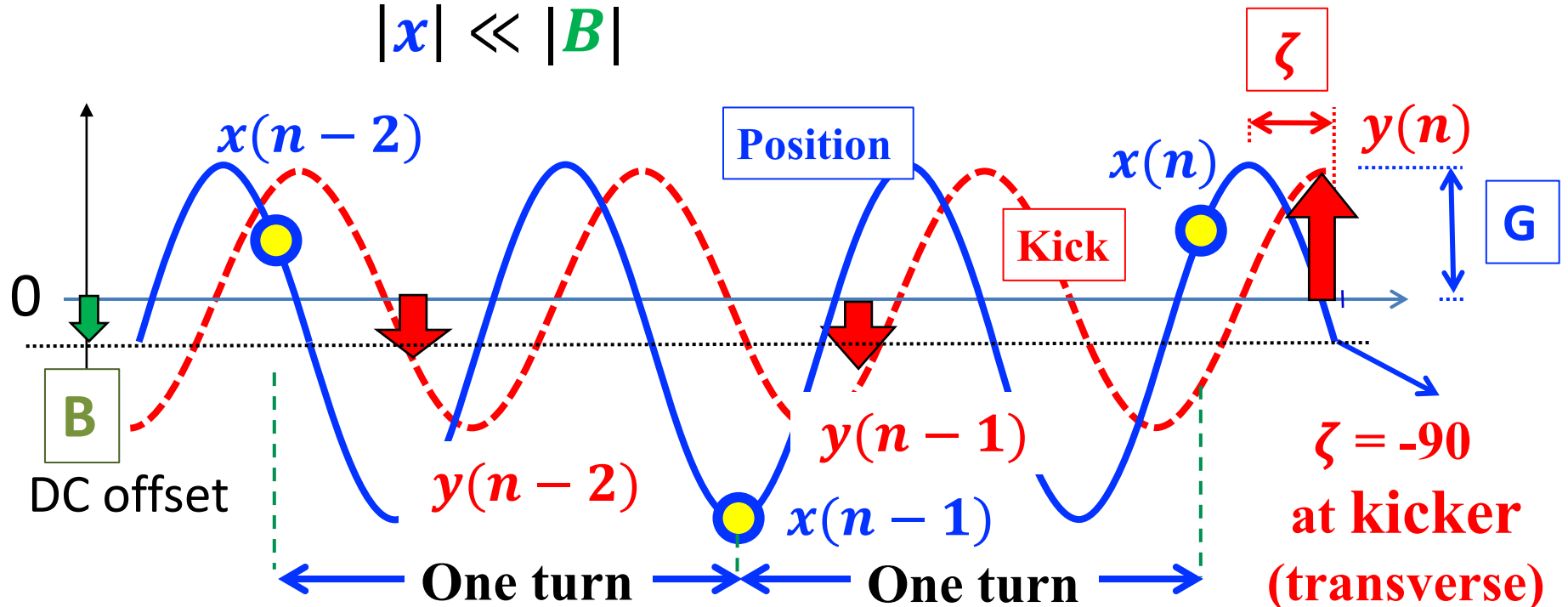
Coefficients

History of turn-by-turn  
**Position data**  
( (N+1) data )

## Function of FIR filter

- \* Beam position = Sinusoidal  $\Leftarrow$  Phase Shift  $\zeta$  and Gain  $G$
- \* Removal of DC offset  $B$  (closed orbit, BPM signal unbalance, )

$$|x| \ll |B|$$



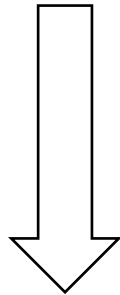
# Frequency (Tune) Response of FIR filter

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“Add Phase Shift  $\zeta$  and Gain  $\mathbf{G}$  , Remove DC offset  $\mathbf{B}$ ”

$$x(k) = \tilde{x} \exp(-ik(2\pi\nu_i)) + \mathbf{B}$$

$$y(k) = \mathbf{G}(\nu_i) e^{i\zeta(\nu)} \tilde{x} \exp(-ik(2\pi\nu_i))$$



$$y(n) = \sum_{p=0}^N a_k x(n-k)$$

2 constraints

$$\mathbf{G}(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i))$$

1 constraints

$$\mathbf{0} = \sum_{k=0}^N a_k$$

# Frequency Domain Condition for FIR filter

## Constraints on Coefficients of FIR filter

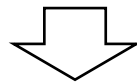
### Setting Phase and Gain

$$G(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i))$$

at Target tunes :  $\nu_i = 0, \nu_1, \nu_2, \dots, \nu_M$  (1+M tunes)

constraints on coefficients  $a_k$

2M (for  $\nu_i \neq 0$ ) + 1 (for  $\nu_i = 0$ )



We have 2M+1 coefficients (only)

⇔ We have more turn-by-turn data if  $2M+1 < N+1$

We need at least one oscillation data to get good response of FIR filter

# Frequency Domain Condition for FIR filter

## Constraints on Coefficients of FIR filter

### Setting Phase and Gain

$$G(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i))$$

### Minimization of

$$P = \int_0^1 |G(\nu)|^2 d\nu = 2\pi \sum_{k=0}^N |a_k|^2$$

- \* Minimization of Noise Power passing through FIR filter
- \* Reduction of gain not at  $\nu = \nu_i$

Minimization : No limit for the number of coefficients up to  $N+1$  (the number of position data)

# Example

**5 Constraints** : Target tune **0.15** with **flat response**

$$G(0) = 0$$

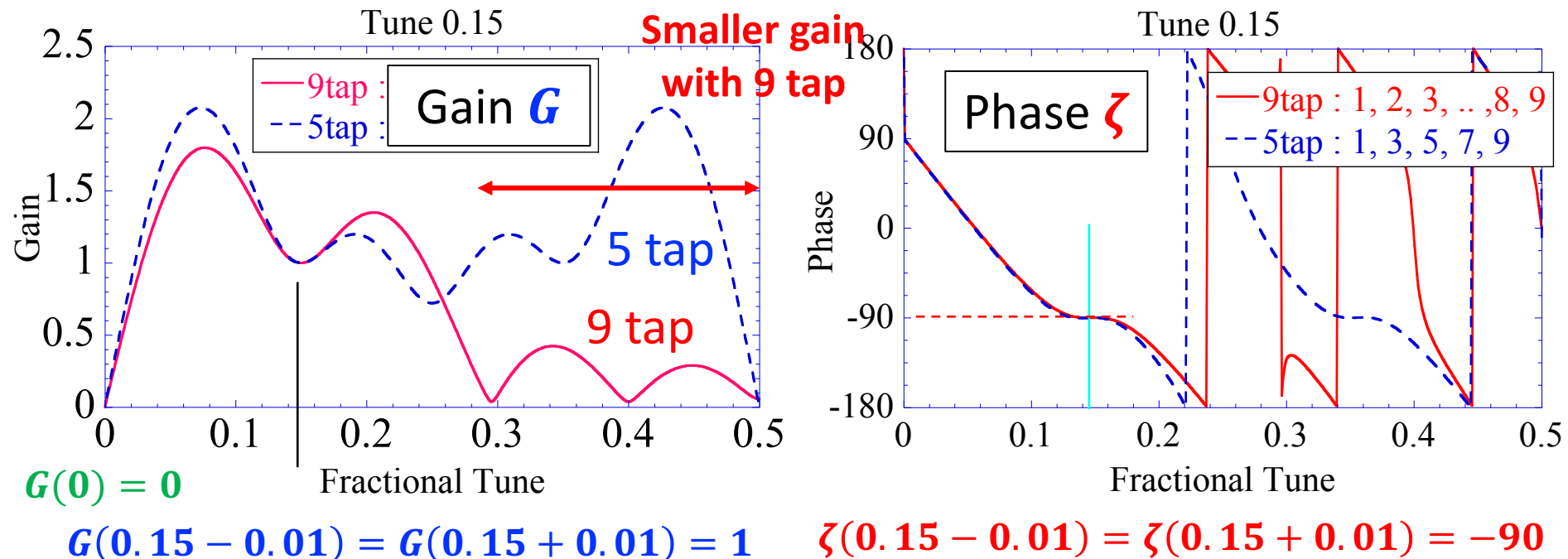
$$G(0.15 - 0.01) = G(0.15 + 0.01) = 1$$

$$\zeta(0.15 - 0.01) = \zeta(0.15 + 0.01) = -90 \text{ deg}$$

position data

5 tap : **-1, -3, -5, -7, -9** turns

9 tap : **-1, -2, -3, -4, -5, -6, -7, -8, -9** turns



# Least Square Fitting (TDLSF method) for Coefficients

$$x[n] = A \cos(2\pi\nu_0 n + \psi) + B$$

Least Square Fitting

$$= p_0 + p_1 \cos 2\pi\nu_0 n + p_2 \sin 2\pi\nu_0 n \quad \Rightarrow \quad p_m \text{ to } x_k$$

$$p_m = \sum_{k=0}^N C_{m,k} x_{-k}$$

Measured position

$$y[0] = GA \cos(\psi + \zeta)$$

$$\phi_0 = 0$$

$$y[0] = p_1 G \cos \zeta + p_2 G \sin \zeta = \sum_{k=0}^N (C_{1,k} G \cos \zeta + C_{2,k} G \sin \zeta) x_{-k}$$

$$a_k = C_{1,k} G \cos \zeta + C_{2,k} G \sin \zeta$$

We have  $a_k, k = 0, 1, 2, \dots, N$

$$y[0] = \sum_{k=0}^N a_k x_{-k}$$

Extension to multiple tunes is easy

TDLSF is equivalent to Frequency Domain with  
Constraints on Coefficients of FIR filter

**Setting Phase and Gain**

$$G(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i))$$

**Minimization of**

$$P = \int_0^1 |G(\nu)|^2 d\nu = 2\pi \sum_{k=0}^N |a_k|^2$$

- \* Minimization of Noise Power passing through FIR filter
- \* Reduction of gain not at  $\nu = \nu_i$

Minimization : No limit for the number of coefficients up to N+1 (the number of position data)

## Constraints on Coefficients of FIR filter

### Setting Phase and Gain

$$G(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i))$$

$$\left. \frac{\partial}{\partial \nu} (G(\nu) e^{i\zeta(\nu)}) \right|_{\nu=\nu_i} = -2\pi i \sum_{k=0}^N a_k k \exp(-ik(2\pi\nu_i)) = 0$$

Flat response at  $\nu \sim \nu_i$

Minimization of 
$$P = \int_0^1 |G(\nu)|^2 d\nu = 2\pi \sum_{k=0}^N |a_k|^2$$

# Frequency Domain Condition for FIR filter

TDLSF is Equivalent to Following Frequency Domain condition

**Gain, Phase and "Flat response" : Equivalent to**

$$\begin{aligned} G(\nu_i) e^{i\zeta(\nu_i)} &= G(\nu_i \pm \Delta) e^{i\zeta(\nu_i \pm \Delta)} \\ &= \sum_{k=0}^N a_k \exp(-ik(2\pi(\nu_i \pm \Delta))) \\ G(\Delta) e^{i\zeta(\Delta)} &= \mathbf{0} \quad \text{with setting } \Delta \ll 1 \end{aligned}$$

Minimization of

$$P = \int_0^1 |G(\nu)|^2 d\nu = 2\pi \sum_{k=0}^N |a_k|^2$$

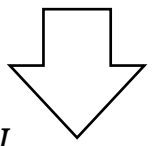
# Least Square Fitting (TDLSF method) for Coefficients : 1<sup>st</sup> order

$$x[n] = A \cos((1 + \Delta)\phi_n + \psi) + B \quad \phi_n = 2\pi\nu_0 n$$

$$\rightarrow p_0 + p_1 \cos \phi_n + p_2 \sin \phi_n + \underbrace{(p_3 \phi_n \cos \phi_n + p_4 \phi_n \sin \phi_n)}_{\sim O(\Delta)}$$

for  $|\Delta| \ll 1$

Linear for  $p_m$



Least Square Fitting

$\sim O(\Delta)$

$$p_m = \sum_{k=0}^N C_{m,k} x_{-k}$$

$p_m$  to  $x_k$

turn-by-turn  
Positions

$$y[0] = GA \cos((1 + \Delta)\phi_0 + \psi + \zeta) = GA \cos(\psi + \zeta) \quad \phi_0 = 0$$

$$y[0] = p_1 G \cos \zeta + p_2 G \sin \zeta = \sum_{k=0}^N (C_{1,k} G \cos \zeta + C_{2,k} G \sin \zeta) x_{-k}$$

$$a_k = C_{1,k} G \cos \zeta + C_{2,k} G \sin \zeta$$

We have  $a_k, k = 0, 1, 2, \dots, N$

$$y[0] = \sum_{k=0}^N a_k x_{-k}$$

**Extension to multiple tunes is easy**

# TDLSF and Frequency Domain : 1<sup>st</sup> order

TDLSF (1<sup>st</sup> order) : Equivalent to

**Setting Phase and Gain**

$$G(\nu_i) e^{i\zeta(\nu_i)} = \sum_{k=0}^N a_k \exp(-ik(2\pi\nu_i)) \quad p_1 \cos \phi_n + p_2 \sin \phi_n$$

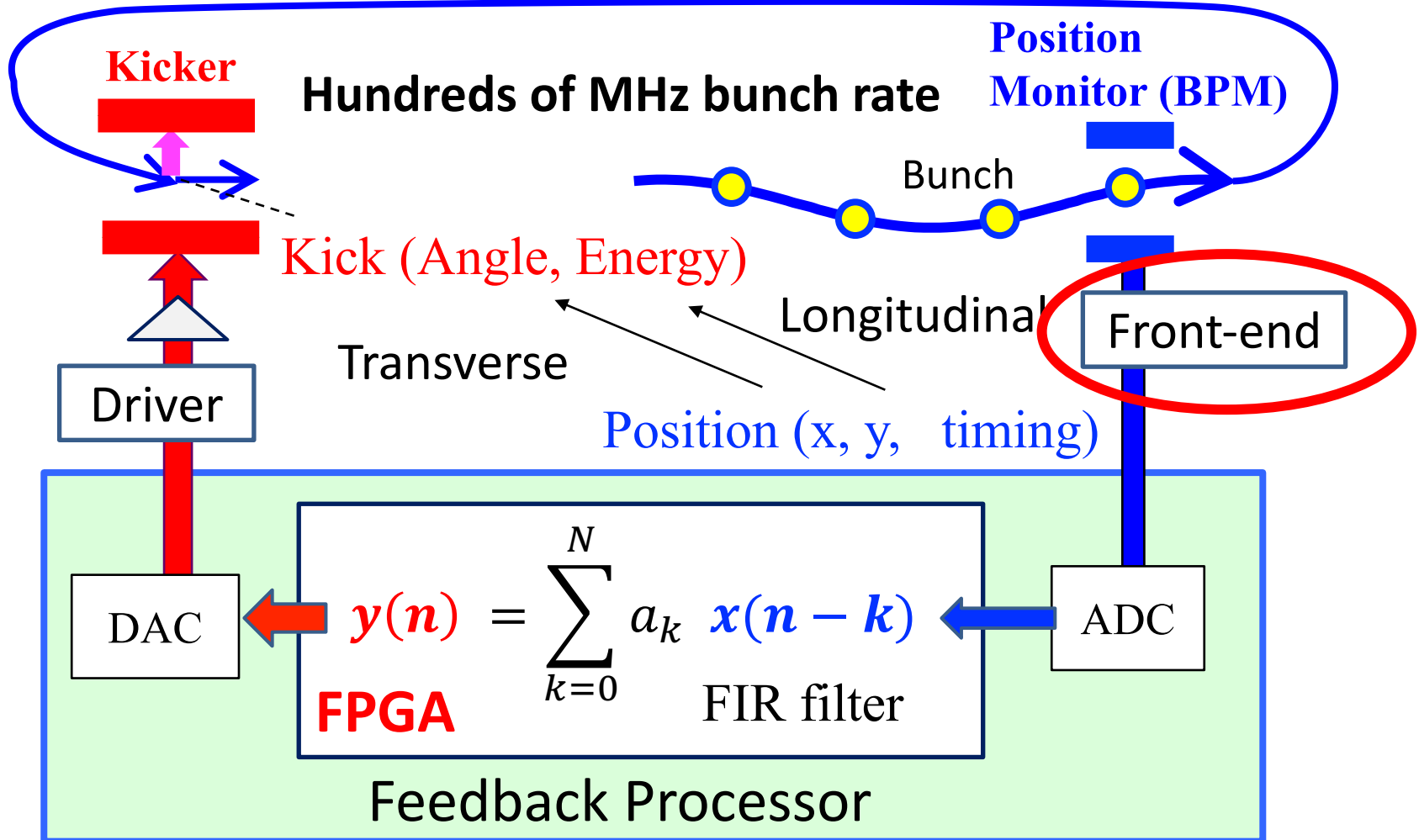
$$\left. \frac{\partial}{\partial \nu} (G(\nu) e^{i\zeta(\nu)}) \right|_{\nu=\nu_i} = -2\pi i \sum_{k=0}^N a_k k \exp(-ik(2\pi\nu_i)) = 0 \quad (p_3 \phi_n \cos \phi_n + p_4 \phi_n \sin \phi_n)$$

