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39th International Free-Electron Laser Conference

FEL19

Physics of post-saturation tapered FEL towards single-frequency terawatt output power

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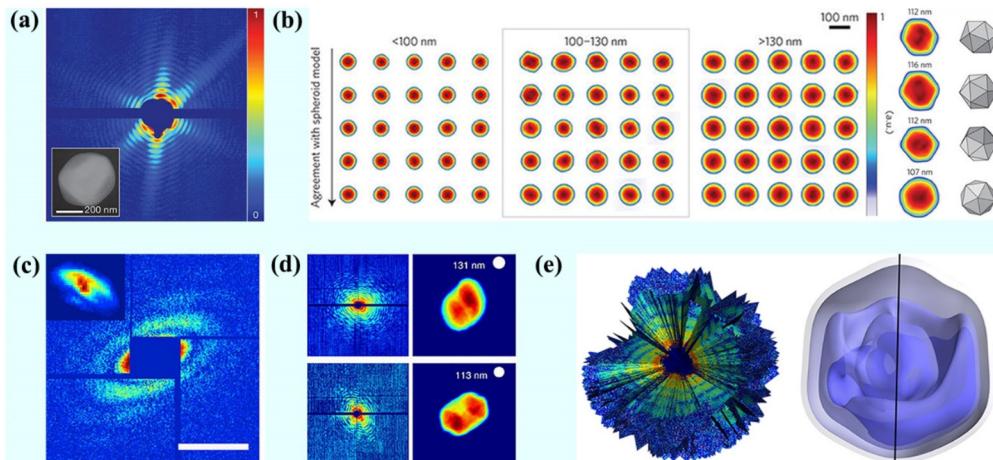
Outline

- Motivations to terawatt (TW) x-ray FEL
- Theoretical approaches to TW XFEL
 - the scope of this presentation
- **Part I:** Sideband instability
 - Summary and discussion
- **Part II:** Radiation diffraction in the post-saturation regime
 - Summary and discussion
- **Part III:** Area-preserving undulator tapering
 - Summary and discussion
- Acknowledgements

Scientific motivations

➤ Coherent diffraction imaging

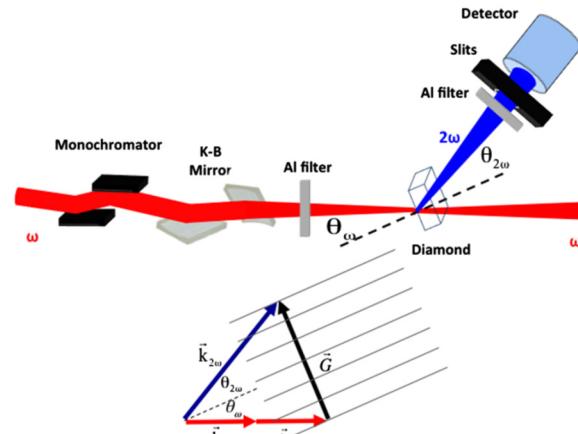
- Femtosecond laser pulse, “diffraction-before-destruction” technique
- Coherent diffractive imaging of biological samples with XFEL



Sun et al., Current Status of Single Particle Imaging with X-ray Lasers, Appl. Sci. 2018, 8(1), 132

➤ High field electrodynamics

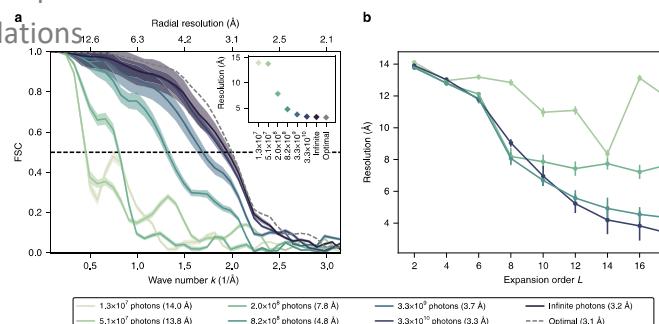
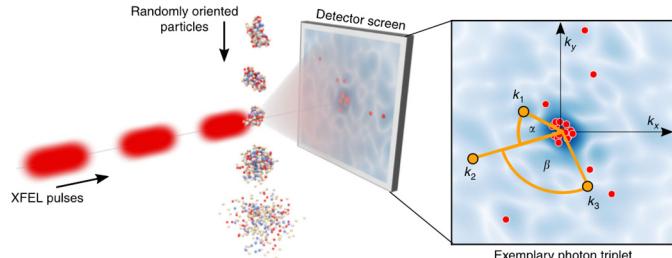
- Femtosecond laser pulse, extremely high power density
- Nonlinear x-ray processes in crystals, test/search strong-field QED phenomena, etc



Shwartz et al., X-Ray Second Harmonic Generation, PRL 112, 163901 (2014)

➤ Single-molecule imaging

- Femtosecond laser pulse, high-repetition rate operation
- Single-molecule scattering and photon correlations



von Ardenne et al., Structure determination from single molecule X-ray scattering with three photons per image, Nature Comm., vol. 9, 2375 (2018)

Motivation

- The above applications set requirements for the laser beam with
 - femtosecond pulse duration
 - number of photons 10^{12} - 10^{14} /pulse
 - photon energy 5~10 keV, pulse energy 5~10 mJ (fundamental mode)
- All these correspond to XFEL output power of 1 TW or higher in a (tens of) femtosecond pulse duration
- Order of magnitude estimate for typical XFEL parameters, the output performance at initial saturation

$$I_b^{\text{pk}} \sim \text{kA}, E_b \sim \text{GeV}, \sigma_{\perp} \sim 20 \mu\text{m}, L_U^{\text{tot}} \sim 50 \text{ m}, \lambda_u \sim \text{cm},$$
$$\rho \sim 10^{-3} \Rightarrow P_{\text{rad}} \approx \rho P_{\text{beam}} \sim 25 \text{ GW}$$

Still a factor of 20~40 before reaching the goal of TW power level

Theoretical studies for TW XFEL

Methodology

- **Analytical/Semi-analytical approach:** simple, idealized model, can give quick estimate, scaling relation
- Numerical simulation: more realistic model, gain physics intuition, suitable for design optimization [e.g., Jiao *et al.* (2012)]
- Typical/proposed schemes to achieve TW FEL (to name a few)
 - **undulator tapering**, to retain resonance condition [KMR (1981)] $\lambda_R = \frac{\lambda_u}{2\gamma_R^2} \left(1 + \frac{K_0^2}{2} \right)$
 - slotted foil plus laser-electron beam delay between undulator sections [e.g., Tanaka (2013)]
 - add multiple slot foils or transverse tilts, use delays to divide electron beam into different parts [Prat *et al.* (2015)]
 - apply multiple phase shifters to amplify a single/target current spike [Kumar *et al.* (2016)]
- In this presentation, we use **semi-analytical approach** and focus on physics involving **undulator tapering** in seeded (x-ray) FEL after saturation, including **sideband instability**, **transverse diffraction**, and **taper scheme** for efficiency enhancement

Schemes

Our focus

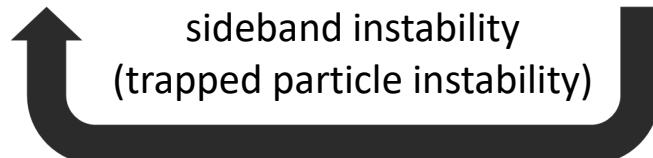
Part I

FEL SIDEBAND INSTABILITY

Ref: C.-Y. Tsai *et al.*, PRAB **20**, 120702 (2017)

FEL simulation (GENESIS)

Phase space bucket → Particles rotate → couple to EM field (w/ freq shift)



1-D FEL system

- Start from 1-D FEL Hamiltonian (in the absence of sideband)

$$\mathcal{H}(\theta, \eta; \hat{z}) = \frac{(\eta - \eta_R)^2}{2f_R} - i \frac{f_B}{f_R} (\mathcal{E} e^{i\theta} - \mathcal{E}^* e^{-i\theta})$$

- The $(2N+1)$ equations of motion

$$\frac{d\theta}{d\hat{z}} = \frac{\partial \mathcal{H}}{\partial \eta} = \frac{\eta - \eta_R}{f_R}$$

$$\frac{d\eta}{d\hat{z}} = -\frac{\partial \mathcal{H}}{\partial \theta} = -\frac{f_B}{f_R} (\mathcal{E} e^{i\theta} + \mathcal{E}^* e^{-i\theta})$$

$$\frac{d\mathcal{E}}{d\hat{z}} = \left(\frac{\partial}{\partial \hat{z}} + \frac{\partial}{\partial \hat{u}} \right) \mathcal{E} = \frac{f_B}{f_R} \langle e^{-i\theta} \rangle$$

- In linear (or exponential) regime, such a system can be well described by the density modulation $b = \langle e^{-i\theta} \rangle$ and the energy modulation $p = \langle \eta e^{-i\theta} \rangle$ (Bonifacio *et al.* 1984)

$$\theta = (k_R + k_u)z - \omega_R t$$

$$\eta = \frac{\gamma - \gamma_{R0}}{\rho \gamma_{R0}}, \eta_R = \frac{\gamma_R - \gamma_{R0}}{\rho \gamma_{R0}}$$

$$\rho = \frac{1}{\gamma_R(0)} \left(\frac{\omega_{pb} K_0 / \sqrt{2}}{4ck_u} \right)^{2/3}$$

$$\mathcal{E} = \frac{E}{\sqrt{4\pi n_0 \rho \gamma_{R0} m_0 c^2}}$$

$$\hat{z} = 2k_u \rho z$$

$$\lambda_R = \frac{\lambda_u}{2\gamma_R^2(0)} \left(1 + \frac{K_0^2}{2} \right)$$

$$K(\hat{z}) = K_0 f_B(\hat{z}) \quad \text{taper profile}$$

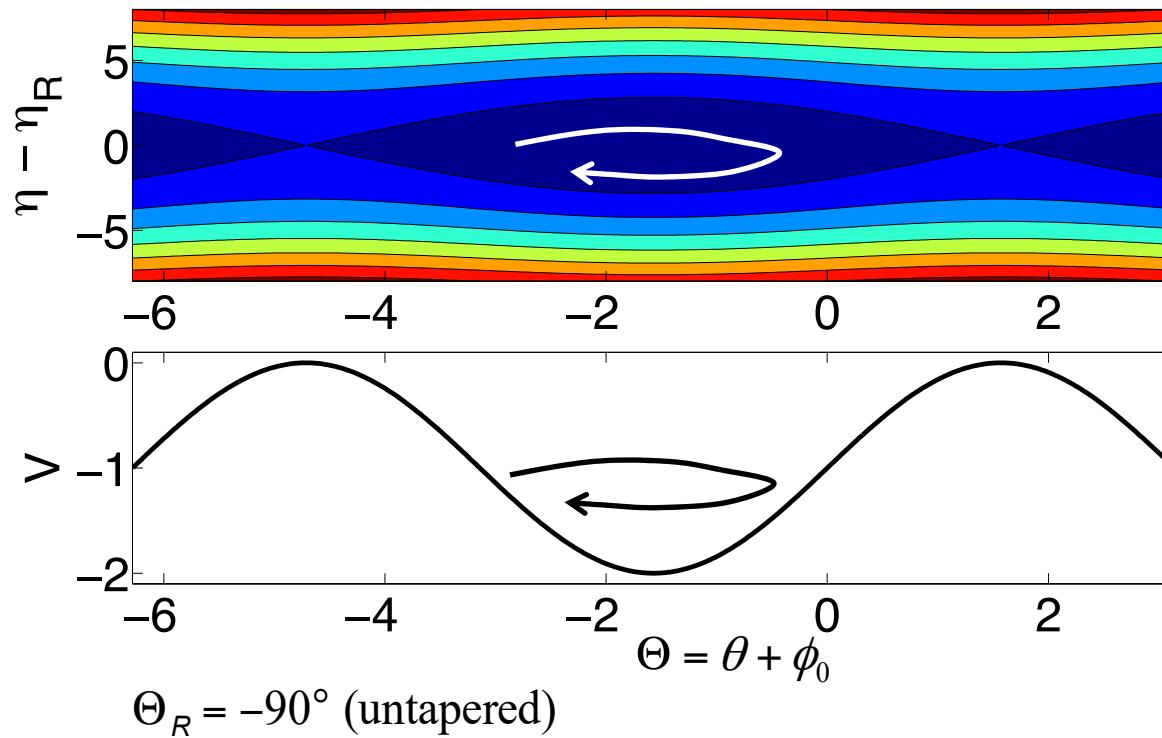
$$\gamma_R(\hat{z}) = \gamma_{R0} f_R(\hat{z})$$

$$f_R(\hat{z}) = \sqrt{\frac{1 + \frac{1}{2} K_0^2 f_B^2(\hat{z})}{1 + \frac{1}{2} K_0^2}}$$

1-D FEL system

- Start from 1-D FEL Hamiltonian (in the absence of sideband)

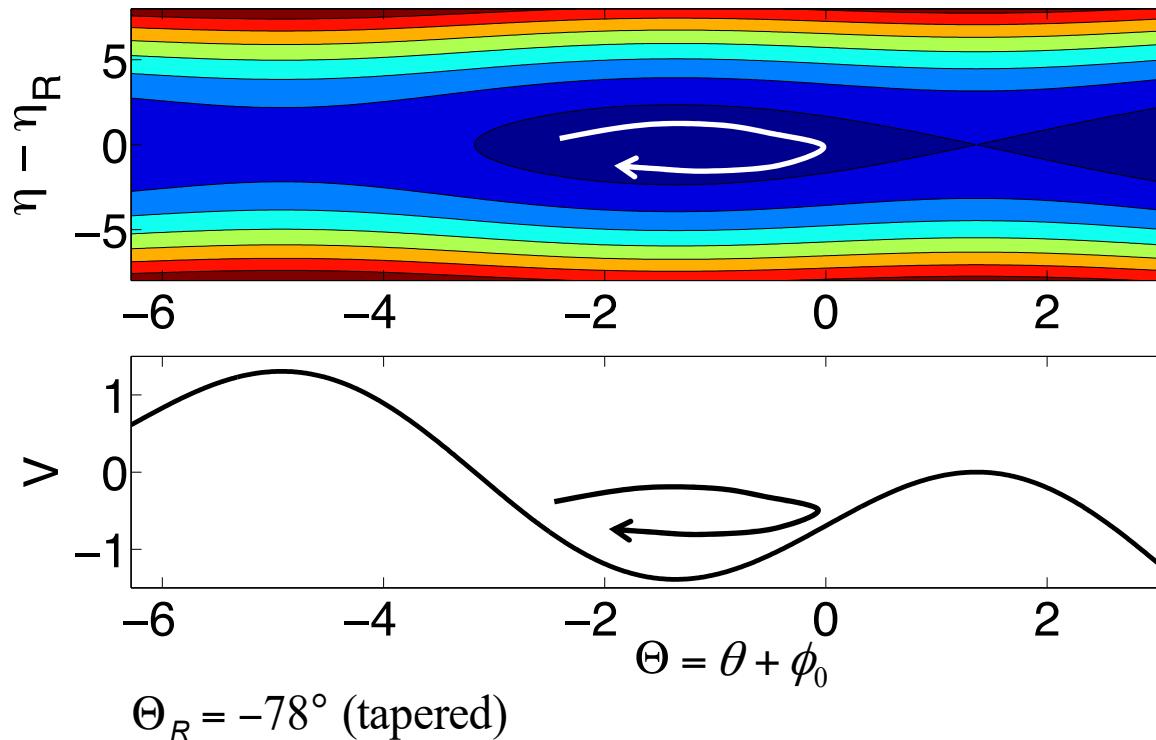
$$\mathcal{H}(\theta, \eta; \hat{z}) = \frac{(\eta - \eta_R)^2}{2f_R} - i \frac{f_B}{f_R} (\mathcal{E} e^{i\theta} - \mathcal{E}^* e^{-i\theta}) = \frac{(\delta\eta)^2}{2f_R} + 2 \frac{f_B(\hat{z})}{f_R(\hat{z})} |\mathcal{E}| [\sin \Theta_R + \sin \Theta - (\Theta + \Theta_R) \cos \Theta_R]$$



1-D FEL system

- Start from 1-D FEL Hamiltonian (in the absence of sideband)

$$\mathcal{H}(\theta, \eta; \hat{z}) = \frac{(\eta - \eta_R)^2}{2f_R} - i \frac{f_B}{f_R} (\mathcal{E} e^{i\theta} - \mathcal{E}^* e^{-i\theta}) = \frac{(\delta\eta)^2}{2f_R} + 2 \frac{f_B(\hat{z})}{f_R(\hat{z})} |\mathcal{E}| [\sin \Theta_R + \sin \Theta - (\Theta + \Theta_R) \cos \Theta_R]$$



Macroparticle model

- To proceed with macroparticle approach, we assume that electrons are deeply trapped in the bottom of the potential well
- In the post-saturation regime, in addition to microbunching, the electron beam begins to rotate in the longitudinal phase space with the small-amplitude synchrotron frequency

$$\frac{d^2}{d\hat{z}^2} \delta\theta + \Omega_{\text{syn},0}^2 \delta\theta = 0 \quad \Omega_{\text{syn},0}^2 = -2 \frac{f_B}{f_R^2} |\mathcal{E}| \sin \Theta_R$$

- It turns out that such electron synchrotron motion will couple EM wave with frequency shift $\omega_s \approx 2c\gamma_R^2 \Omega_{\text{syn},0}$ apart from the main signal
- Usually **undesired**: degrade spectral purity, cause particle detrapping, prevent further growth of the main signal...etc
 - in the following analysis we restrict to onset of the sideband instability

Linear stability analysis

- First order perturbation

– refer the unperturbed solution to that at first saturation

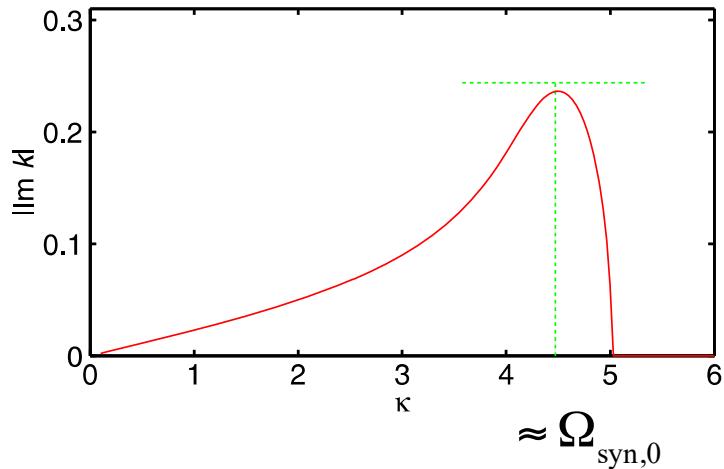
$$\begin{aligned} \mathcal{E} &= (|\mathcal{E}_0| + \delta\mathcal{E}' + i\delta\mathcal{E}^{\prime\prime})e^{i\phi_0} & \Theta &= \theta + \phi_0, \quad \Theta_R = \theta_R + \phi_0 \in \left[\frac{-\pi}{2}, 0 \right] \\ \eta &= \eta_R + \delta\eta & (\delta\theta, \delta\eta, \delta\mathcal{E}', \delta\mathcal{E}^{\prime\prime}) &\propto \text{Re}(e^{ik\hat{z} - i\kappa\hat{u}}) \\ \theta &= \theta_R + \delta\theta, \end{aligned}$$

- Stability is determined by the determinant of the matrix

$$\begin{pmatrix} ik & -f_R^{-1} & 0 & 0 \\ f_R\Omega_{\text{syn},0}^2 & ik & 2\frac{f_B}{f_R}\cos\Theta_R & \frac{f_R}{|\mathcal{E}_0|}\Omega_{\text{syn},0}^2 \\ -\frac{f_R}{2|\mathcal{E}_0|}\Omega_{\text{syn},0}^2 & 0 & i(k-\kappa) & -\frac{f_R}{2|\mathcal{E}_0|^2}\Omega_{\text{syn},0}^2 \\ \frac{f_B}{f_R}\cos\Theta_R & 0 & \frac{f_R}{2|\mathcal{E}_0|^2}\Omega_{\text{syn},0}^2 & i(k-\kappa) \end{pmatrix} \begin{bmatrix} \langle \delta\theta \rangle \\ \langle \delta\eta \rangle \\ \delta\mathcal{E}' \\ \delta\mathcal{E}'' \end{bmatrix} = \mathbf{0}$$

- Given κ , solve $\det(\dots) = \mathbf{0}$ for k (complex quantity, in general)

Linear stability analysis



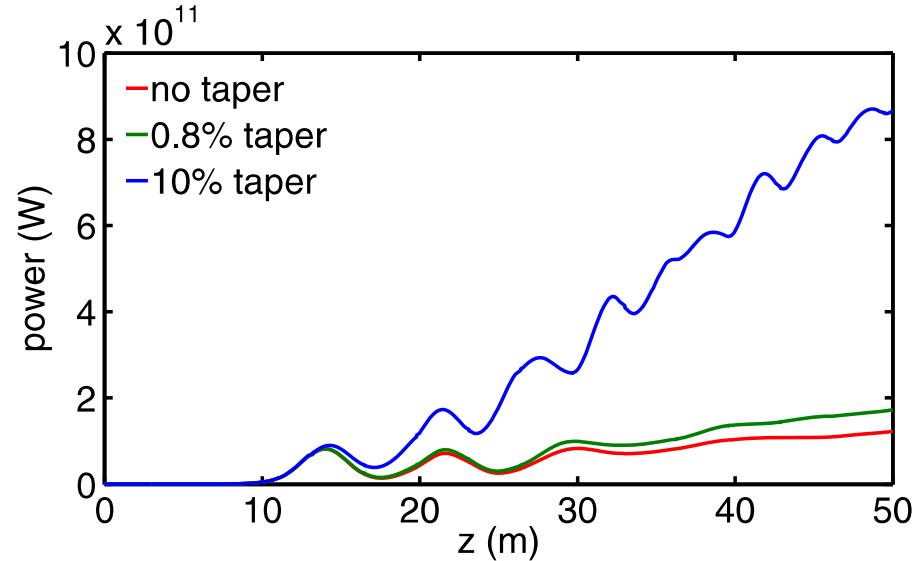
- $\text{Im } k > 0$: growth
- Maximum growth rate corresponds to $\Omega_{\text{syn},0}$, the electron synchrotron frequency
- For untapered FEL, the sideband growth rate remains a constant along z
- For tapered FEL, we may expect z -dependent growth rate

Numerical simulations

- Use LCLS-like beam and undulator parameters
- Taper profile assumed constant- Θ_R , starting location not optimized
- 1-D simulation, only focus on sideband dynamics
- Particle simulation results need postprocessing to extract sideband information