**Flat response at  $\nu \sim \nu_i$**

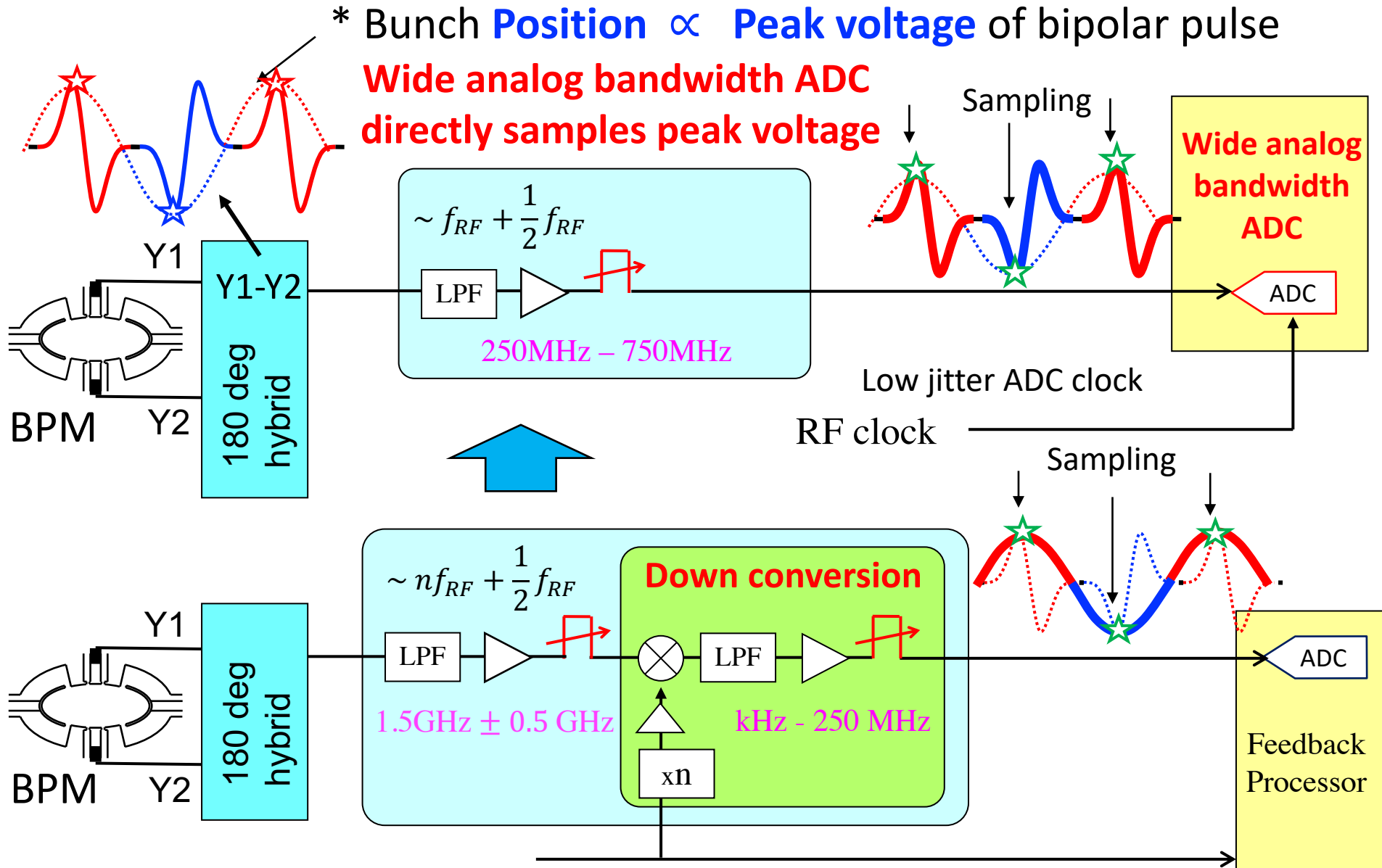
Minimization of 
$$P = \int_0^1 |G(\nu)|^2 d\nu = 2\pi \sum_{k=0}^N |a_k|^2$$

# Font-End

Devices for Damping of Betatron or Synchrotron Oscillations  
for Suppression of beam instabilities  
Fast damping of excited oscillation (mostly at injection)



# Front-End with Direct Sampling for Transverse Feedback



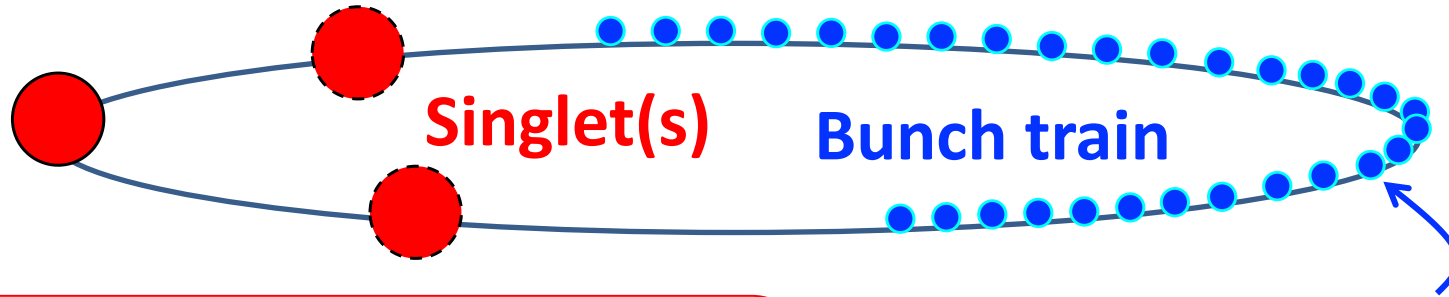
# Transverse Feedback for Hybrid Filling

**High** Bunch Current Singlet Bunch(es) + **Low** Bunch Current Trains  
Requested by Synchrotron Radiation Users

~ 5mA/bunch

← x 50 →

0.1 mA/bunch ~



## Single-bunch Instability

Mode-coupling

Beam pipe broad band impedance,  
Resistive-wall, tapers of In-Vacuum IDs

## Multi-bunch Instabilities

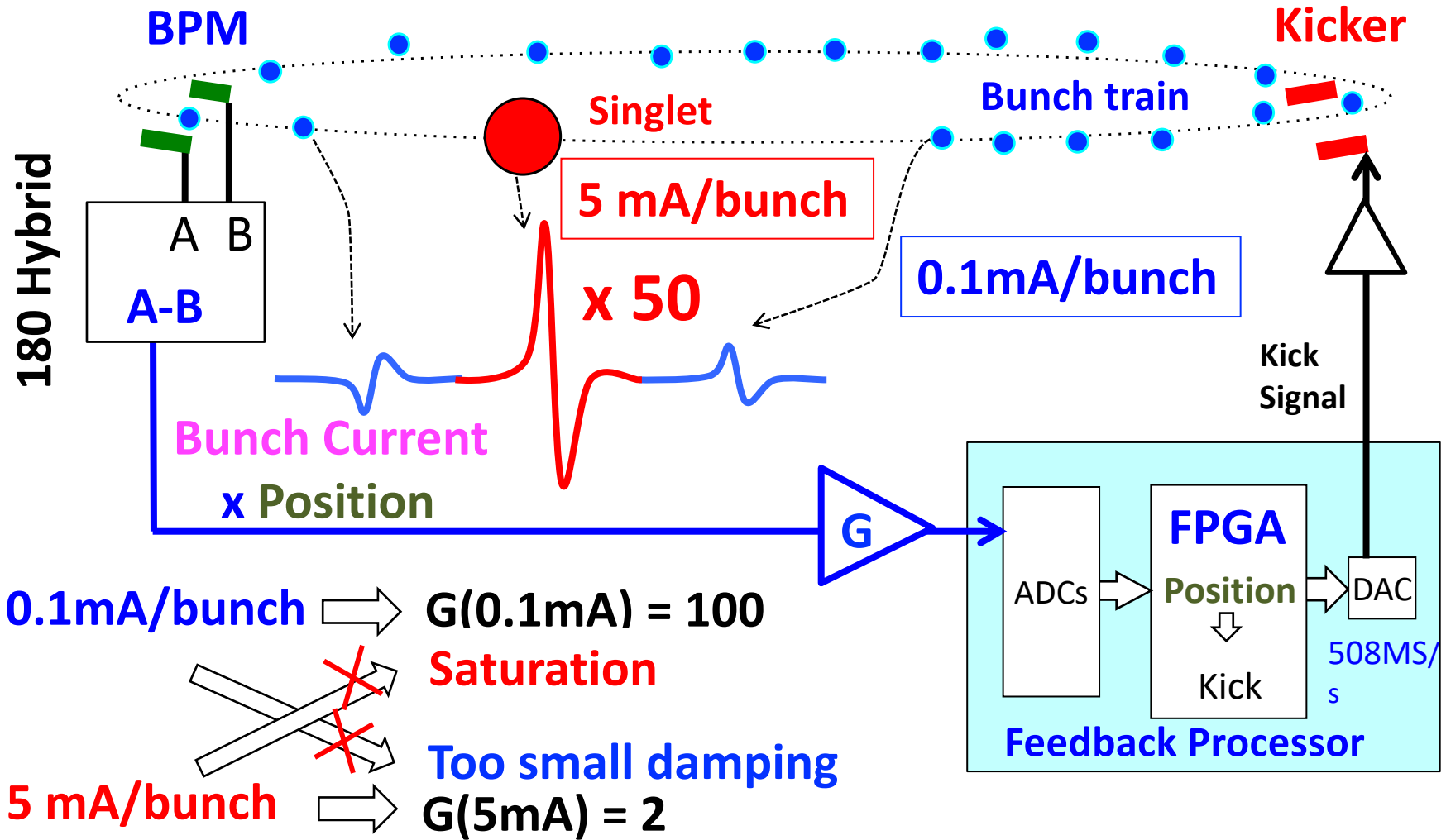
Resistive-wall of in-vacuum IDs  
Cavity HOM

Simultaneous Suppression

**Transverse Bunch-by-bunch Feedback System**

1 x 5mA/bunch + 1/3 fill, 5 x 3mA/bunch + 1/7 fill, ... for SPring-8

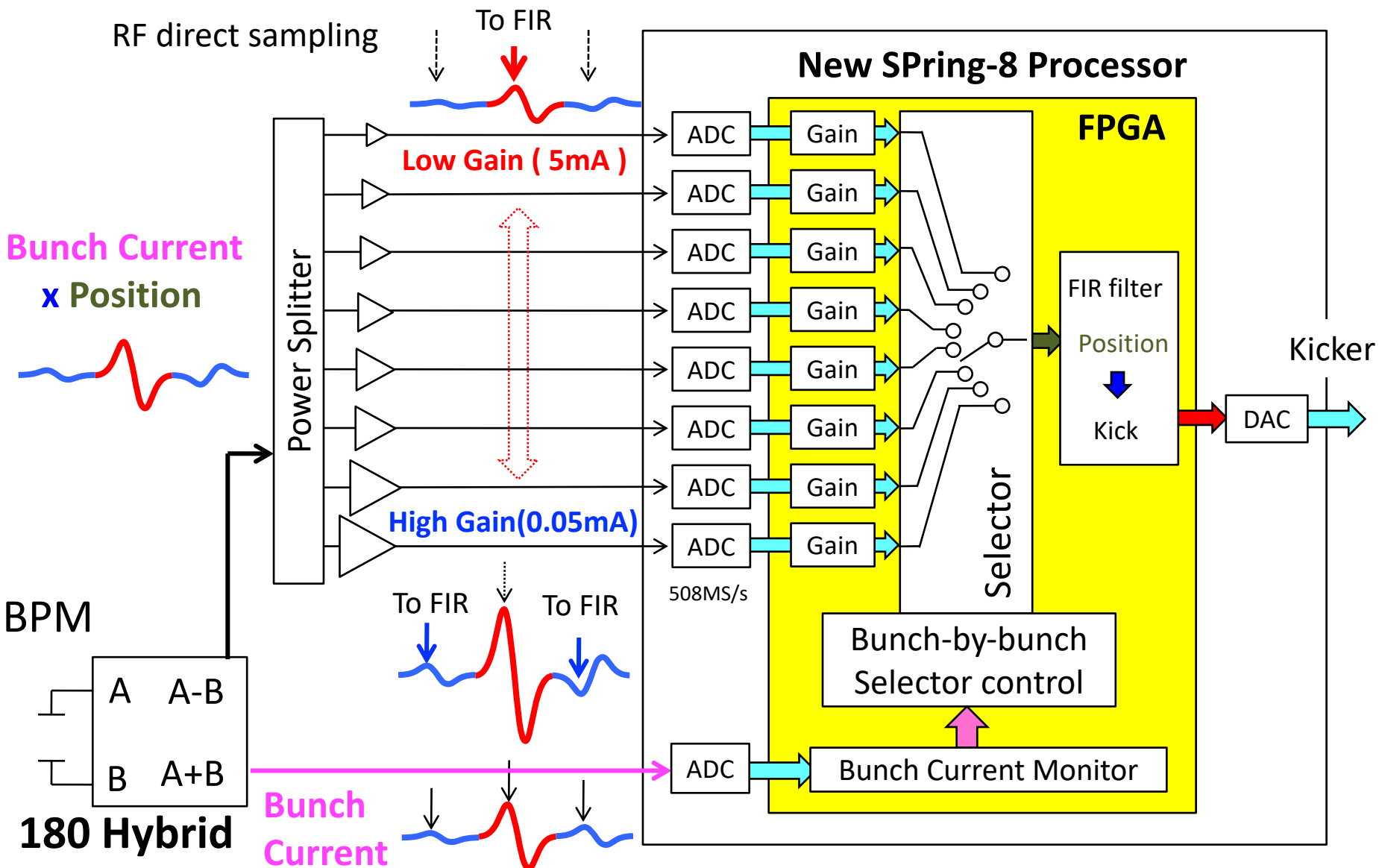
Simple Front-end cannot Handle Both bunch current