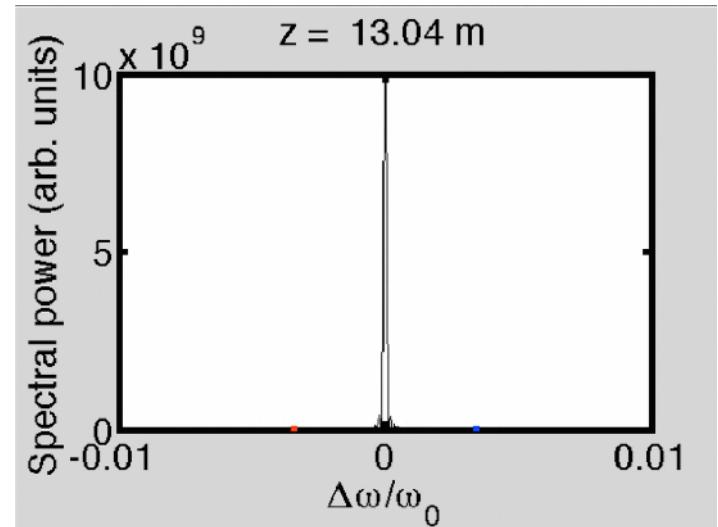
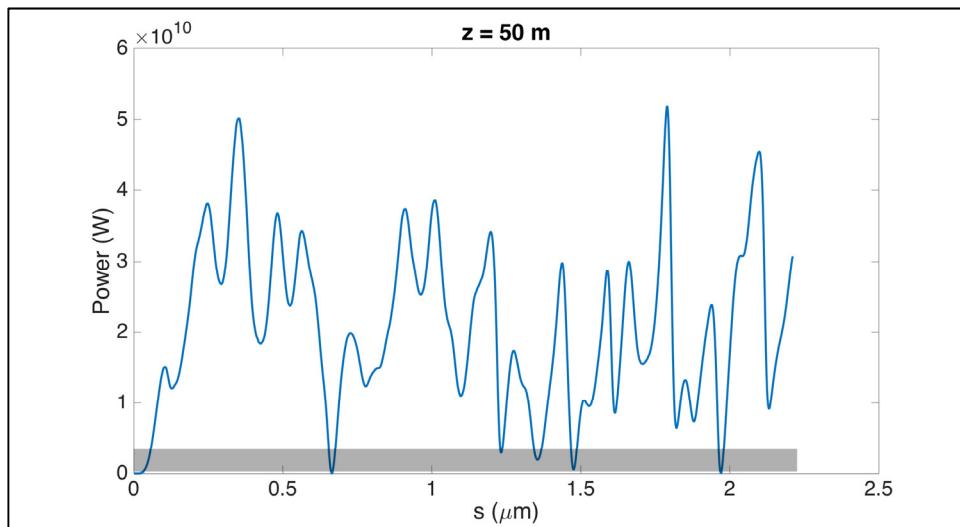
TABLE I. Numerical parameters for the beam, undulator and radiation fields for the hard x-ray FELs.

Name	Value	Unit
Electron beam energy	10.064	GeV
RMS relative energy spread	10^{-4}	
Peak current	4	kA
Normalized emittances (x, y)	0.3,0.3	$\mu\text{m}\cdot\text{rad}$
Average beta function (x, y)	5,5	m
Undulator parameter K_0 (peak)	3.5	
Undulator period	3	cm
Input seed power	1	MW
Resonance wavelength	2.755/4.5	$\text{\AA}/\text{keV}$
First saturation power	~ 80	GW
First saturation length	~ 13	m



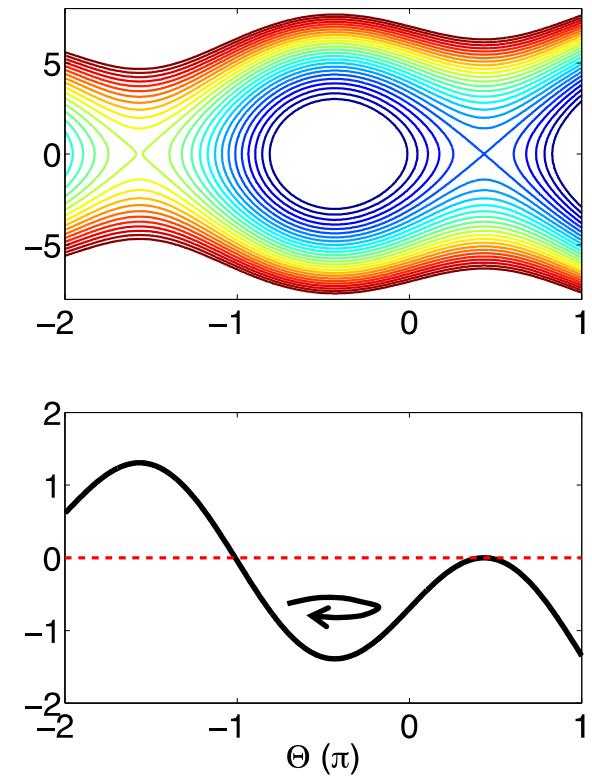
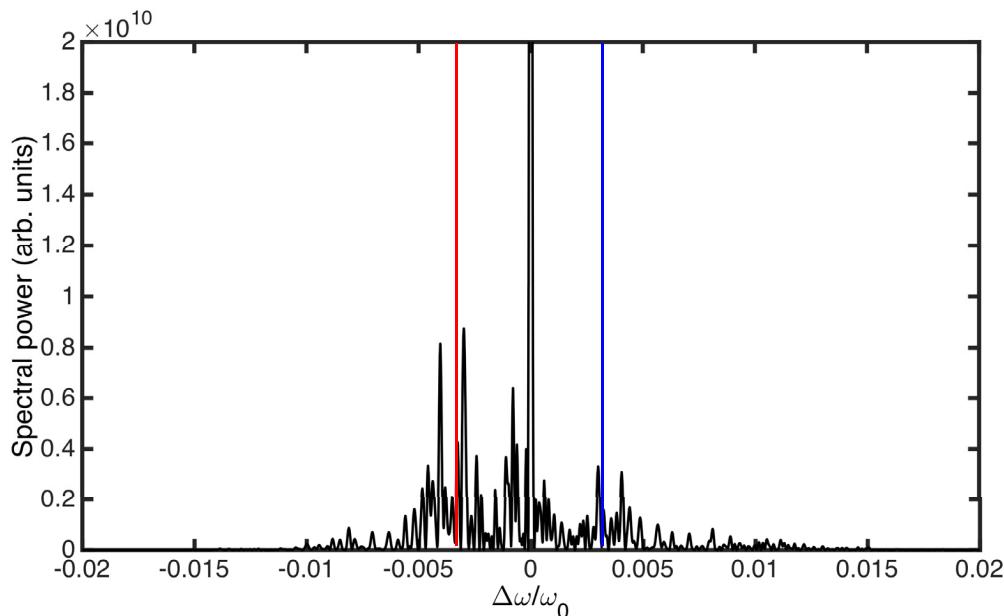
Data postprocessing

- The sideband spectrum can be fluctuating
 - each longitudinal slice responds slightly differently
 - within a slice, electron finite energy spread may result in spread of synchrotron/sideband frequency → finite sideband bandwidth



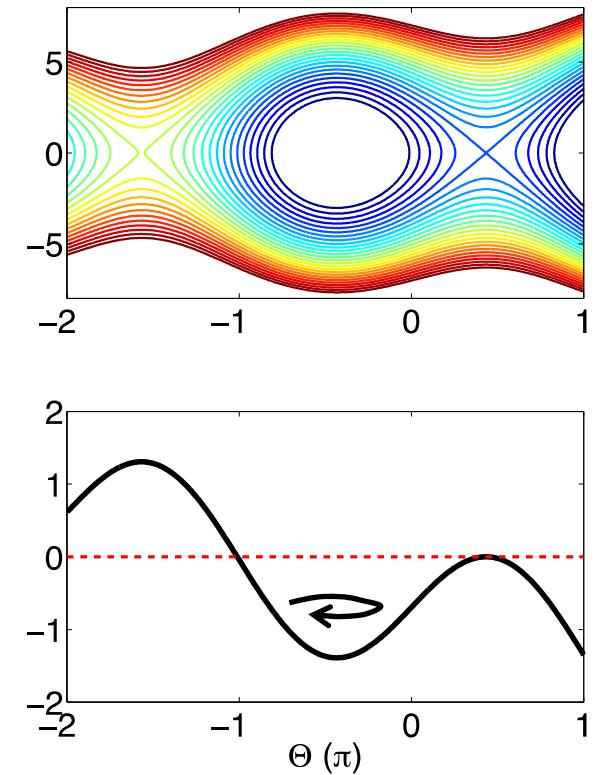
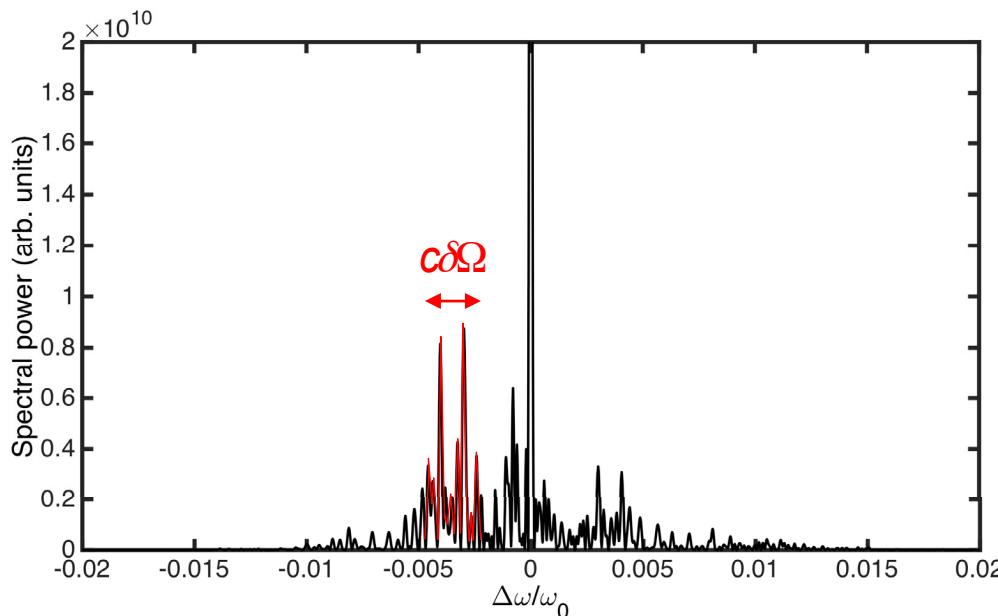
Data postprocessing

- Locate the sideband frequency by $\omega_s^\pm \approx \omega_0 \pm 2c\gamma^2 \Omega_{\text{syn},0}$ (**lower** and **upper**)



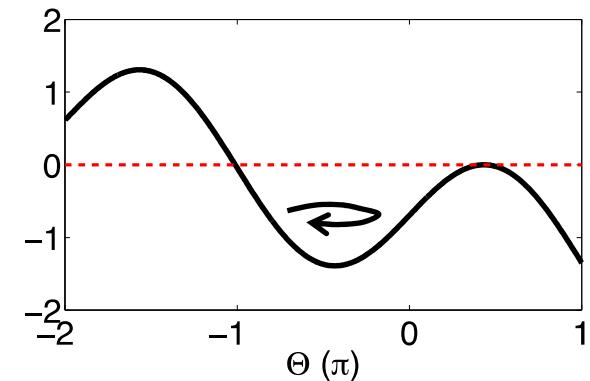
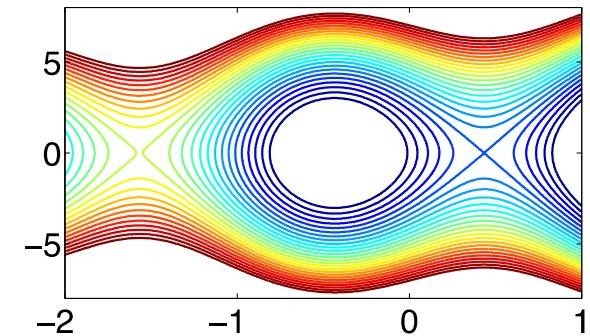
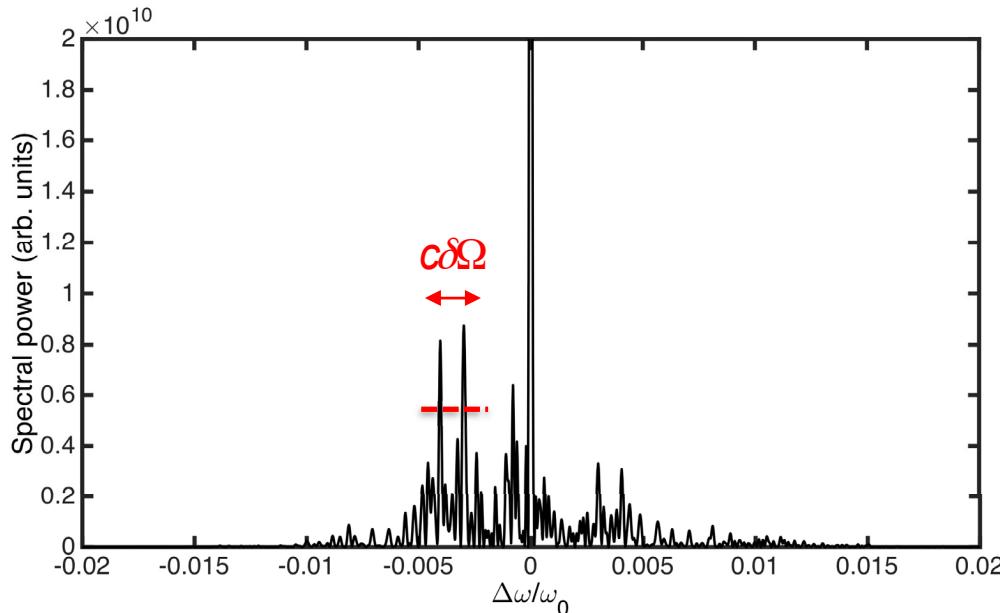
Data postprocessing

- Locate the sideband frequency by $\omega_s^\pm \approx \omega_0 \pm 2c\gamma^2 \Omega_{\text{syn},0}$ (**lower** and **upper**)
- Estimate the spread of sideband (due to finite electron energy spread)

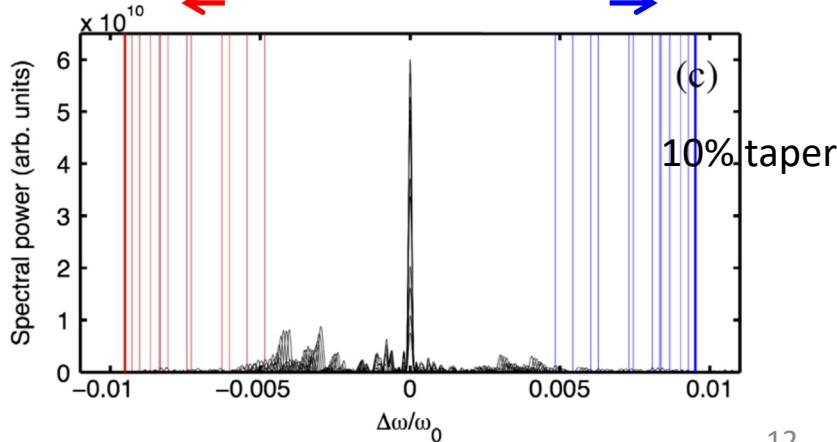
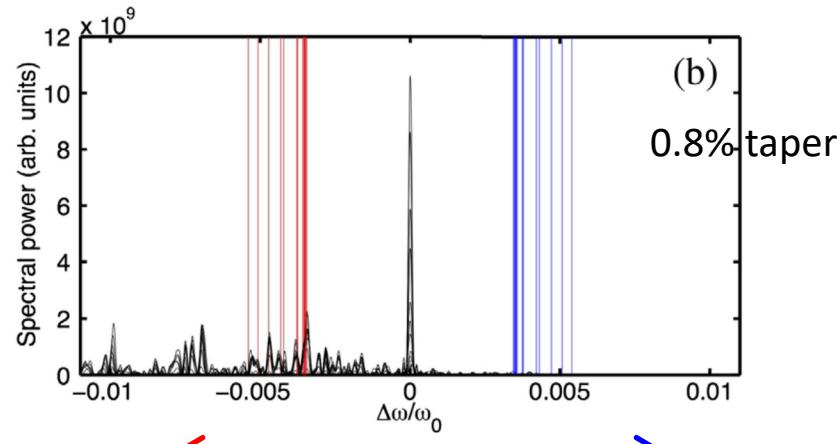
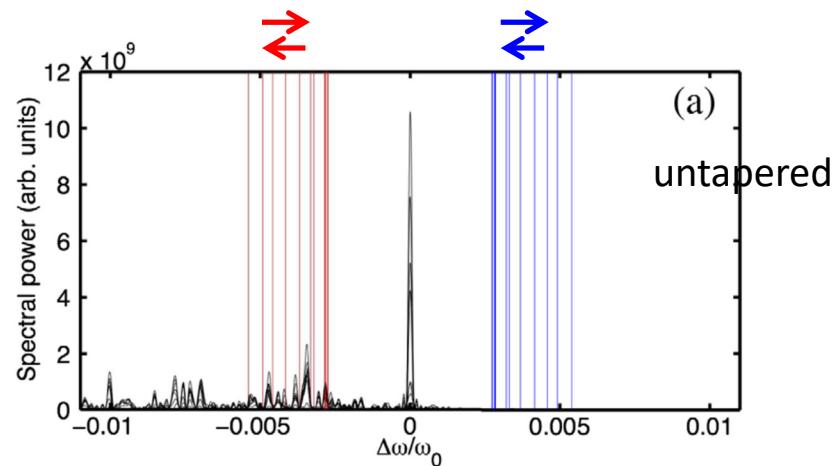
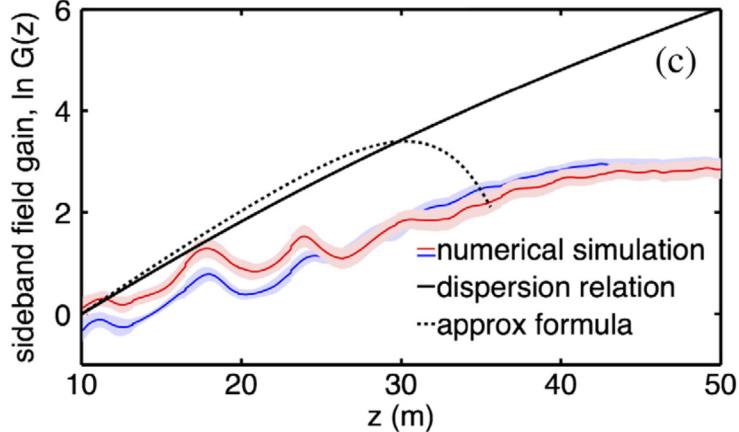
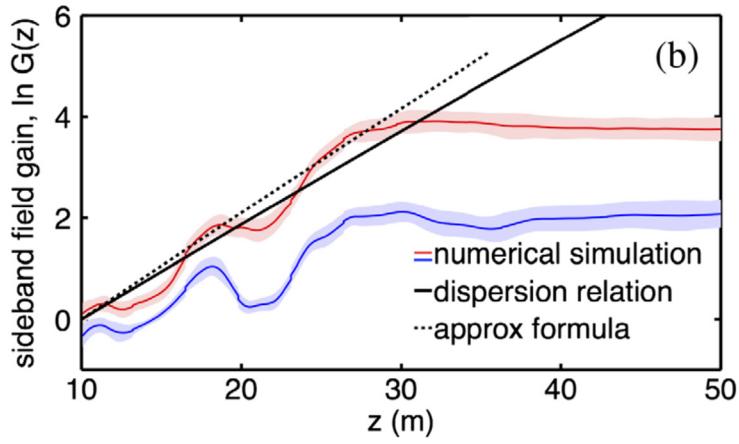
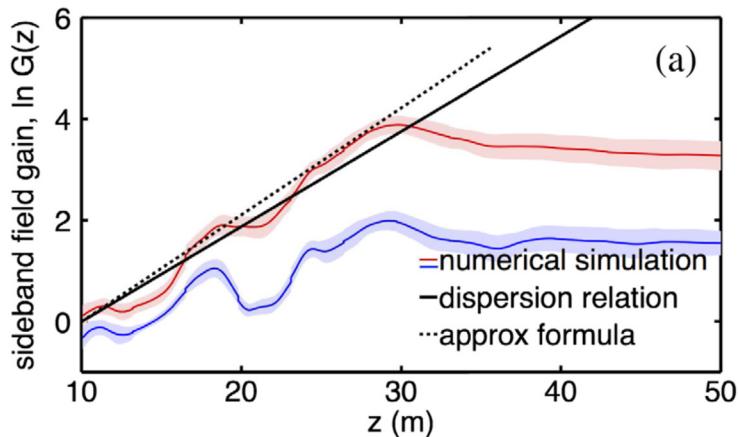


Data postprocessing

- Locate the sideband frequency by $\omega_s^\pm \approx \omega_0 \pm 2c\gamma^2 \Omega_{\text{syn},0}$ (**lower** and **upper**)
- Estimate the spread of sideband (due to finite electron energy spread)
- Take average on the finite sideband bandwidth
- Identify the sideband field



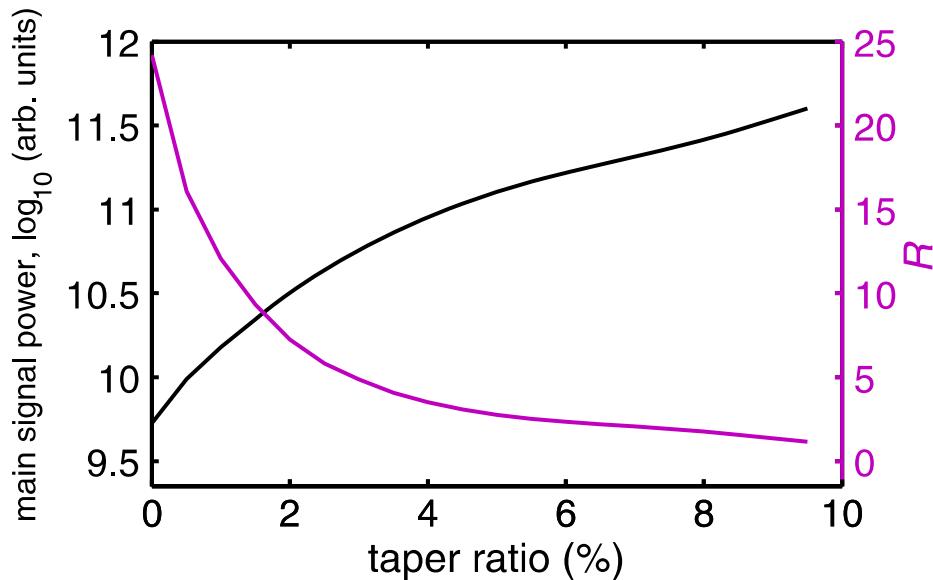
$$G(\hat{z}) \equiv \left| \frac{\mathcal{E}_s(\hat{z})}{\mathcal{E}_s(\hat{z}_b)} \right| = e^{\Lambda(\hat{z})}$$