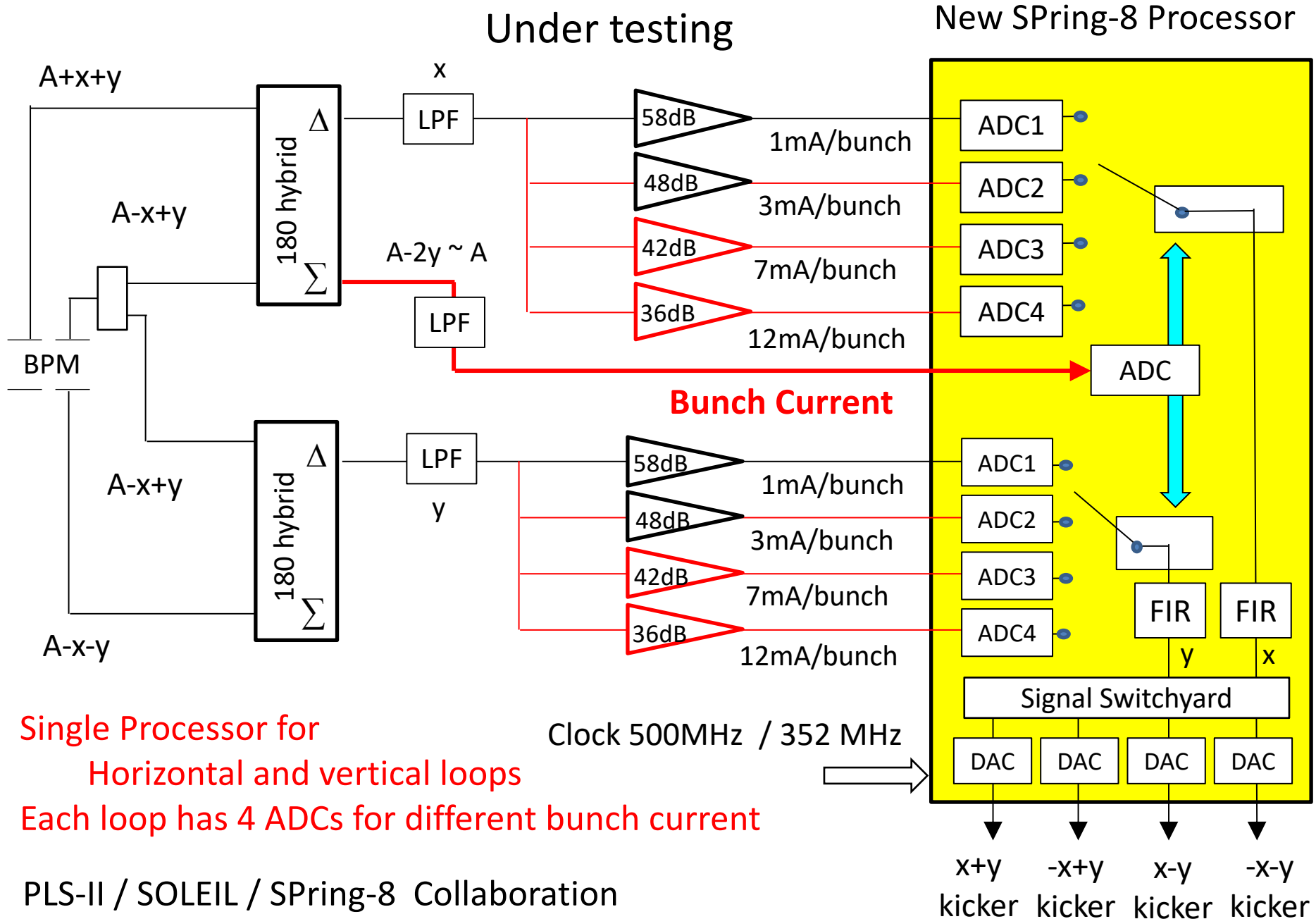
“Fast automatic bunch-by-bunch Attenuator” is one solution

# New SPring-8 Feedback Processor for Hybrid Filling

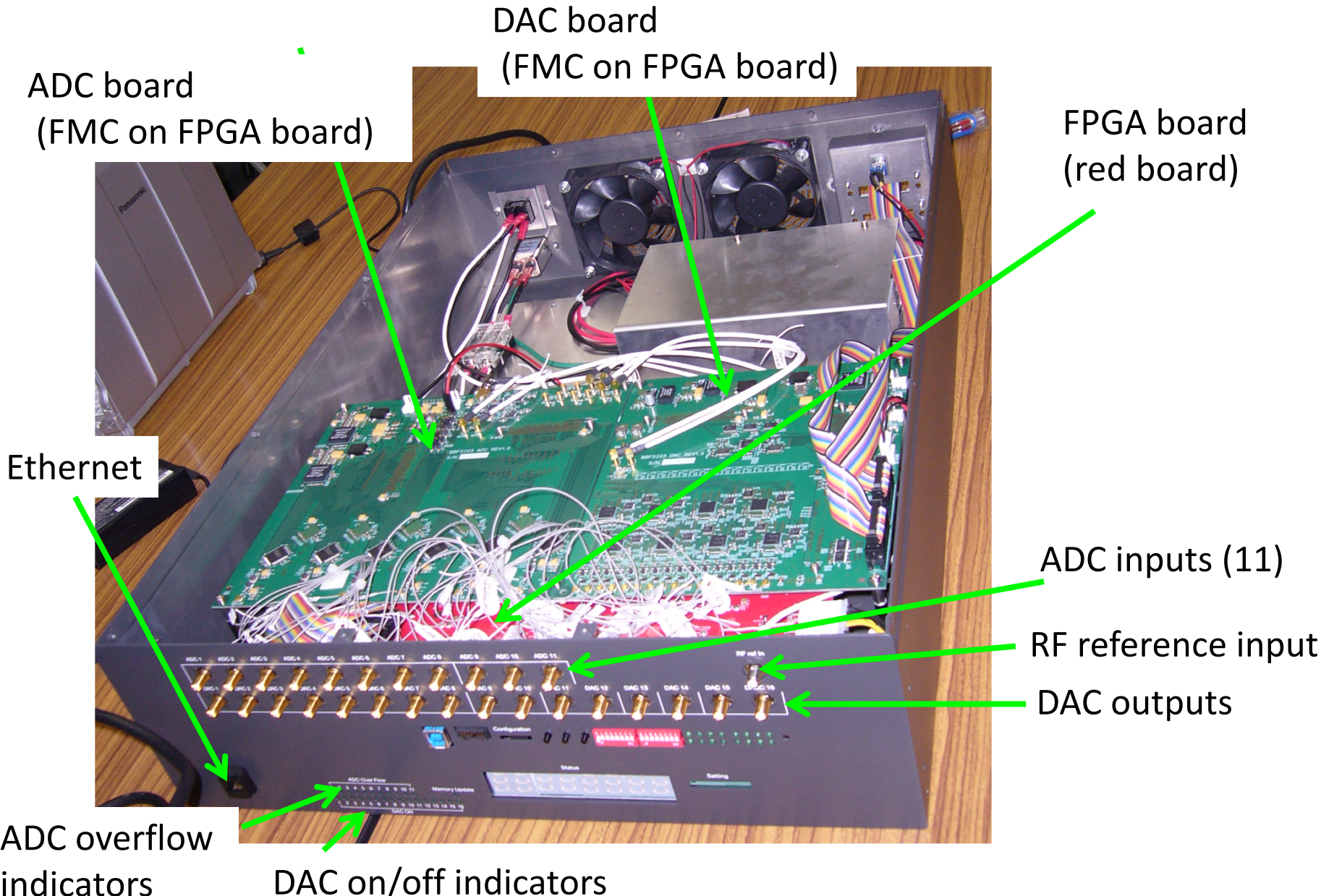
Select ADC with "good" signal level Front-end based on measured bunch current



# For Hybrid Filling for PLS-II and SOLEIL : H and V in one processor

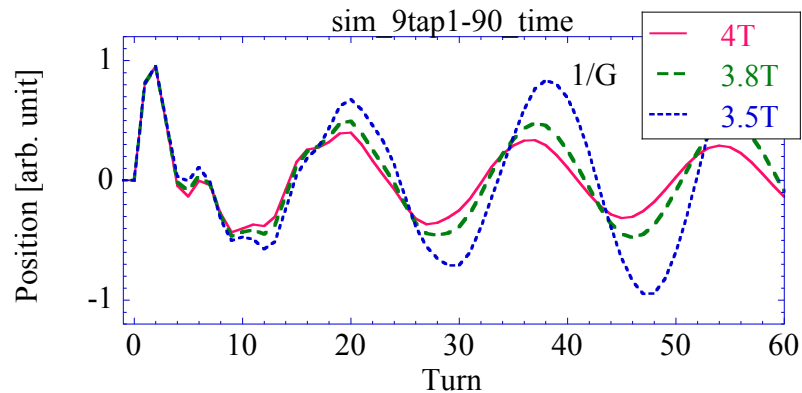
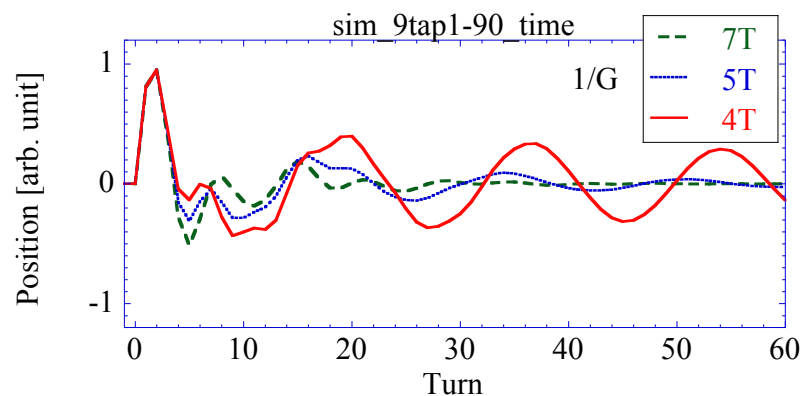
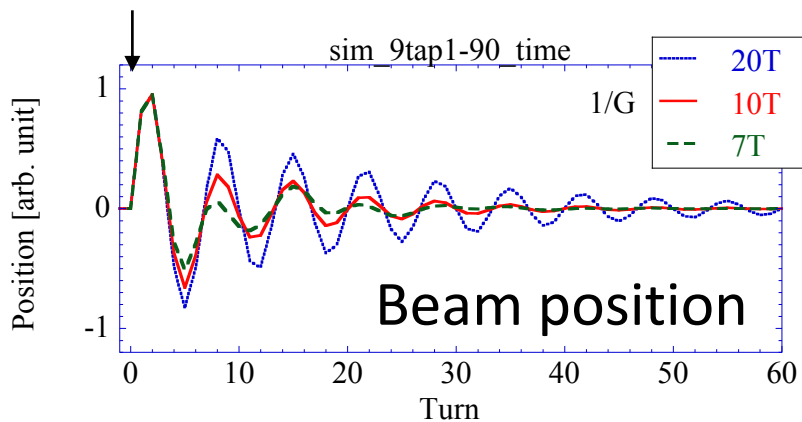


# New SPring-8 Signal Processor (upside down)



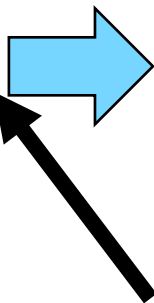
# Instability of Feedback at High Gain

Kick At High Gain, feedback system drives beam oscillation



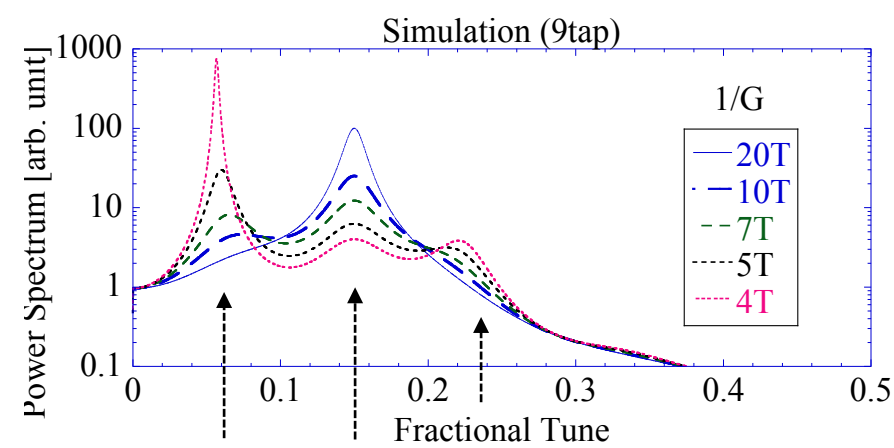
Higher Gain

Fourier Trans.



$nT \leq$  Gain corresponding to Damping time  $n$  turns

Beam is unstable at High gain with Different tune from original



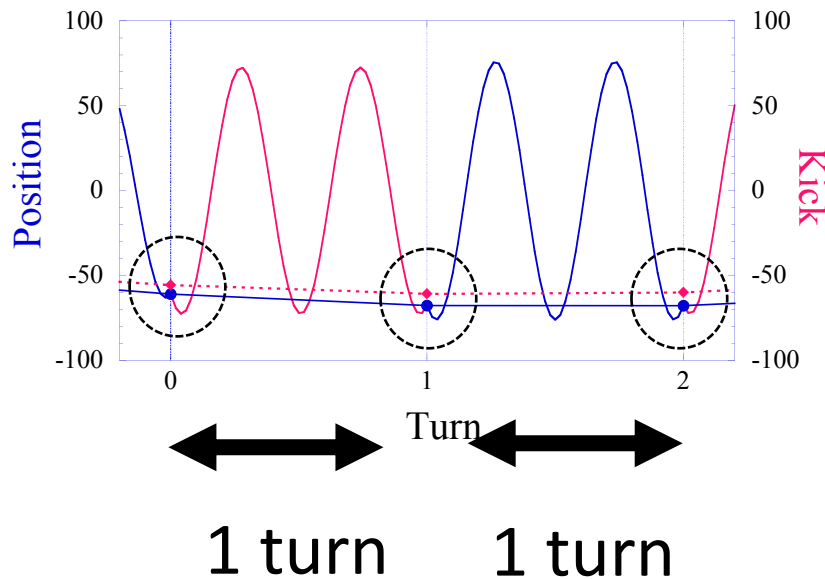
Excited Original Excited  
0.05 0.15 0.23

1/Threshold Gain = 3.8 turns

# Tune Shift by Feedback at High Gain

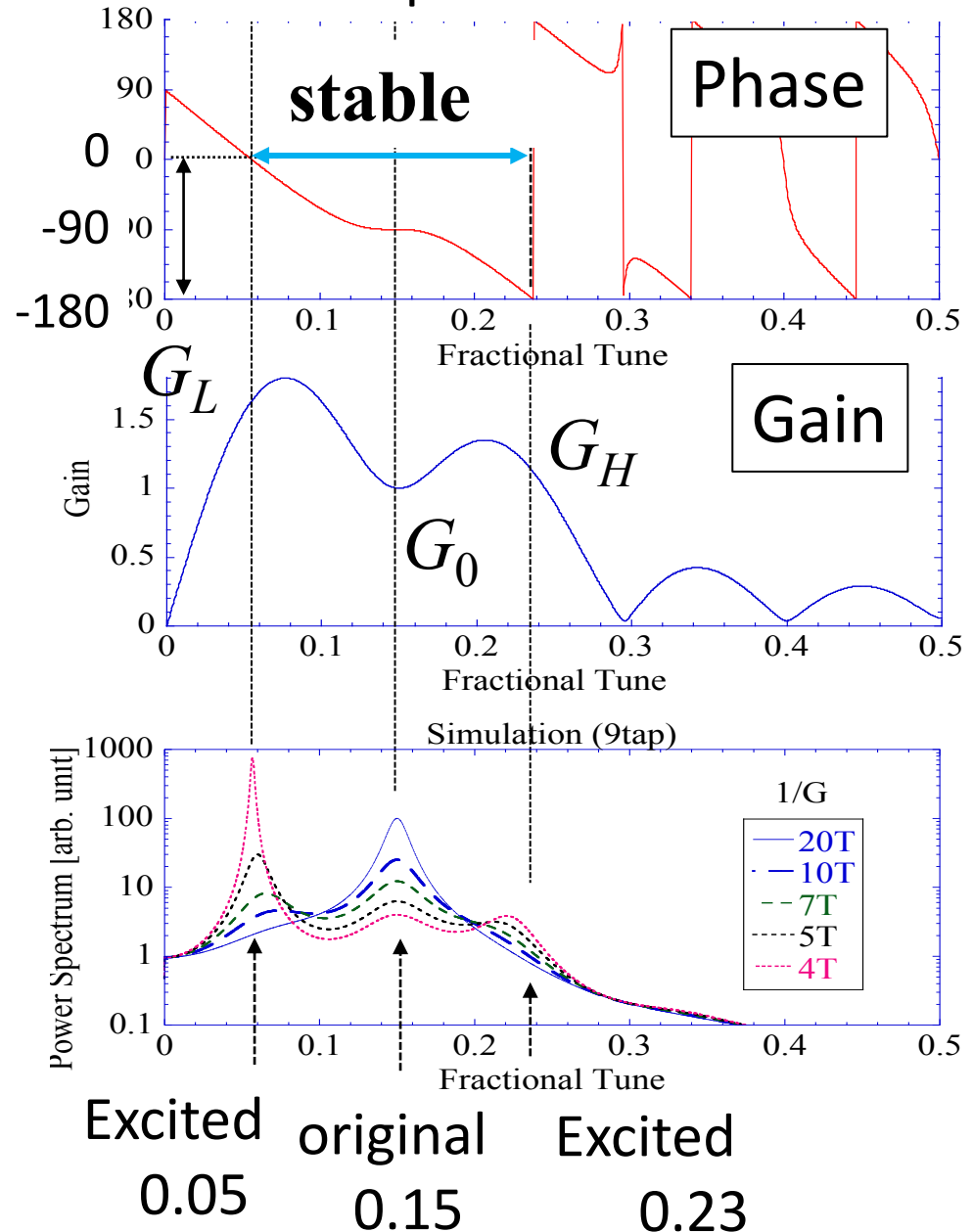
High Gain Feedback Drives Tune to Unstable Region

$1/G = 2.8 T < 3.8 T$  (threshold)

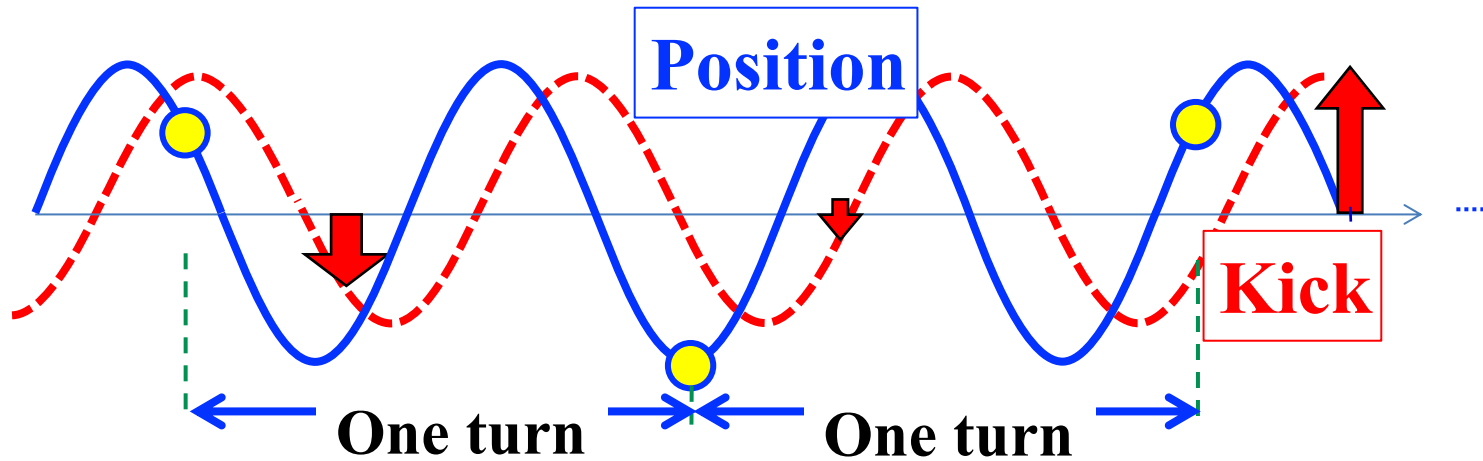


Feedback is Defocusing kick  
gain  $G_L$  is strong enough  
to shift tune from  
 $0.15 \rightarrow 0.05$

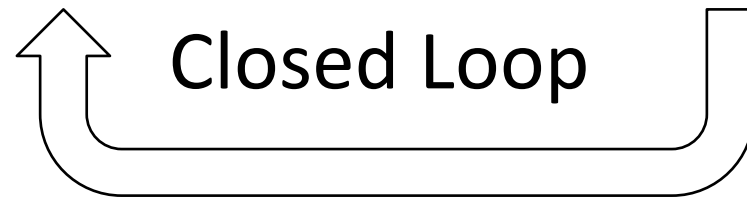
Tune response of FIR filter



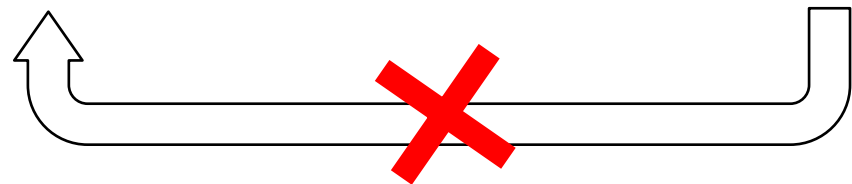
# Instability of Feedback Driven by Closed Loop : Position - Kick



**Turn-by-turn position data**  $\Rightarrow$  **Kick**



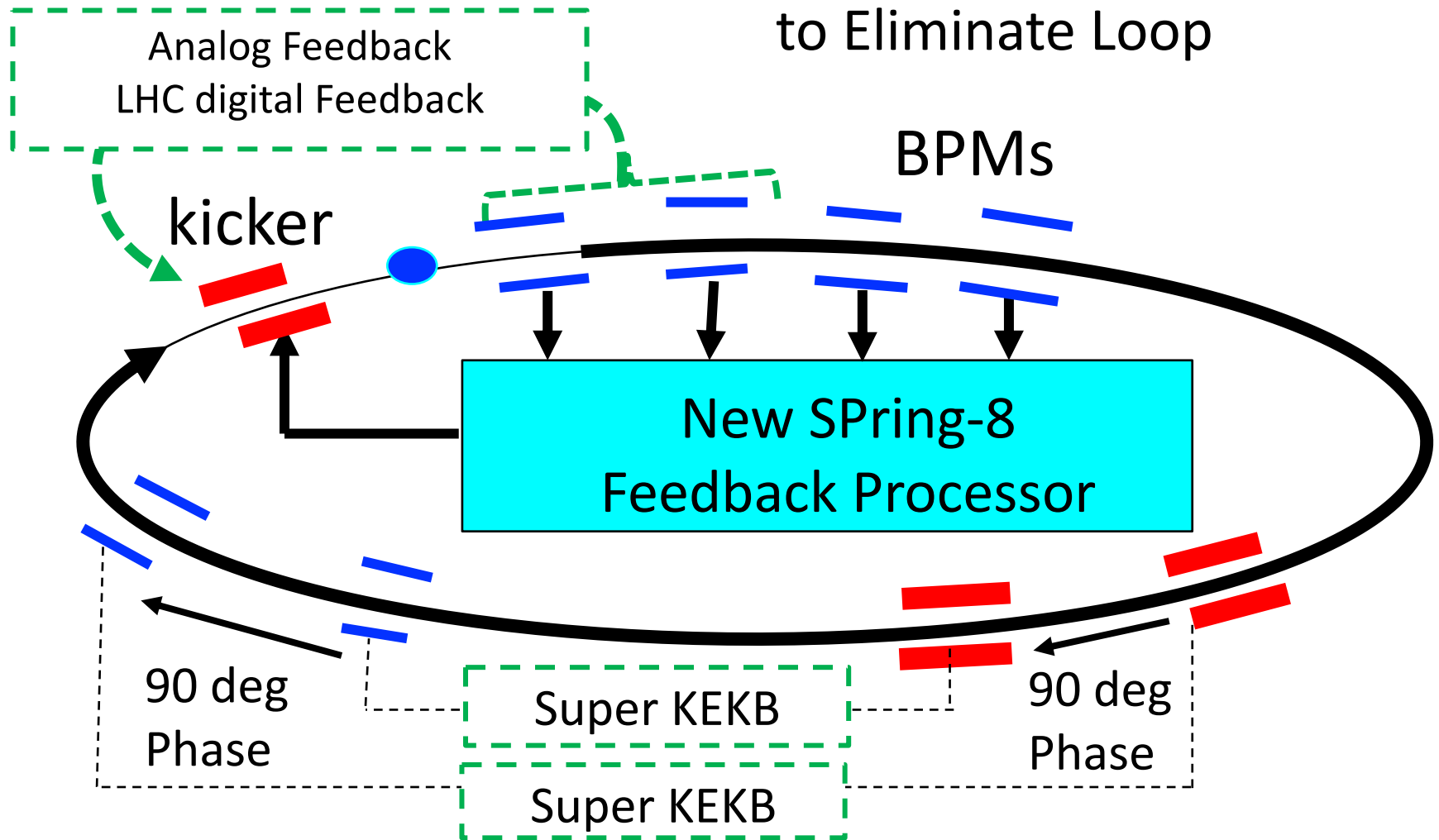
**Position data at multiple Locations  
at one previous turn**  $\Rightarrow$  **Kick**



# Digital Feedback with Position Data at Multiple Locations (BPMs)

kick is calculated with beam **Positions at Multiple Locations**

to Eliminate Loop



For LHC with Two BPM : P. Baudrenghien, et al. EPAC'08

T. Nakamura, TWIICE 2014 (SOLEIL), Phys. Soc. of Japan(2016), Part. Acc. Soc. of Japan(2017)

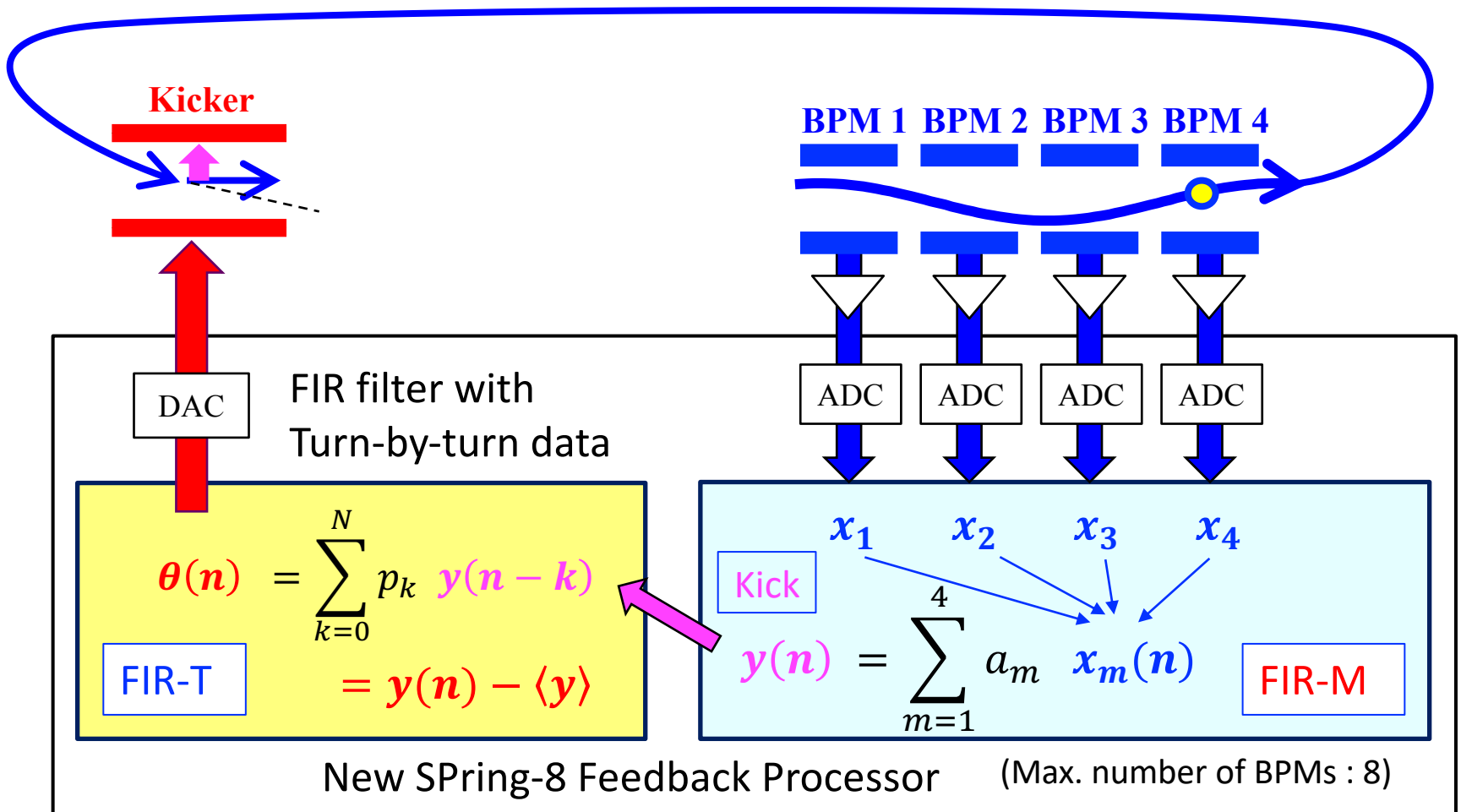
# Digital Feedback with Position Data at Multiple Locations (BPMs)

**FIR-M** for Kick from beam positions at multiple locations

4 BPM -> DC offset subtraction is possible for **Ideal case (static)**

**FIR-T** for Subtraction of DC offset

Produced by drift of **Closed orbit, Amplifier gain, ADC gain and timing**



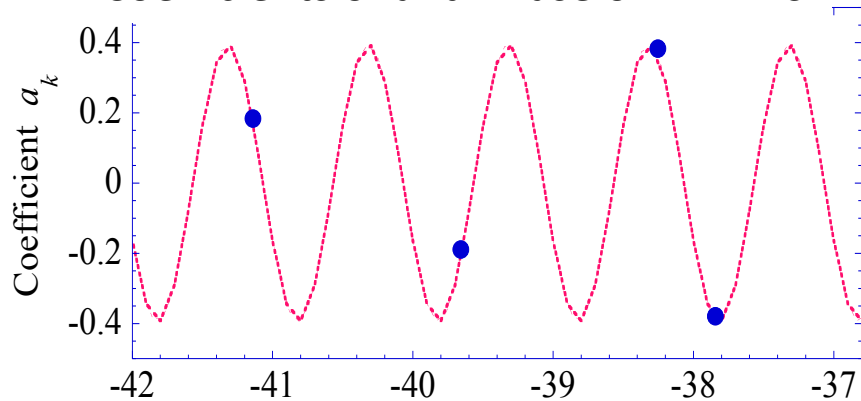
# Digital Feedback with Position Data at Multiple Locations (BPMs)