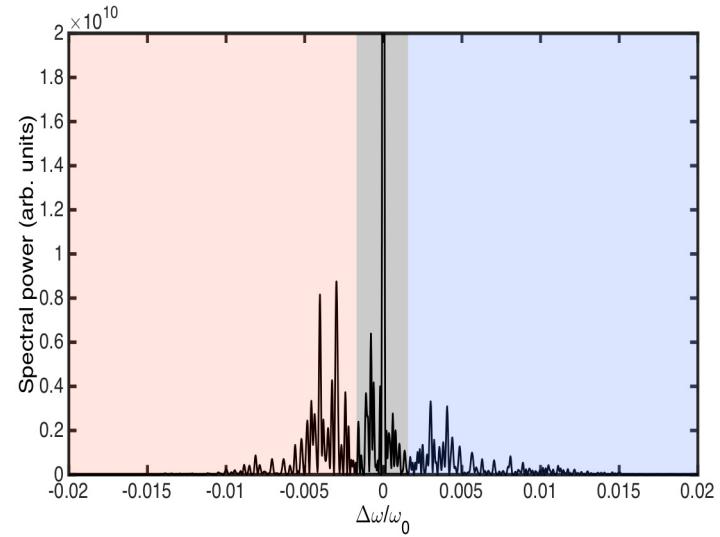
Numerical simulations

- Another way to quantify the sideband contribution is to define the integrated sideband-to-main-signal power ratio

$$R(\Delta) = \frac{\text{spectral power outside } 2\rho}{\text{spectral power within } 2\rho} = \frac{\text{red box} + \text{blue box}}{\text{grey box}}$$



averaged over 50 independent runs for each taper ratio Δ



Part I: Summary and Discussion

- In tapered case, the synchrotron sideband frequency tends to **sweep away** from the main signal
- From the macroparticle analysis, we find that **strong** undulator tapering can help **mitigate** sideband instability in the post-saturation regime
- Effects of undulator tapering on the sideband growth *simply* go into z-dependence of the relevant quantities, e.g., taper profile f_B , main-signal resonance energy change f_R , $|\mathcal{E}_0(\hat{z})|$ and $\Omega_{\text{syn},0}(\hat{z})$
- Comparison of macroparticle model with the 1-D numerical simulation gives **qualitative agreement**
- Other remaining issues for the theoretical model
 - effect of finite-depth electrons in the potential well (we have noticed this when postprocessing the particle simulation results) or the effect of finite energy spread not included
 - the asymmetric sideband growth, transient sideband evolution, effect of various phase space distributions on sideband growth, and second saturation need to be further investigated

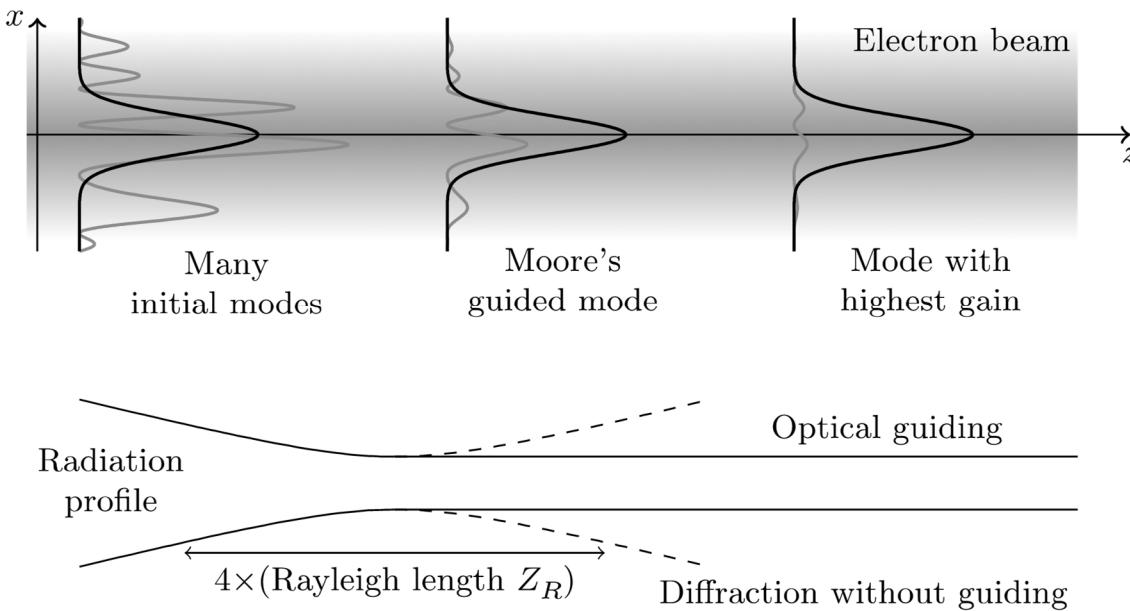
Part II

TRANSVERSE DIFFRACTION IN POST-SATURATION TAPERED FEL

Ref: C.-Y. Tsai *et al.*, PRAB **21**, 060702 (2018)

Transverse diffraction, refractive & gain guiding

- In the **linear** regime the compensation effect (balance) between the natural tendency of radiation diffraction and the presence of electron beam lead to the refractive & gain guiding
- Kroll, Morton and Rosenbluth (1981), Moore & Scharlemann *et al.* (1985)

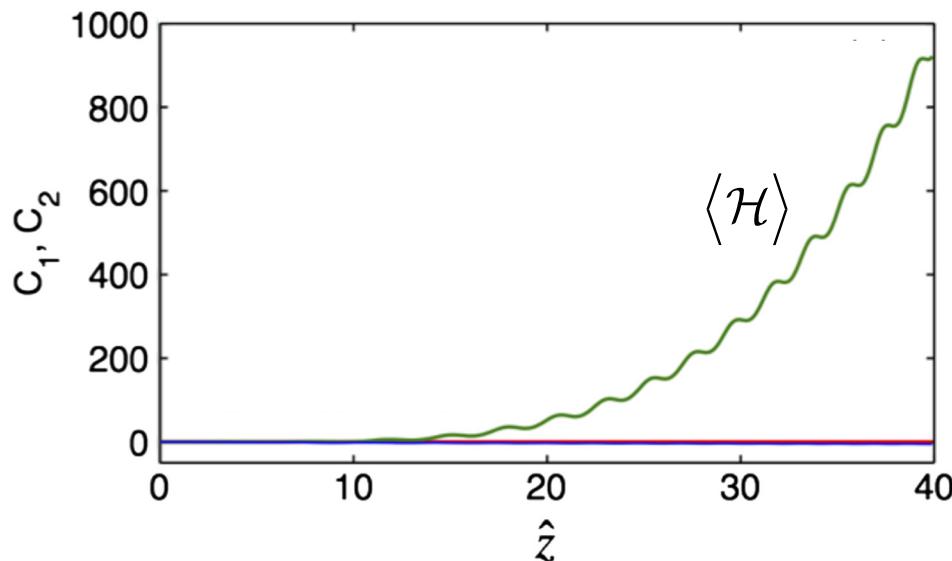


Transverse diffraction in post-saturation regime

- In the **post-saturation** regime, the gain guiding effect becomes reduced by less rapidly growing radiation and gradually increasing radiation beam size
- In the semi-analytical analysis, we rely on the constants of motion (or system invariants)

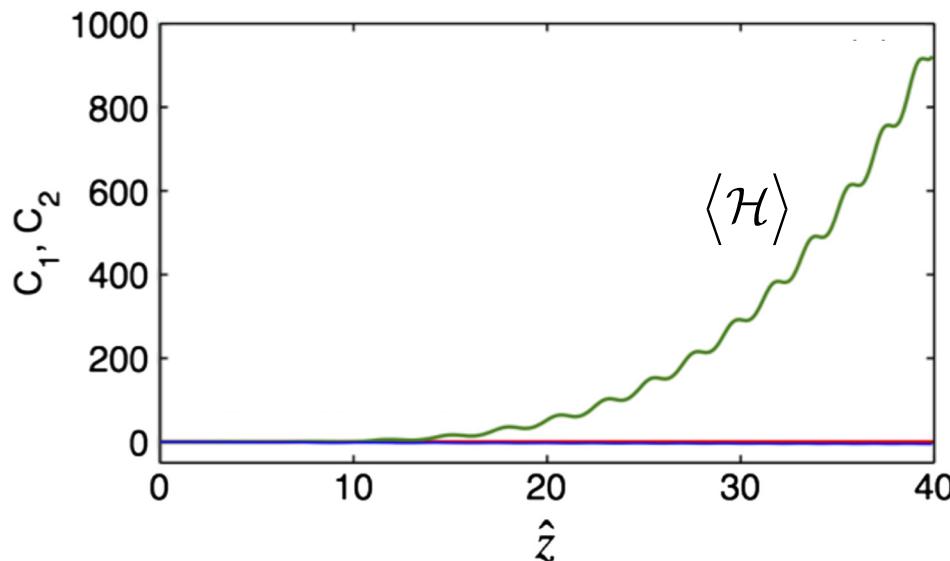
Analysis in post-saturation regime

- Two constants of motion
 - energy conservation $|\mathcal{E}(\hat{z})|^2 + \langle \eta \rangle = C_1$
 - z-independent Hamiltonian
- Gluckstern *et al.*, PRE (1993), Huang and Kim, NIMA (2002) for untapered case



Analysis in post-saturation regime

- Two constants of motion
 - energy conservation $|\mathcal{E}(\hat{z})|^2 + \langle \eta \rangle = C_1$
 - ~~z-independent Hamiltonian phase space action variable~~ $\langle \mathcal{H}(\hat{z}) \rangle / \Omega_{\text{syn}}(\hat{z}) = C_2$



Analysis in post-saturation regime

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 - ~~\hat{z} -independent Hamiltonian phase space action variable~~ $\langle \mathcal{H}(\hat{z}) \rangle / \Omega_{\text{syn}}(\hat{z}) = C_2$
- Parameterize the solution of the radiation field as

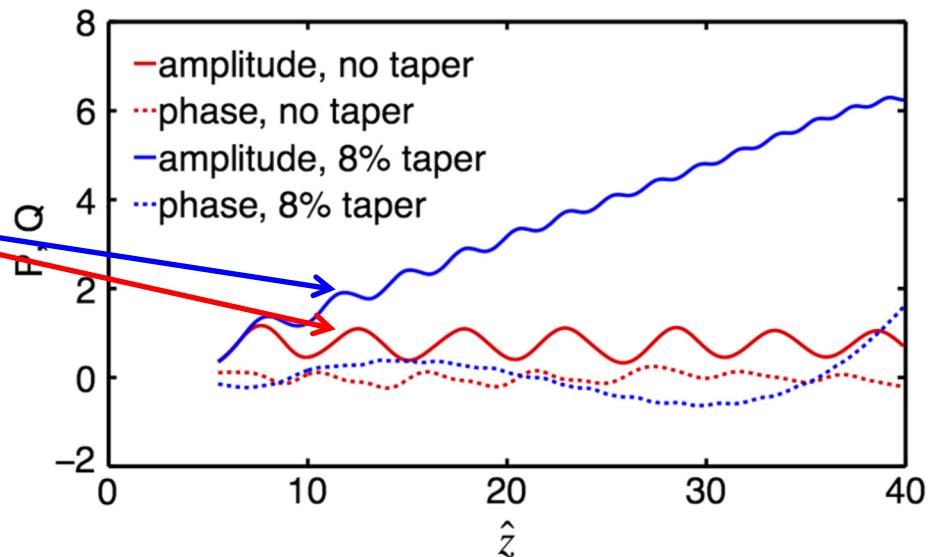
$$\mathcal{E} = (P + iQ) e^{i\Phi}$$

$$\Phi \approx \kappa_0 + \kappa_1 (\hat{z} - \hat{z}_0) + \frac{\kappa_2}{2} (\hat{z} - \hat{z}_0)^2$$