**FIR-M**

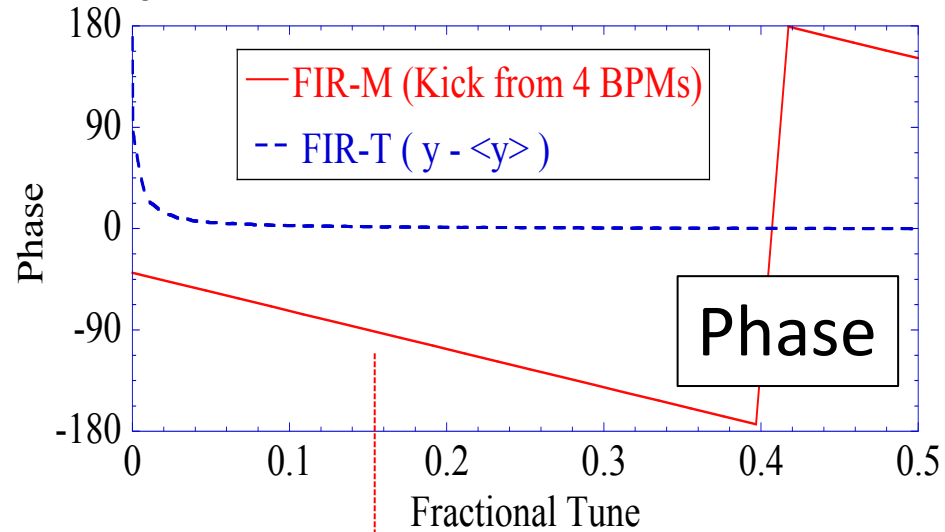
$$y(n) = \sum_{m=1}^4 a_m x_m(n)$$

**FIR filter response**

Coefficients of and Phase of 4 BPMs



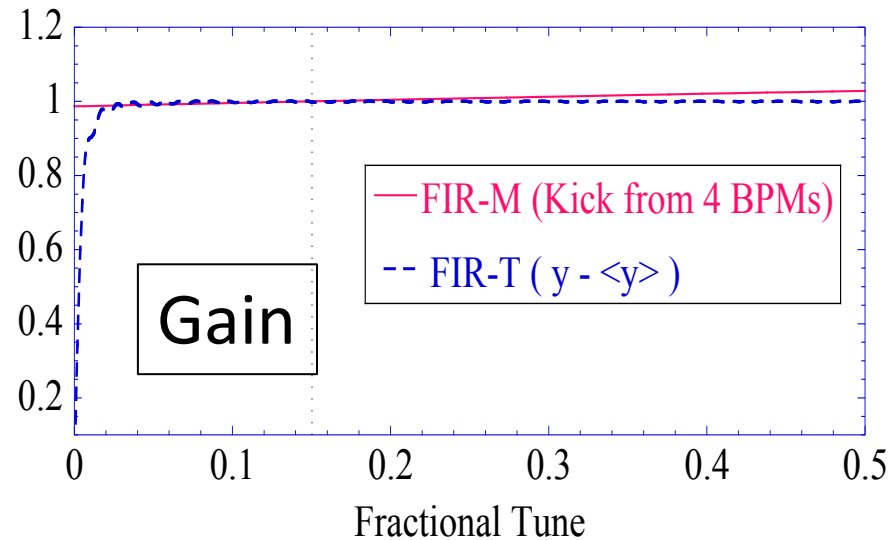
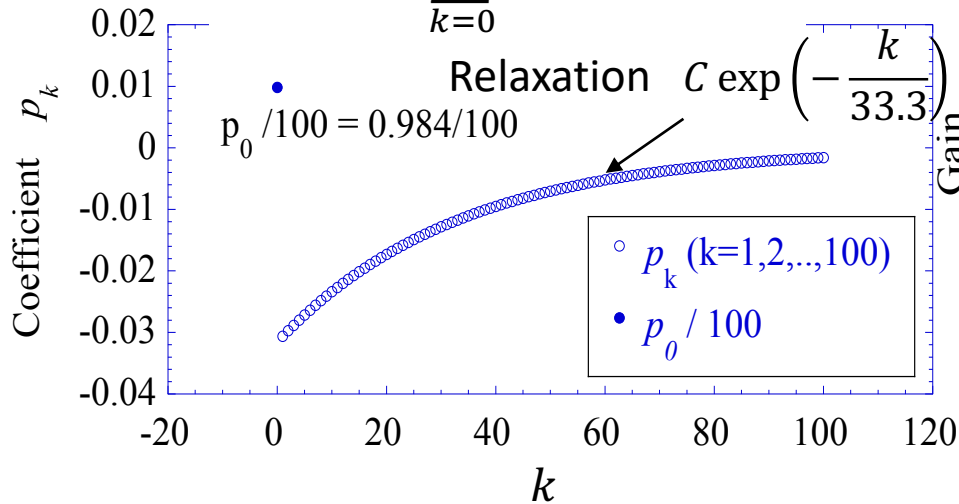
Phase Shift / (2π) at BPM from Kicker



Tune should be **FIXED** even at High Gain

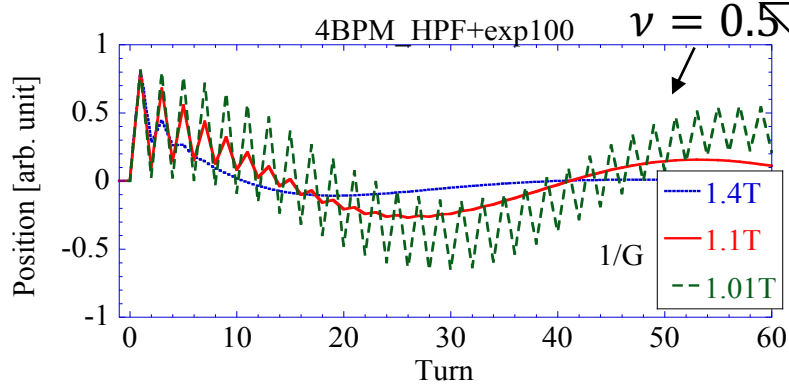
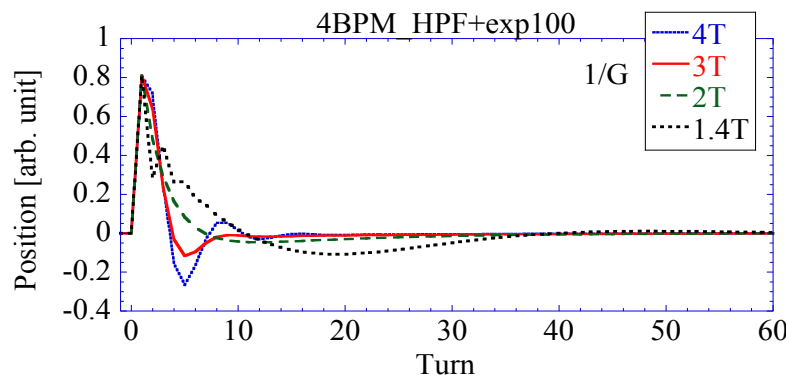
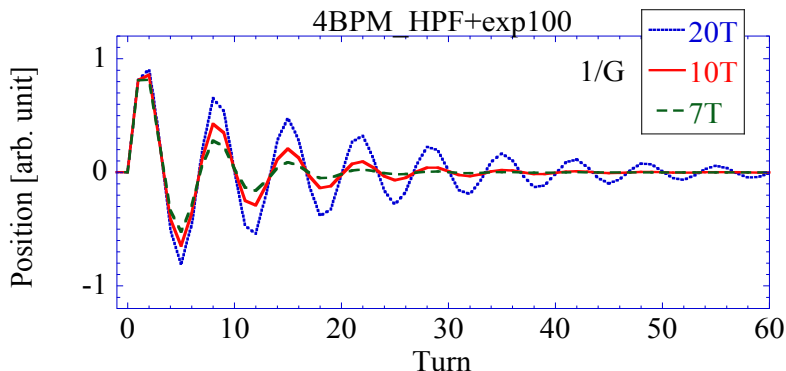
**FIR-T**

$$\theta(n) = \sum_{k=0}^{100} p_k y(n-k)$$

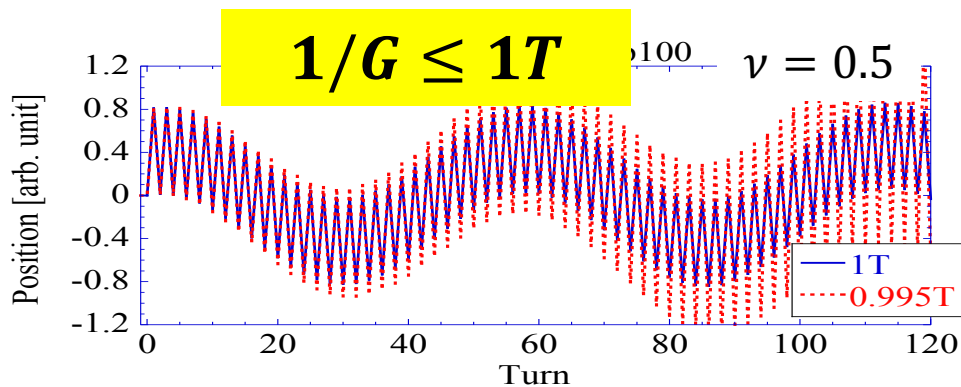


# Simulation Results : Feedback with Position Data at Multiple Locations

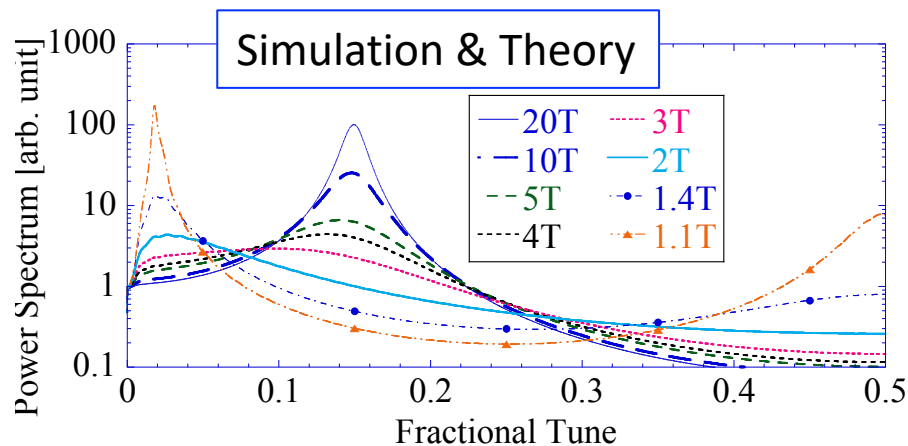
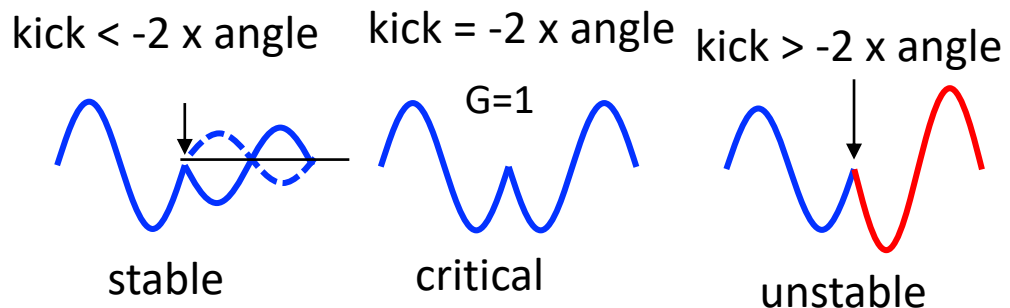
Damping time up to  $\sim 1.1$  turns  
No growth



Increase of Gain

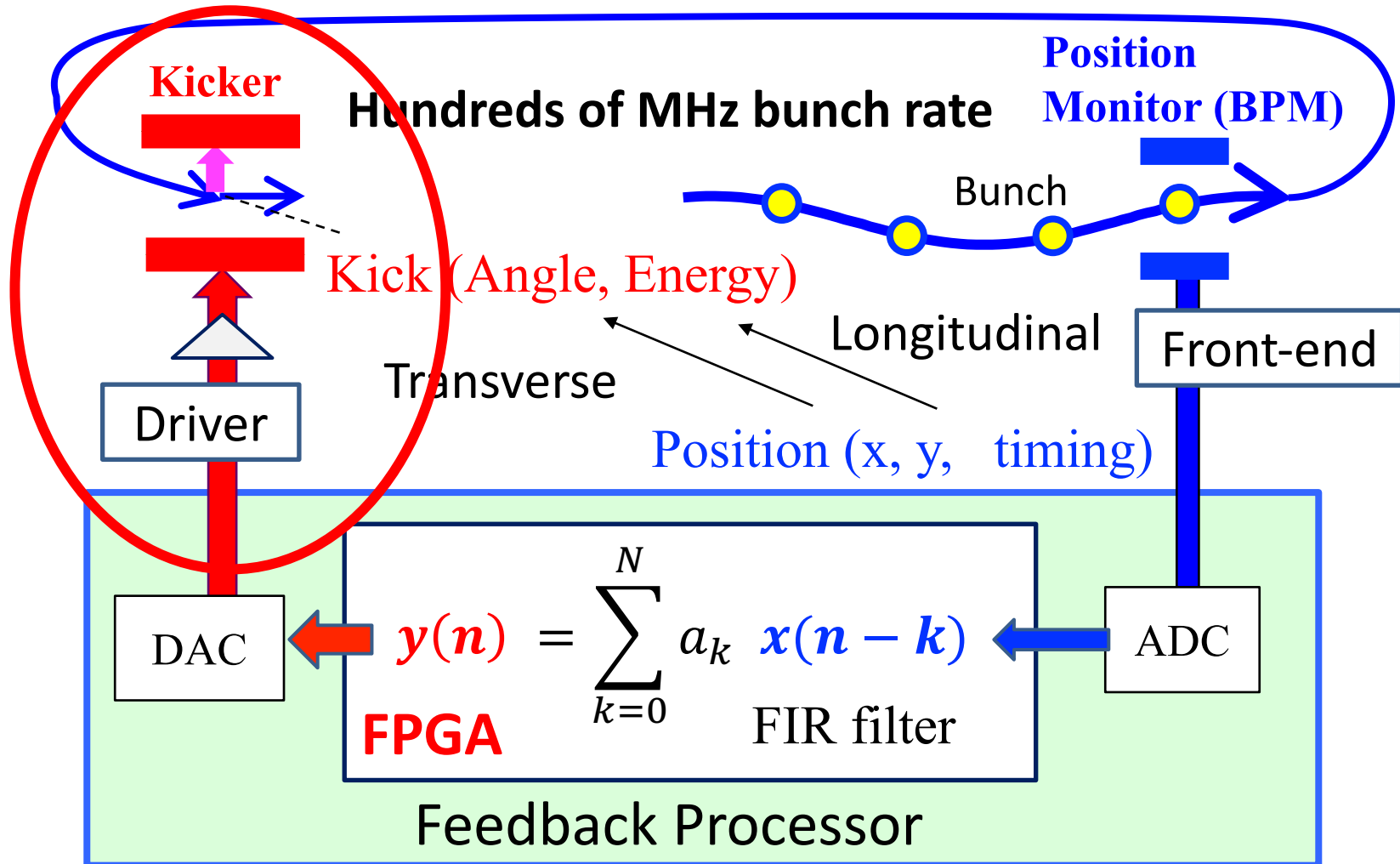


Beam is unstable for  $> G=1T$   
even with ideal feedback : **kick = - 2 G x angle**



# Kicker

Devices for Damping of Betatron or Synchrotron Oscillations  
for Suppression of beam instabilities  
Fast damping of excited oscillation (mostly at injection)



# SPring-8 Longitudinal Kicker

SPring-8 Storage ring ( at 6 GeV operation )

\* Large Revolution Period (5 $\mu$ s) and High Energy (6GeV)

=> **Large** kick

\* Limited space for kickers

=> **Short** kicker

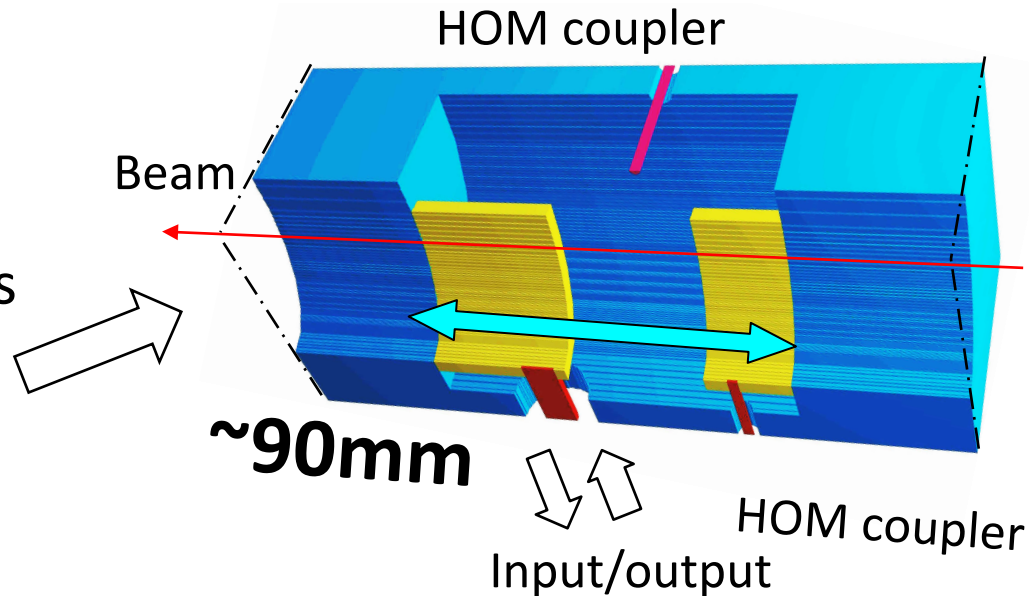
\* Higher frequency

**3 + 1/4** period / bunch spacing @500MHz is preferable

=> **Simple drive circuit without QPSK modulator**

**High Shunt Impedance**  
**Short Kicker**

1/4 part  
Beam pipe shape is  
Preserved  
no taper transition  
is necessary

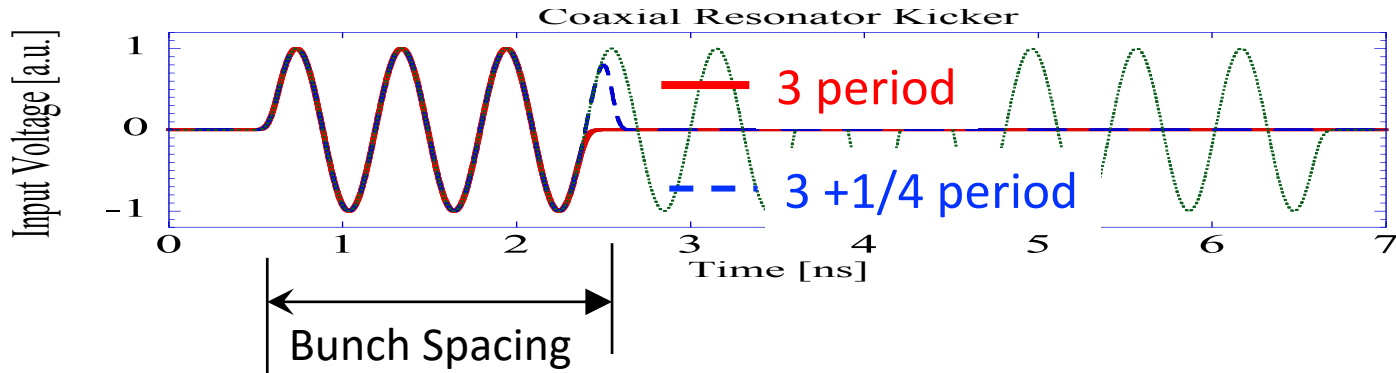


# SPring-8 Longitudinal Kicker

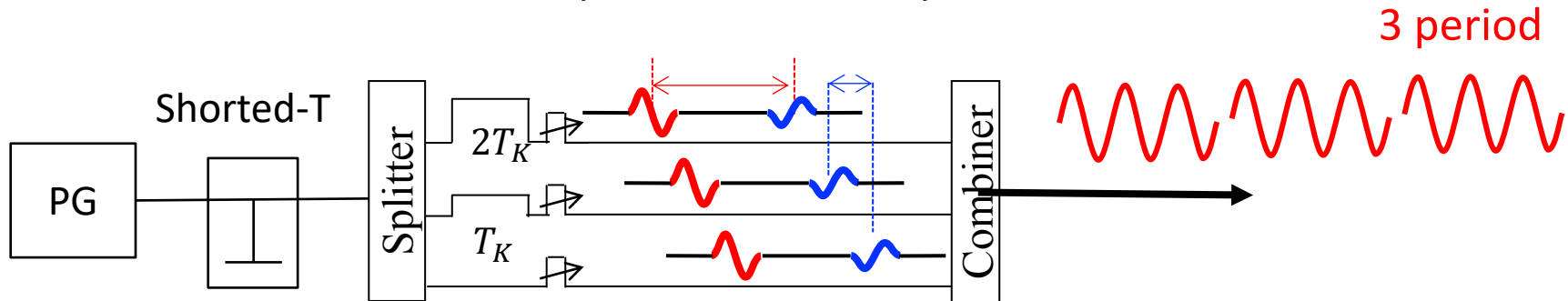
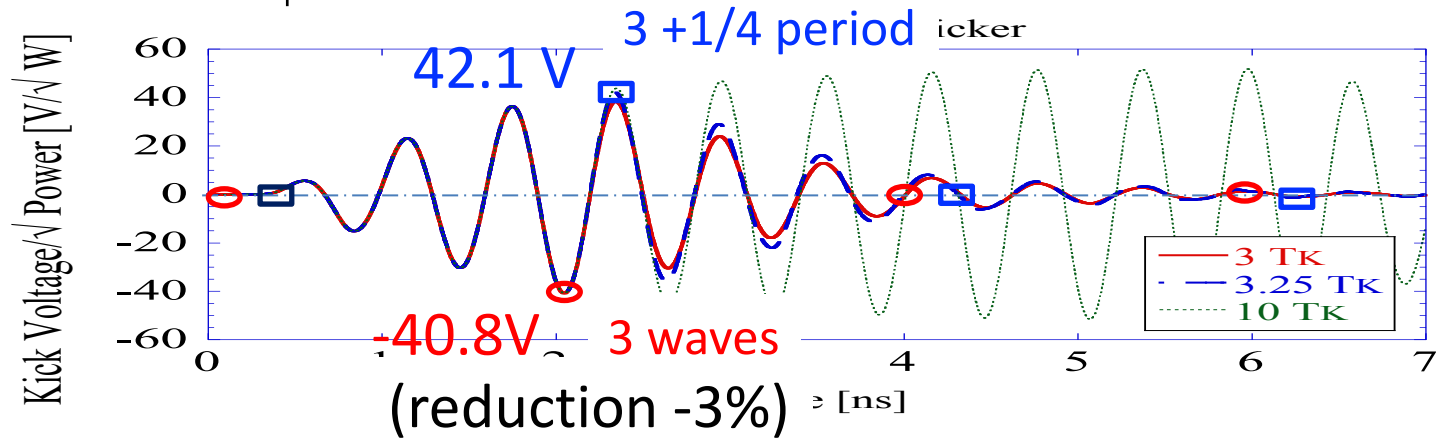
**3 + 1/4** period / bunch spacing @500MHz is preferable

=> Simple drive circuit **without QPSK modulator**

Kicker  
Drive  
Signal



Kicker  
Voltage



# Longitudinal Kicker (Comparison)

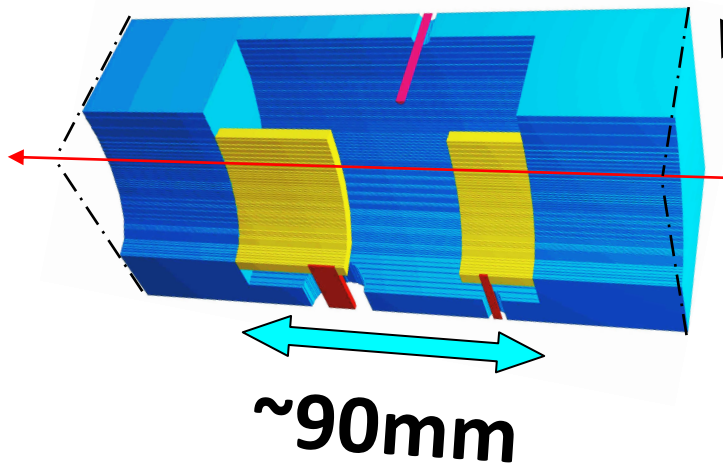
## SPring-8 Type Kicker

1.6 GHz :  $3 + 1/4$  period / bunch

3 period drive : 3% loss

No QPSK modulator

Shunt Impedance  $\sim 1.3 - 1.4 \text{ k}\Omega$



Standard Kicker widely used

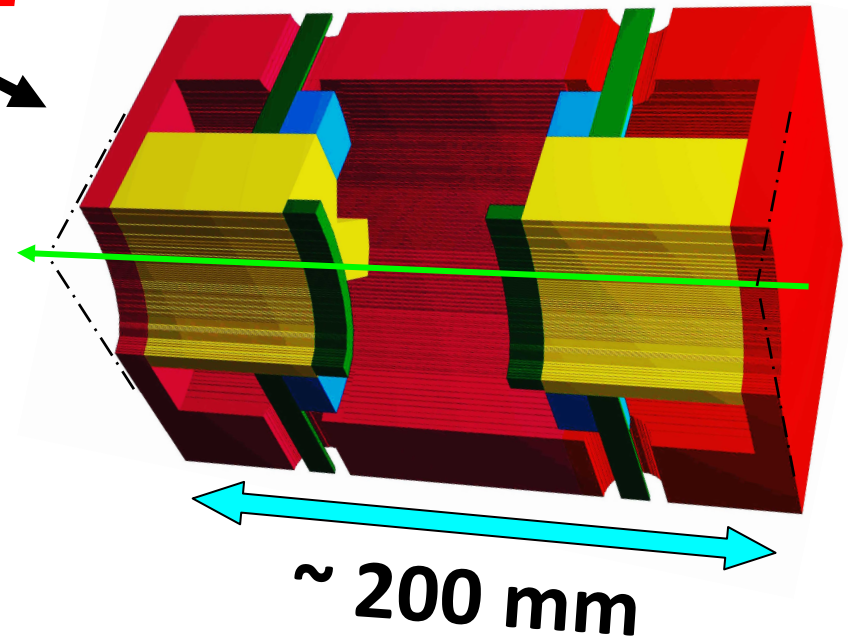
## DAΦNE type Overdamped Cavity

1.4 GHz :

$2 + 3/4$  period / bunch

needs QPSK modulator

( 2 period drive : 20 % loss )

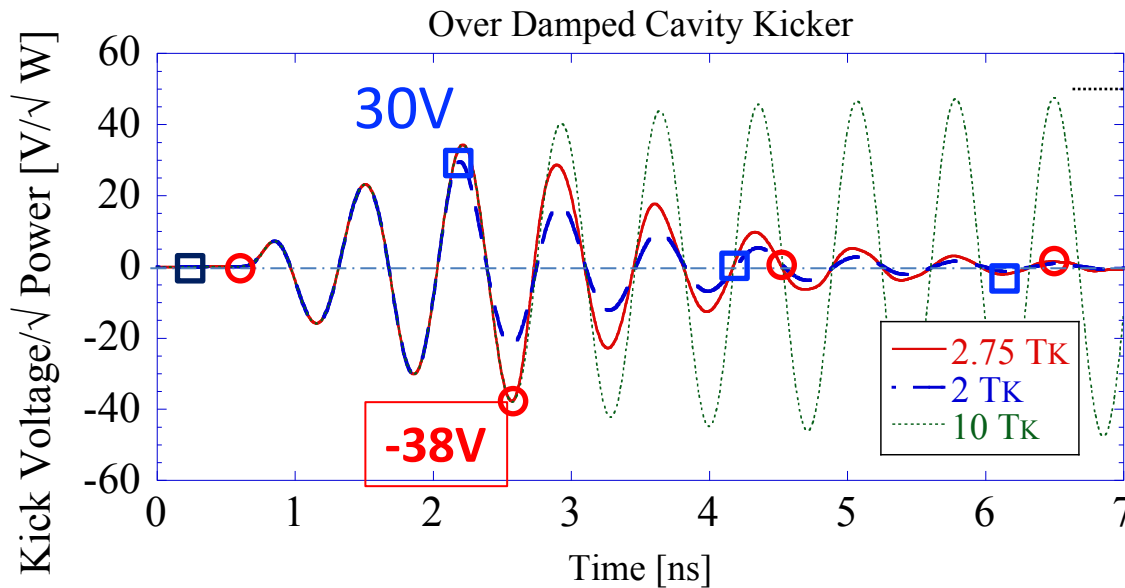
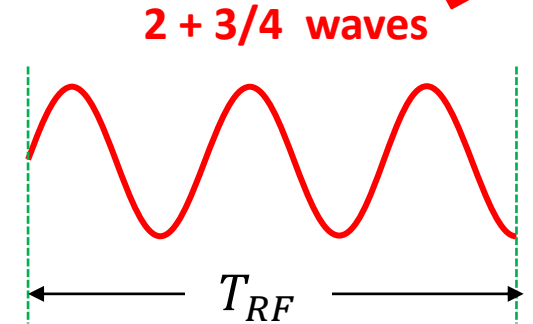
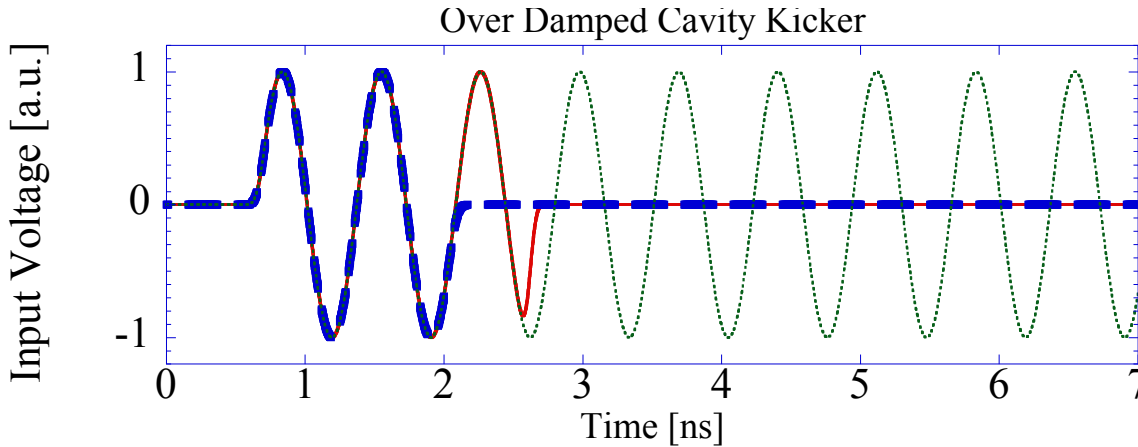
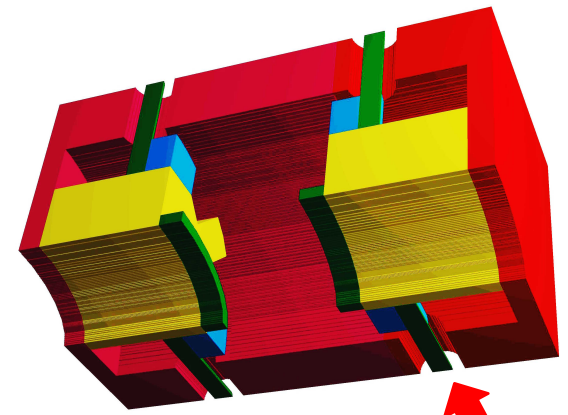