↓

growing part

oscillating part

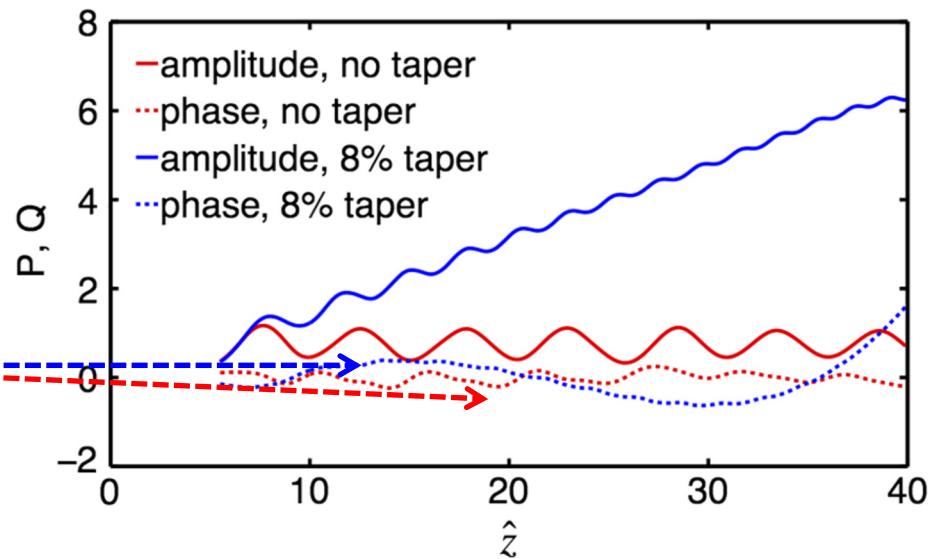
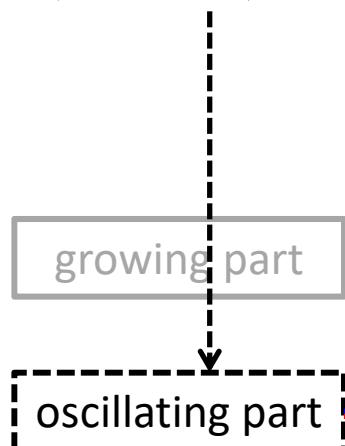


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- Parameterize the solution of the radiation field as

$$\mathcal{E} = (P + iQ)e^{i\Phi}$$

$$\Phi \approx \kappa_0 + \kappa_1(\hat{z} - \hat{z}_0) + \frac{\kappa_2}{2}(\hat{z} - \hat{z}_0)^2$$



Analysis in post-saturation regime

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- Parameterize the solution of the radiation field as

$$\mathcal{E} = (P + iQ)e^{i\Phi} \quad \Phi \approx \kappa_0 + \kappa_1(\hat{z} - \hat{z}_0) + \frac{\kappa_2}{2}(\hat{z} - \hat{z}_0)^2$$

- Assume the electron phase space distribution takes the form

$$f_{\text{BZM}} = \mathcal{N} e^{-\alpha \tilde{I}(\beta, \beta'; \hat{z})}$$

α : particle energy spread in the potential well
 β : displaced electron phase from bottom well
 \tilde{I} : C_2 expressed in the new coordinate

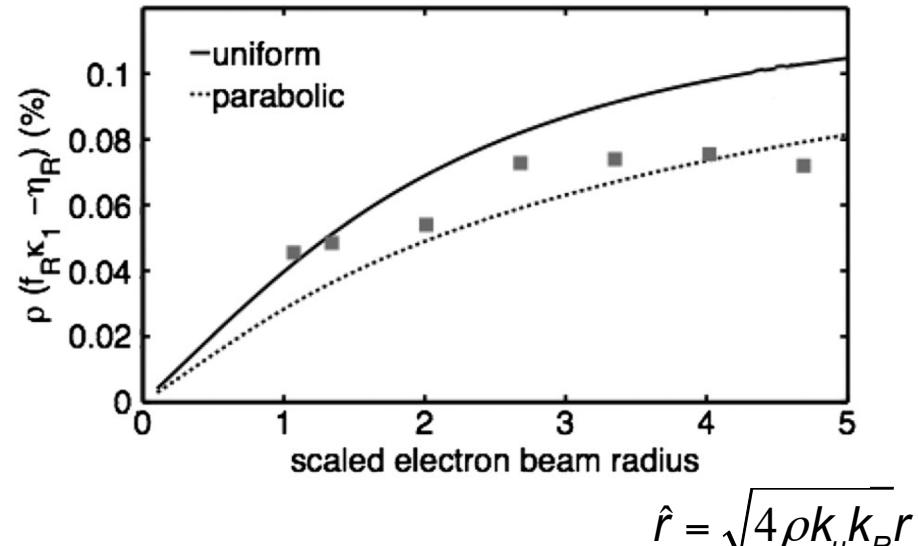
- Field equation including the transverse diffraction

$$\frac{\partial \mathcal{E}}{\partial \hat{z}} - i\nabla_{\perp}^2 \mathcal{E} = \frac{f_B(\hat{z})}{f_R(\hat{z})} U(\hat{r}) \langle e^{-i\theta} \rangle$$

Transverse diffraction in post-saturation regime

- FEL power efficiency

$$f_R \kappa_1 - \eta_R = \frac{\int \hat{r} d\hat{r} P^2(\hat{r}; \hat{z})}{\int \hat{r} d\hat{r} U(\hat{r})}$$

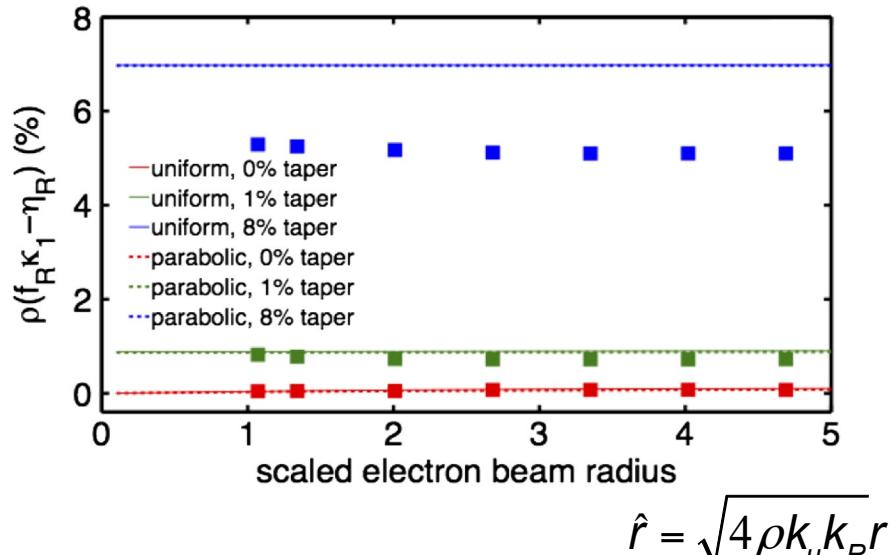


$\rho \approx 1.5 \times 10^{-3}$, based on LCLS-like parameters

Transverse diffraction in post-saturation regime

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$$f_R \kappa_1 - \eta_R = \frac{\int \hat{r} d\hat{r} P^2(\hat{r}; \hat{z})}{\int \hat{r} d\hat{r} U(\hat{r})}$$

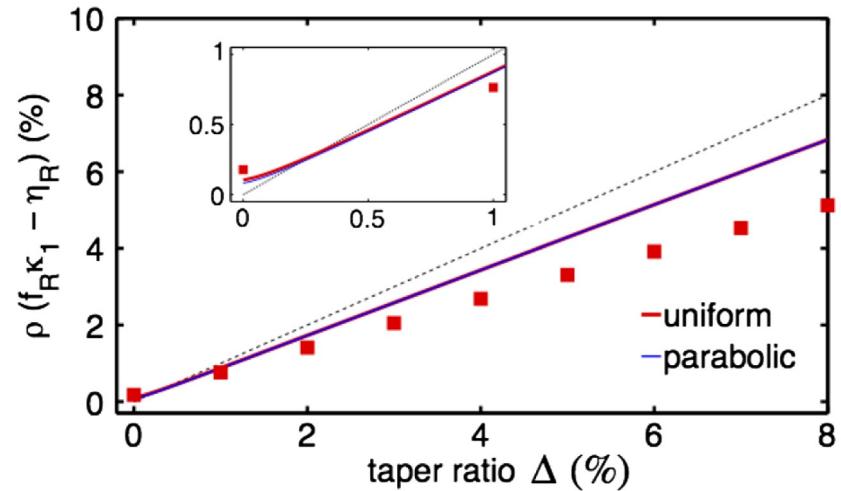


Almost **independence** on the transverse beam size
(Note: the analysis assumed finite beam size but
still zero beam emittance, i.e., no betatron motion)

Transverse diffraction in post-saturation regime

- FEL power efficiency

$$f_R \kappa_1 - \eta_R = \frac{\int \hat{r} d\hat{r} P^2(\hat{r}; \hat{z})}{\int \hat{r} d\hat{r} U(\hat{r})}$$

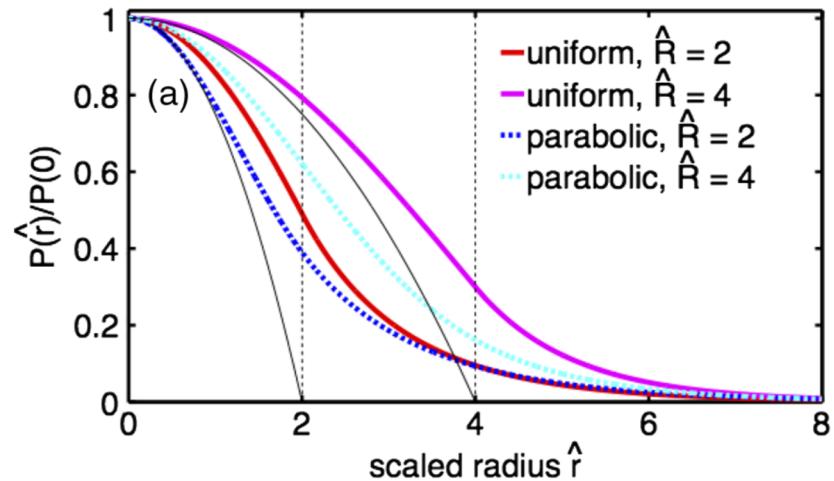


Power efficiency \leq total taper ratio Δ ($\neq 0$)