$f_{RF} \sim 500\text{MHz}$  region

BESSYII/SLS/Elettra/TLS kicker shape

# Drive Signal for Overdamped cavity (DAFNE type kicker)

$f_K \sim 1.4 \text{ GHz} \Rightarrow 2 + 3/4$  period / bunch (500MHz)



**48V**

Rsh = 1.14 k Ohm

$$\frac{V_K(2 \text{ wave})}{V_K(2+3/4 \text{ wave})} \sim 80\%$$

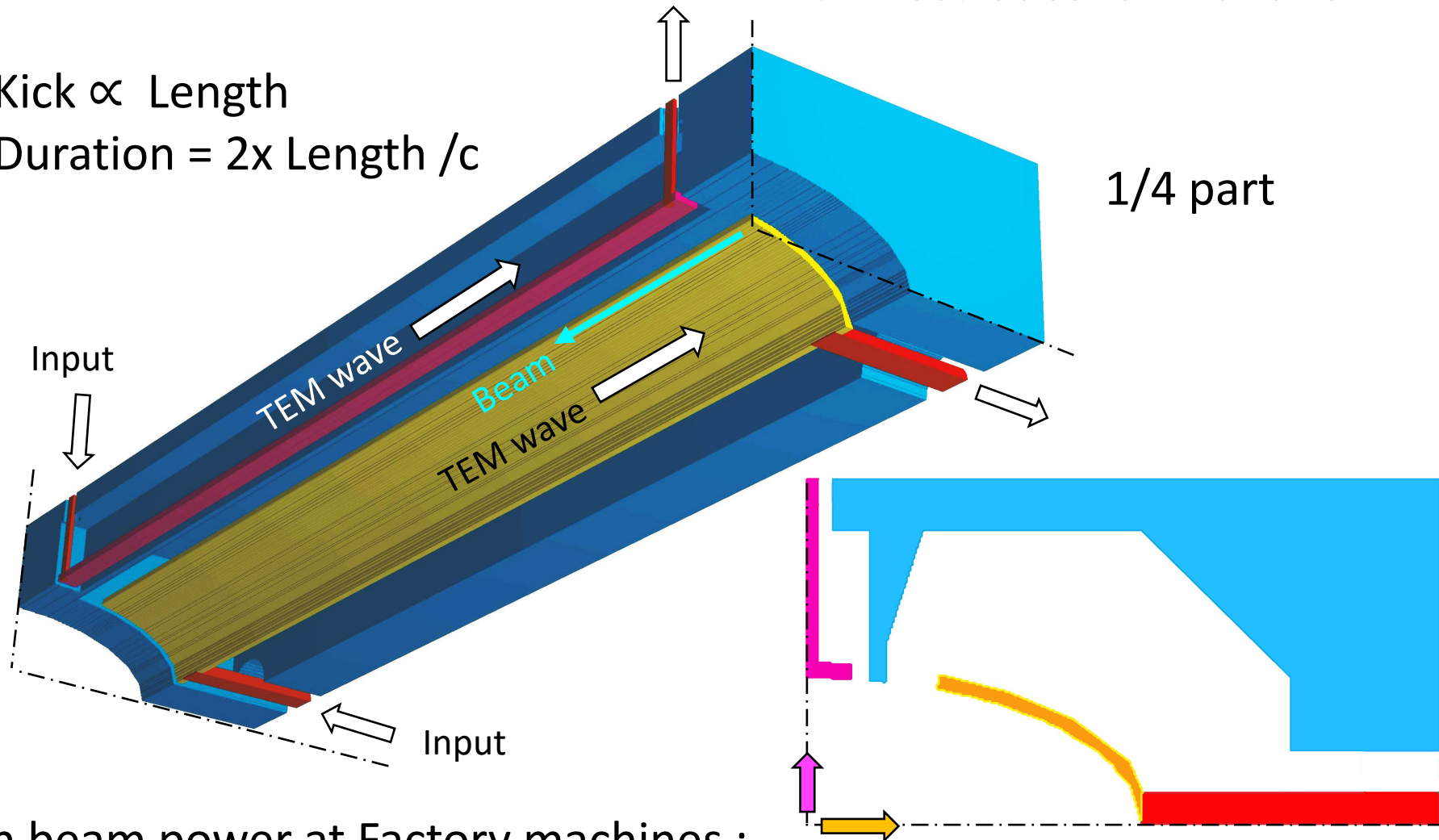
# Example of Transverse Kicker : Stripline type

Length : half of bunch spacing  
30 cm for 500MHz

\* Kick  $\propto$  Length

\* Duration =  $2 \times$  Length / c

Example of Orthogonal Kicker  
with Electrodes for H and for V



1/4 part

High beam power at Factory machines :

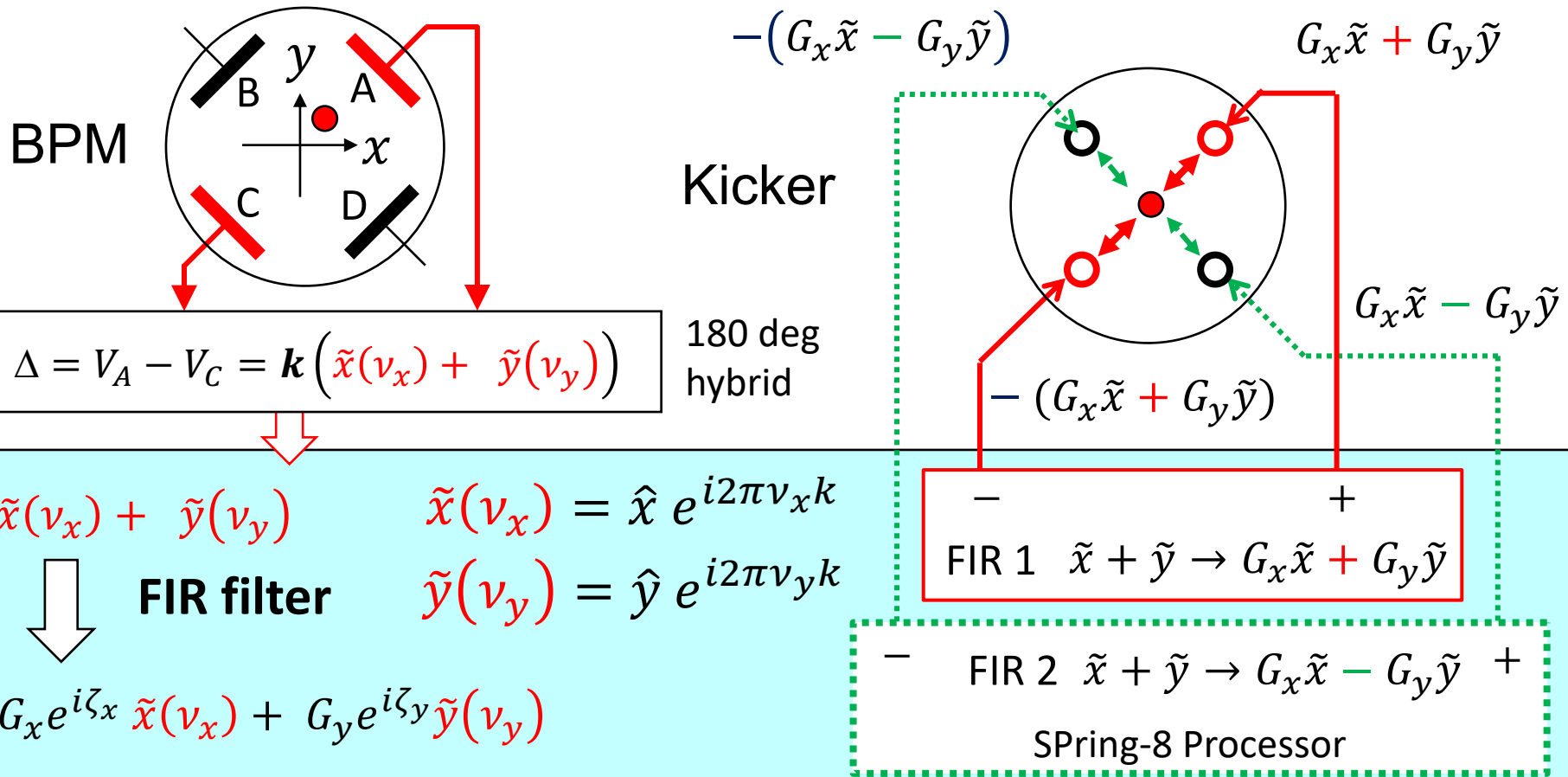
kicker for high current beam is under development ( TobiYama, KEK )

# Single-Loop Two-Dimensional Transverse Feedback

**One Position Signal, One Processor**, for **Horizontal and Vertical feedback**



- \* **Less components, cost and tuning points**
- \* **No special devices** are needed ( but SPring-8 Processor for all kick electrodes)



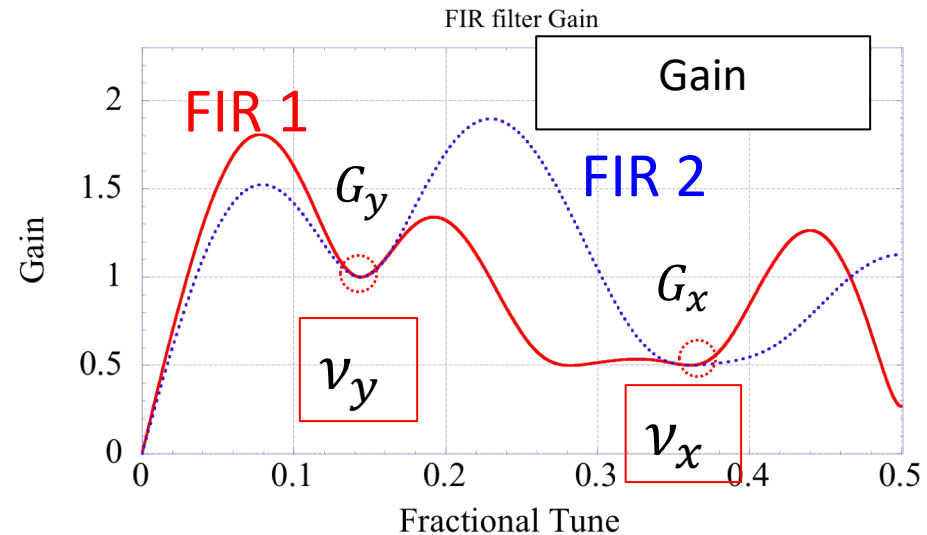
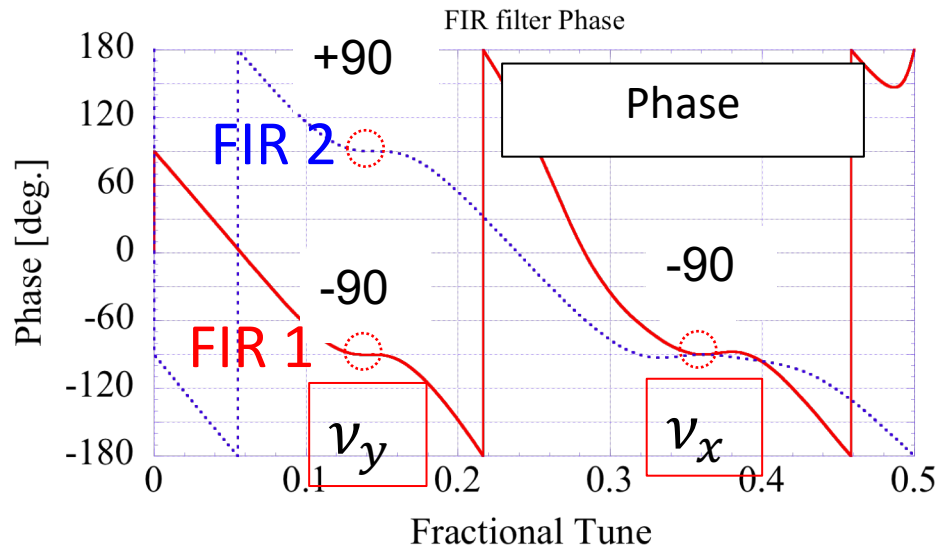
T. Nakamura, et al, EPAC06, "Single-loop Two-Dimensional Transverse Feedback for Photon Factory"

PF, TLS, SOLEIL for their early stage, PLS-II in operation

# PLS-II Two-Dimensional Feedback

$$\text{FIR 1} \quad \tilde{x} + \tilde{y} \rightarrow G_x \tilde{x} + G_y \tilde{y}$$

$$\text{FIR 2} \quad \tilde{x} + \tilde{y} \rightarrow G_x \tilde{x} - G_y \tilde{y}$$



Adjust gain for required damping / acceptance  
with beta function at BPM and Kicker

# Two Tune Drive in Longitudinal Feedback

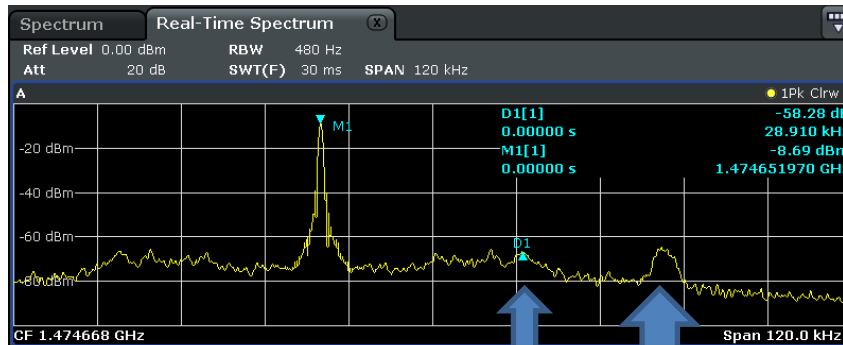
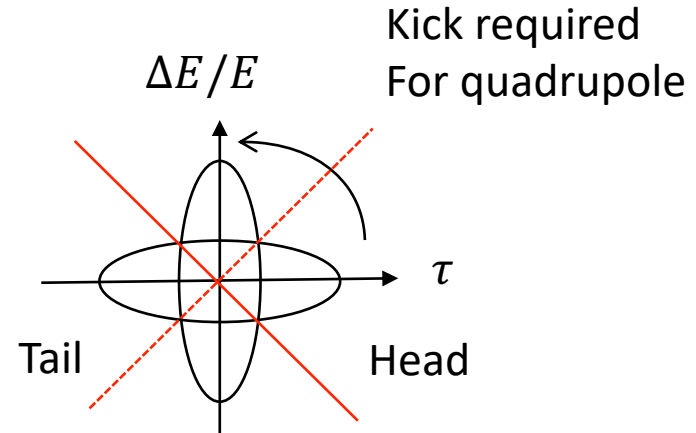
DAΦNE