Transverse diffraction in post-saturation regime

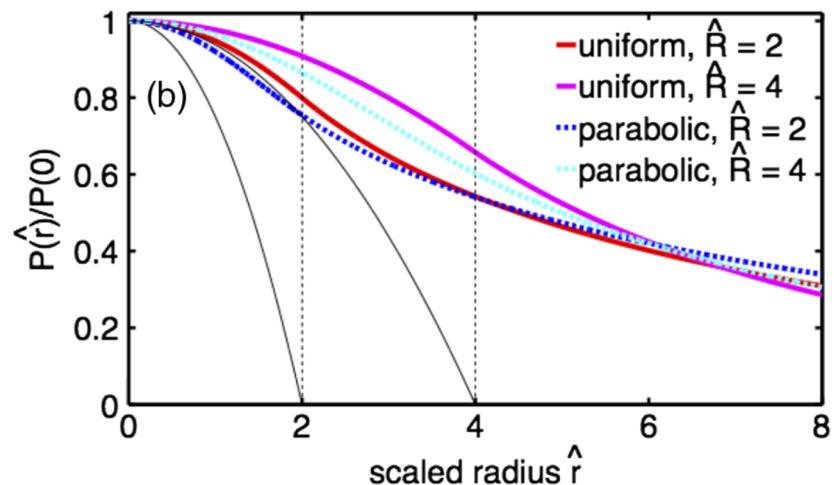
- Transverse radiation field profile

untapered



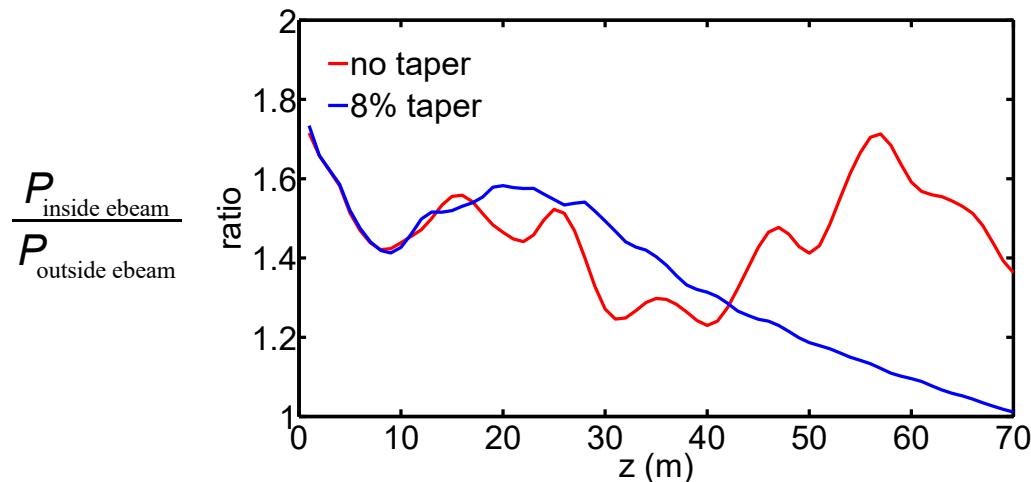
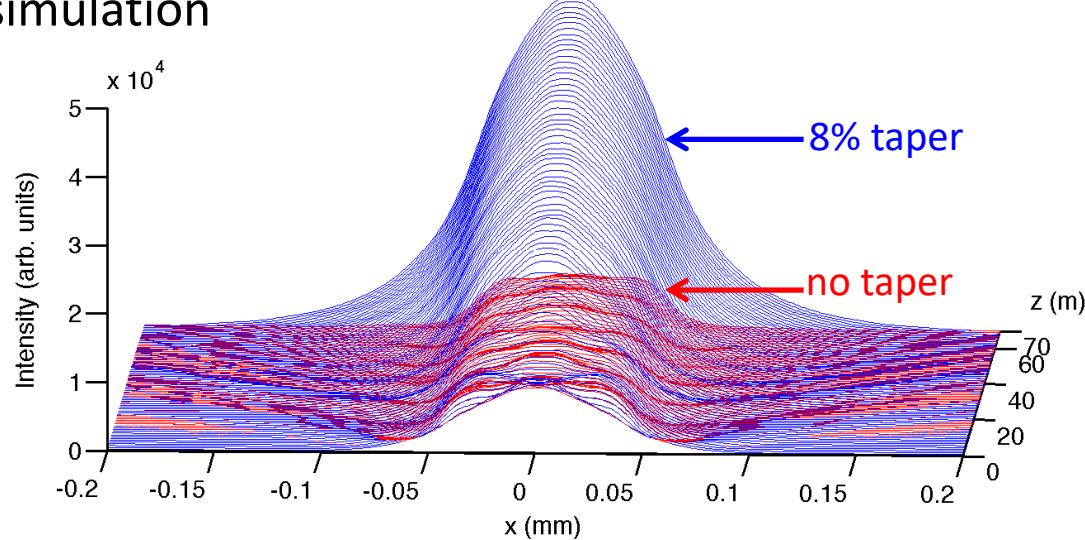
8% taper

More of the enhanced radiation field is contributed **from outside** of the transverse electron beam **than inside**



Transverse diffraction in post-saturation regime

- GENESIS simulation



Part II: Summary and Discussion

- Although FEL dynamics in the post-saturation regime becomes more involved than the linear regime, we may analyze it by taking advantage of the integrals of motion
- Tapered power efficiency is **almost independent** on the transverse beam size (for the case of weak or absent transverse focusing)
- Tapered power efficiency can be close to (smaller than) the total taper ratio, if the taper design is optimized
- In the deep saturation regime, **more** field intensity is contributed from **outside** of the transverse electron beam **than** that from **inside**
- Other remaining issues for the theoretical model
 - Further extension of the semi-analytical formulation to include transverse electron beam emittance should provide a useful tool for FEL design consideration of post-saturation undulator line
 - combine with sideband instability analysis

Part III

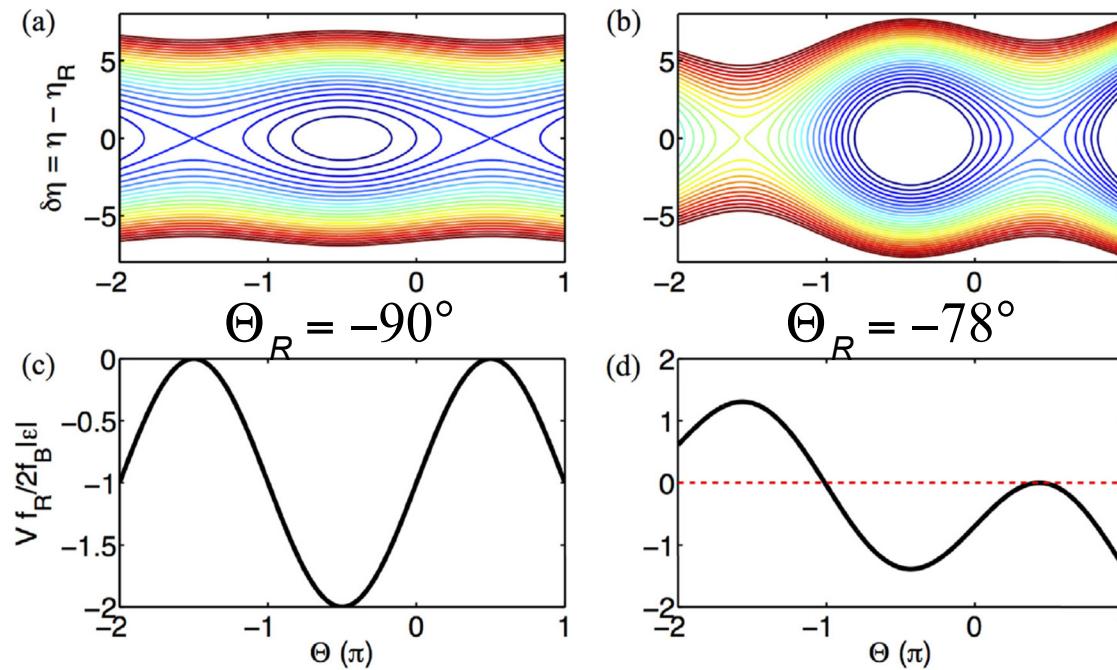
AREA-PRESERVING TAPER SCHEMES FOR HIGH-EFFICIENCY FEL

Ref: C.-Y. Tsai *et al.*, NIMA **913**, 107-119 (2019)

1-D analysis: action-angle transform

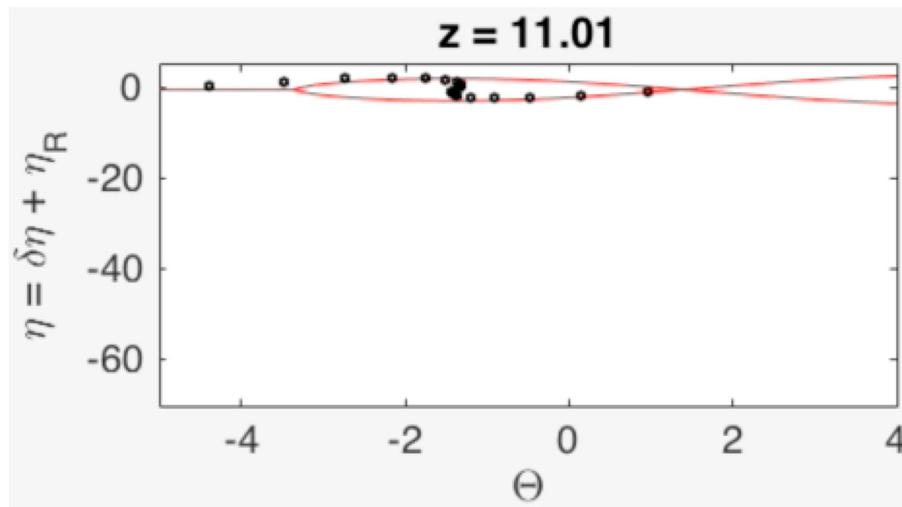
- To better capture the phase space bucket characteristics $(\theta, \eta) \leftrightarrow (\varphi, J)$

$$\mathcal{H}(\theta, \eta; \hat{z}) = \frac{(\eta - \eta_R)^2}{2f_R} - i \frac{f_B}{f_R} (\mathcal{E} e^{i\theta} - \mathcal{E}^* e^{-i\theta}) = \frac{(\delta\eta)^2}{2f_R} + 2 \frac{f_B(\hat{z})}{f_R(\hat{z})} |\mathcal{E}| [\sin \Theta_R + \sin \Theta - (\Theta + \Theta_R) \cos \Theta_R]$$



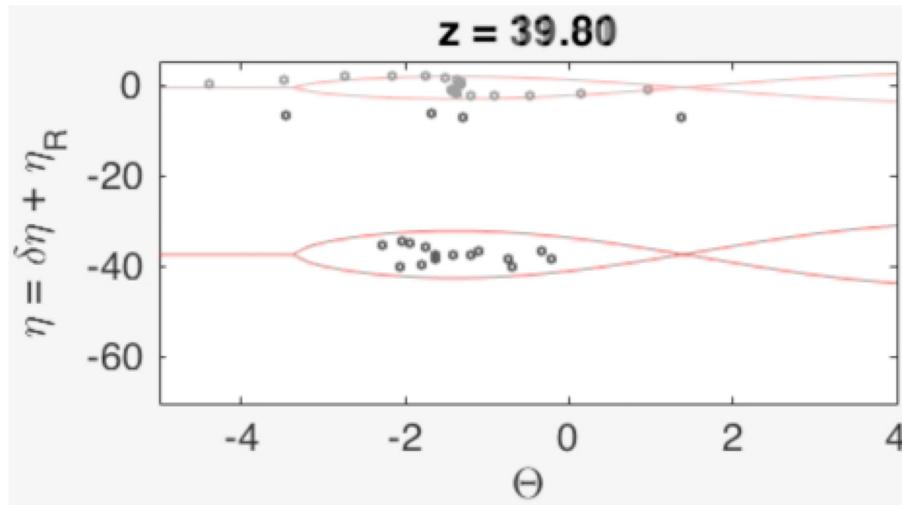
Energy extraction in post-saturation tapered FEL