Longitudinal

Dipole Oscillation  $\nu_s$

Quadrupole Oscillation  $\sim 2\nu_s$

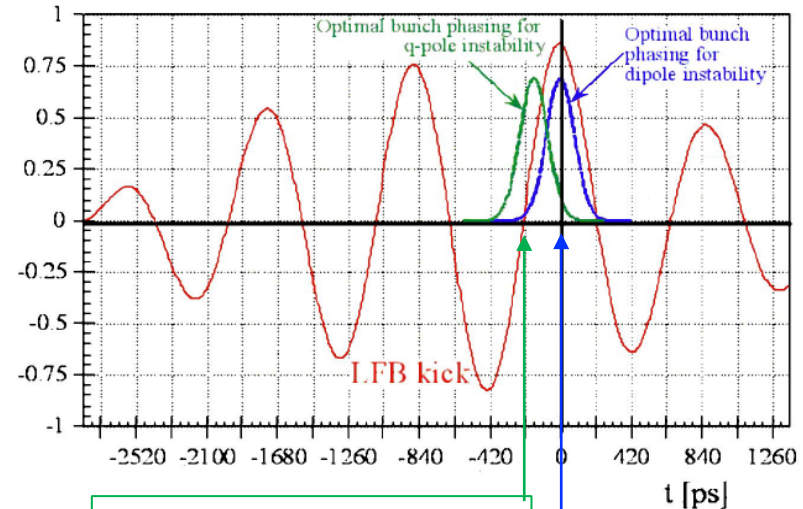
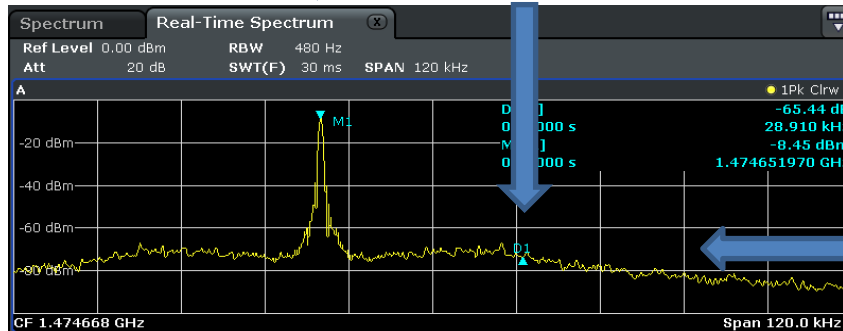
FIR filter optimized for **two tunes** & Kick timing shift



Revolution harmonic

Quadrupole

$\nu_s$   $\sim 2\nu_s$

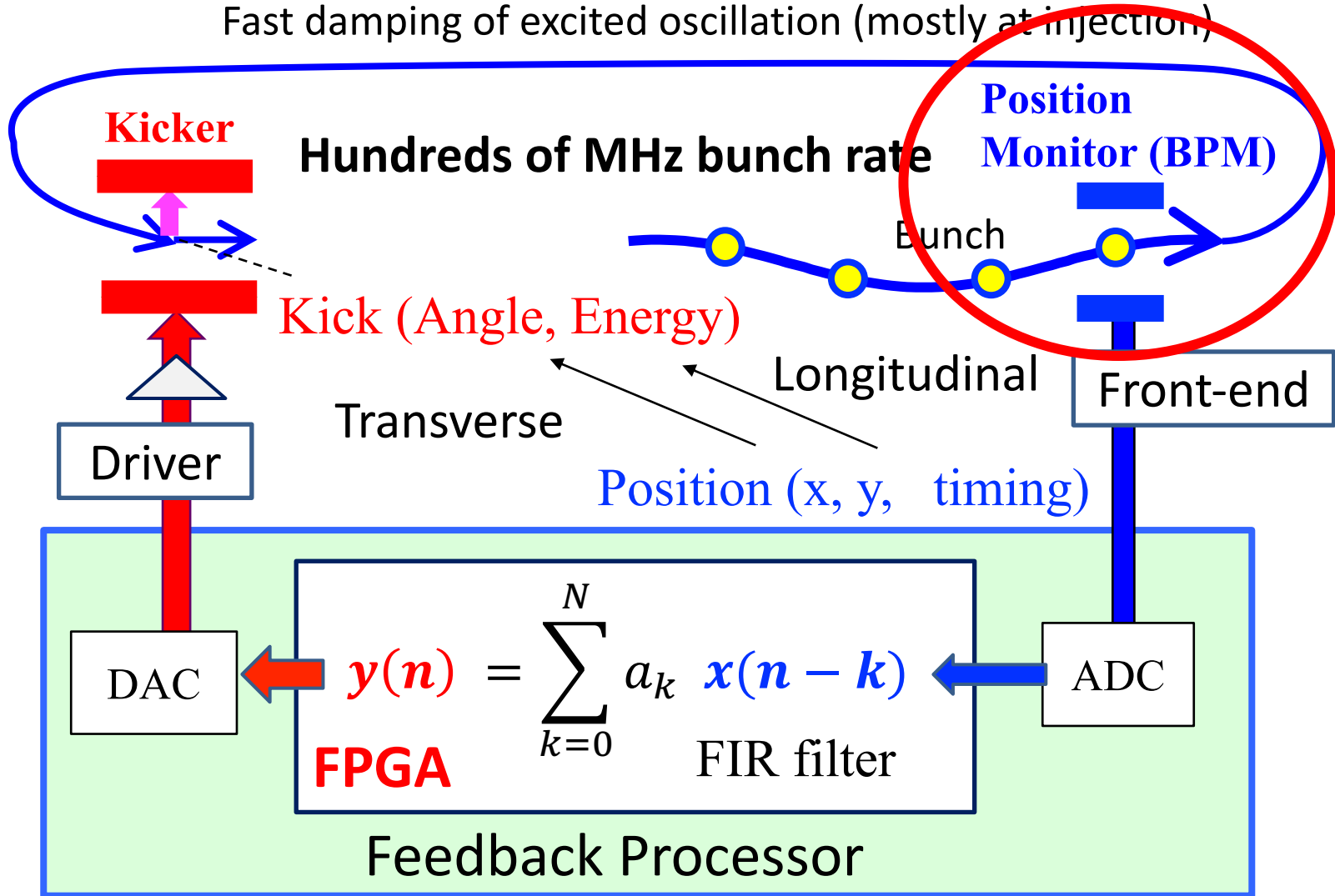


For Quadrupole Kick

For Dipole kick

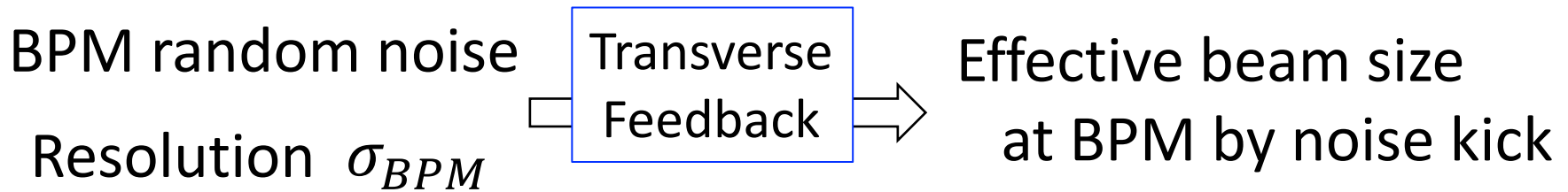
# Transverse and Longitudinal Digital Feedback

Devices for Damping of Betatron or Synchrotron Oscillations  
for Suppression of beam instabilities  
Fast damping of excited oscillation (mostly at injection)



# Increase of beam size by BPM noise

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$$\sigma_x = \frac{\sqrt{\tau_{total} T_0}}{\tau_{FB}} \sigma_{BPM} \sim \sqrt{\frac{T_0}{\tau_{FB}}} \sigma_{BPM}$$

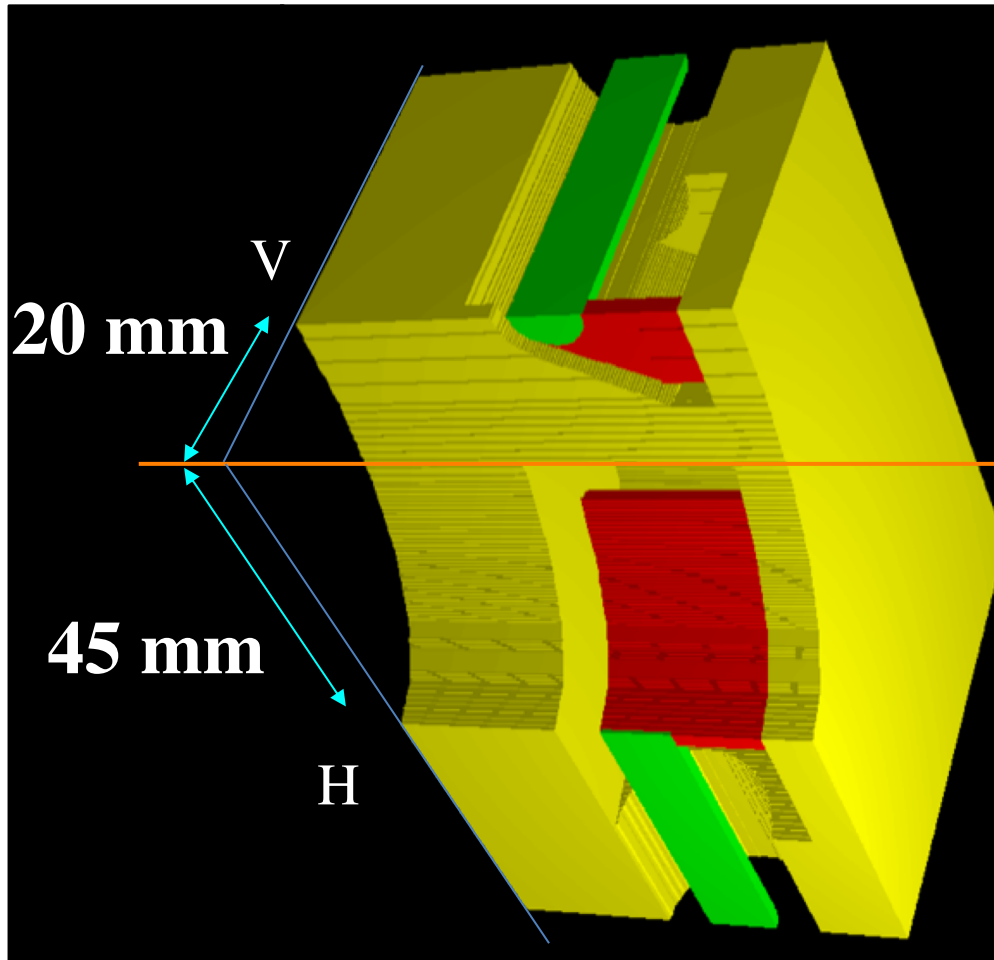
$$\tau_{FB} = 0.5\text{ms} = 100T_0$$

$$\sigma_x = \frac{1}{10} \sigma_{BPM} \ll \text{Vertical Beam size} \sim 5 \mu\text{m}$$

$$\sigma_{BPM} \sim 5 \mu\text{m}$$

for one passage of bunch

# High Resolution BPM by Shorted Stripline Structure



1/4 of structure

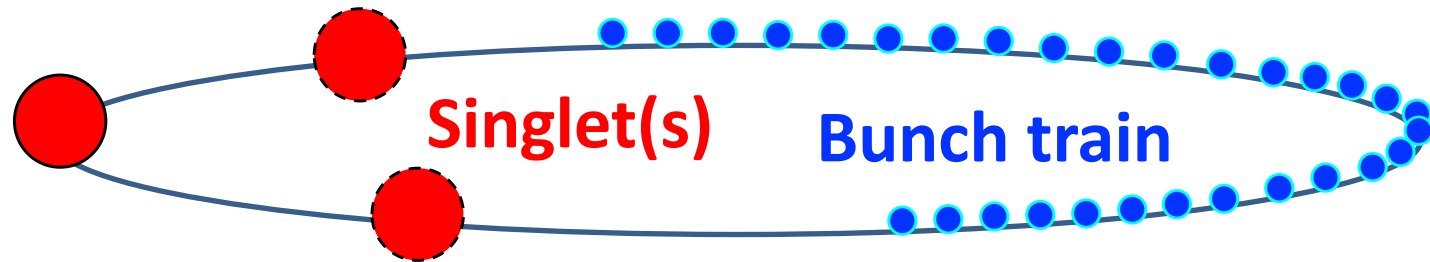
Beam axis

$$\sigma_V = 5\mu\text{m}$$

for 0.2nC bunch  
(= 100mA x 2ns)

# Hybrid Filling

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# Bunch Timing Spread at Hybrid Filling (Localized Filling)

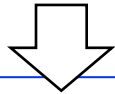
Localized Filling (1/3 fill, 1/14 fill, ... )

at Large Ring ( 5 $\mu$ s revolution )

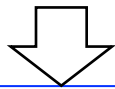
Beam time structure ~ a few  $\mu$ s

Normal RF Acceleration Cavities

Filling time ~ a few  $\mu$ s



Beam Loading by Localized Filling Modulates  
Voltage and Phase of Cavity Voltage



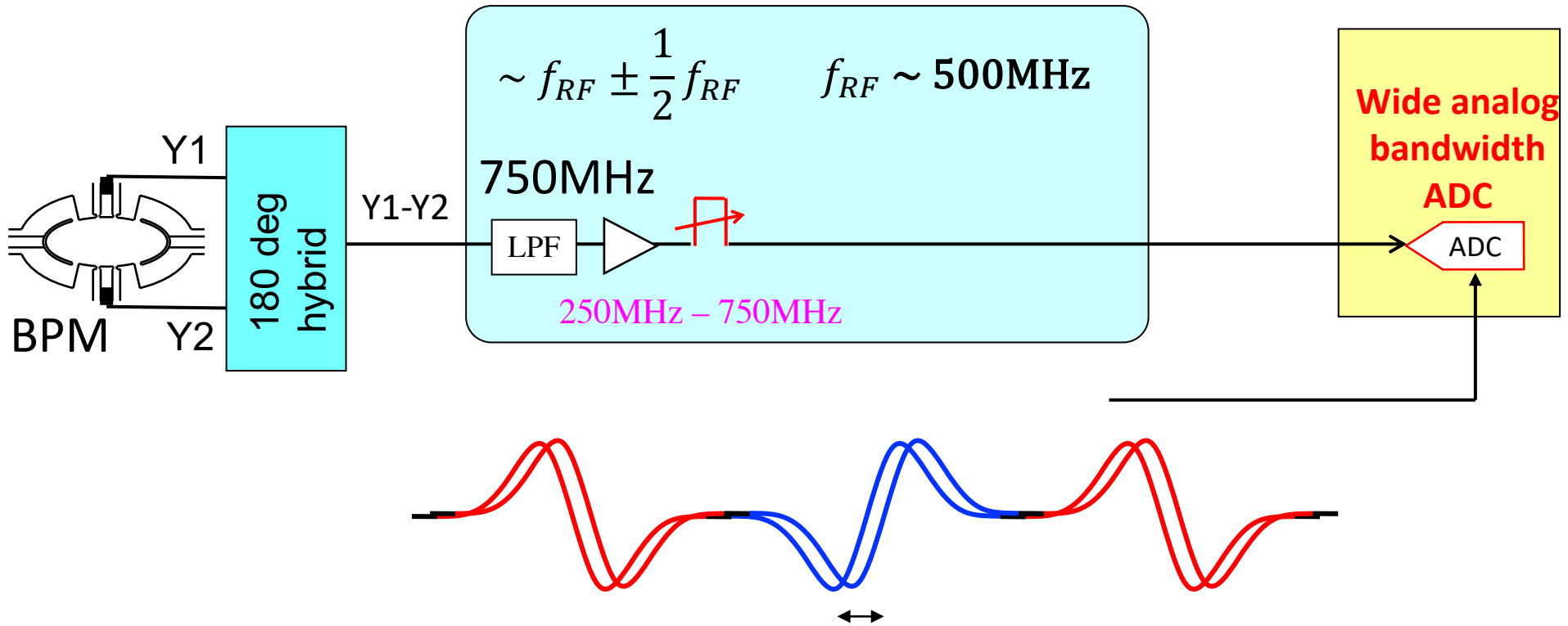
Timing Spread of Bunches  
~ 100ps (SPring-8 case)

We choose Lowest Carrier frequency for BPM

$$n \times f_{RF} = f_{RF} (n=1) \sim 500\text{MHz}$$

for wider acceptance for timing

# Low Carrier Frequency in Front-End



100ps spread (not jitter) is not big problem for 250-750MHz

# Acknowledgement

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Kumagai, M. Shoji, M. Ohishi, K. Tamura,  
and

all feedback people for their exploring the interesting world

Many Reports from the world are presented in IPAC18. Don't miss.

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Information related to this talk is in <http://acc-web.spring8.or.jp/~nakamura>