- Involves two main physical mechanisms:
 - 1) **bucket deceleration**: phase space bucket moving *downward* to give energy to the radiation field
 - 2) **particle detrapping**: some particles executing large amplitude will detrap



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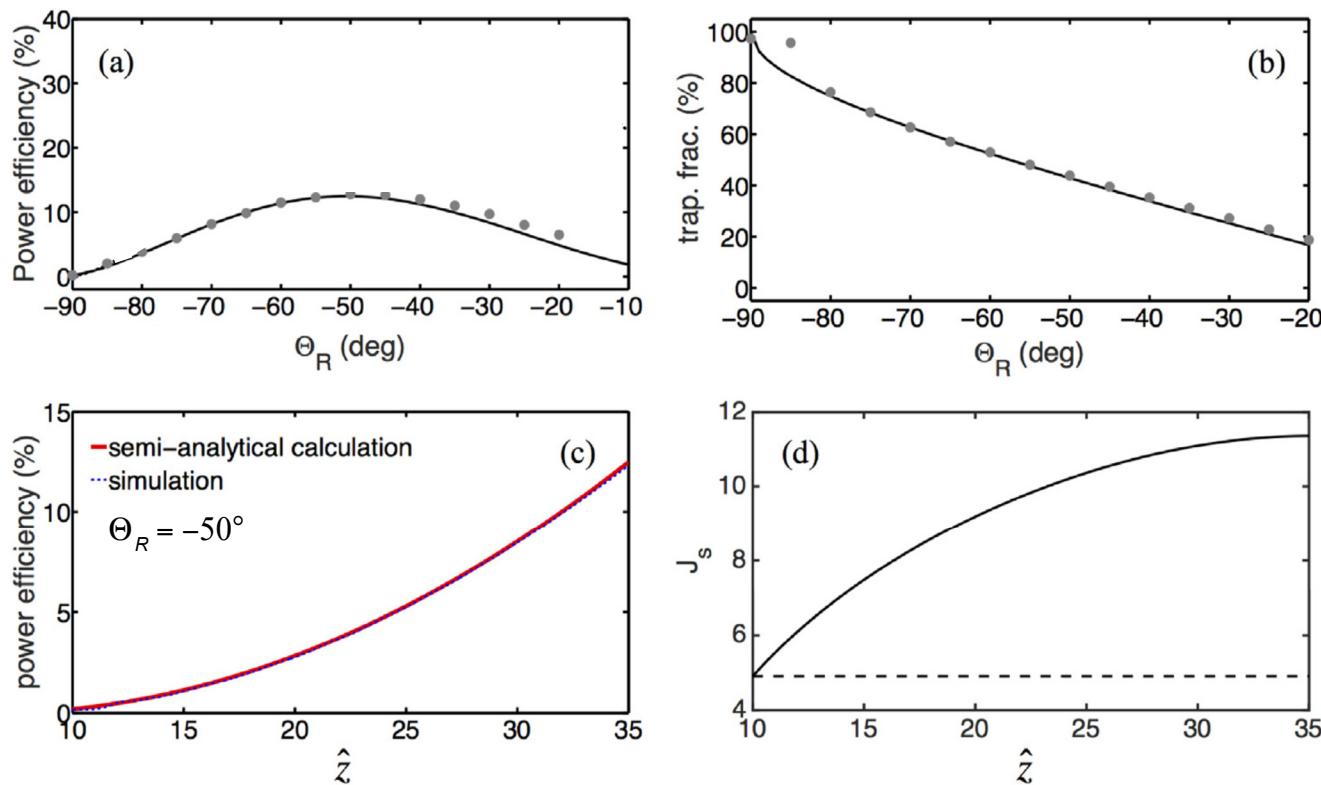


Energy extraction in post-saturation tapered FEL

- Involves two main physical mechanisms:
 - 1) **bucket deceleration**: phase space bucket moving *downward* to give energy to the radiation field
 - 2) **particle detrapping**: some particles executing large amplitude will detrap
- The desire of undulator tapering for efficiency enhancement is to **precipitate** the bucket deceleration process, and, in the meanwhile, to **keep as many as possible** the electrons in the phase space bucket

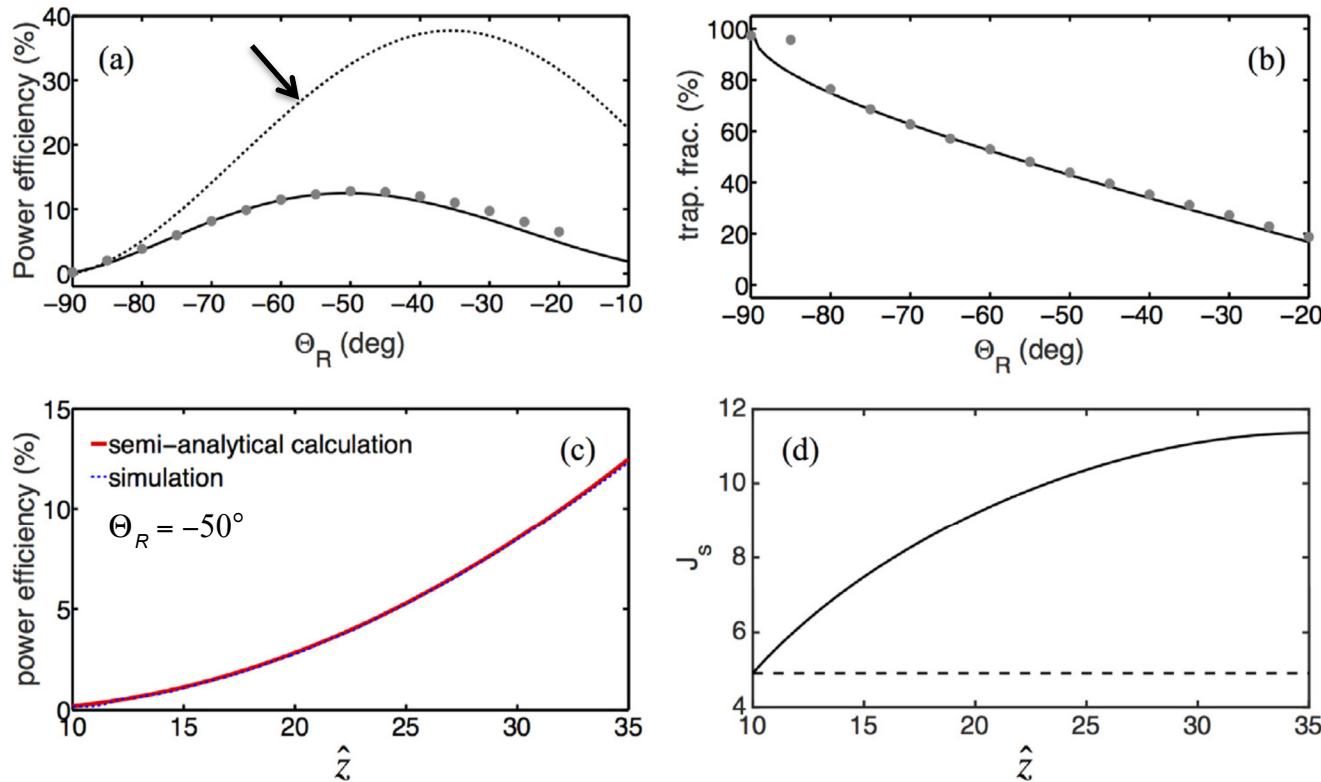
Constant- Θ_R taper scheme

- Kroll, Morton, and Rosenbluth, IEEE QE **17**, 1436-1468 (1981)
- Undulator taper profile follows constant- Θ_R along z
- The optimum efficiency can be close to 14% at $\Theta_R = -50^\circ$ (coasting beam)



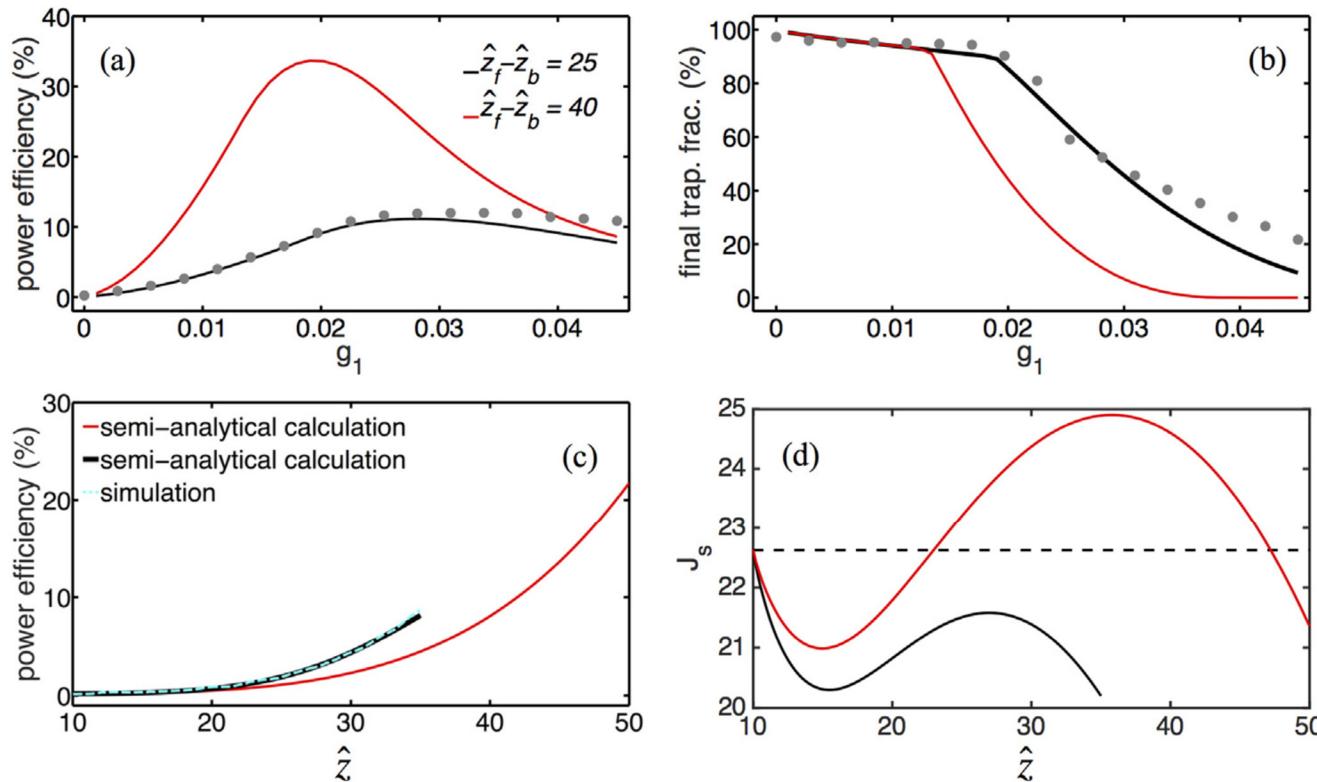
Constant- Θ_R taper with prebunched beam

- C. Emma *et al.*, PRAB **20**, 110701 (2017)
- Undulator taper profile follows constant- Θ_R along z , and the beam at the initial saturation is prebunched
- The optimum efficiency can be close to 40% at $\Theta_R = -35^\circ$



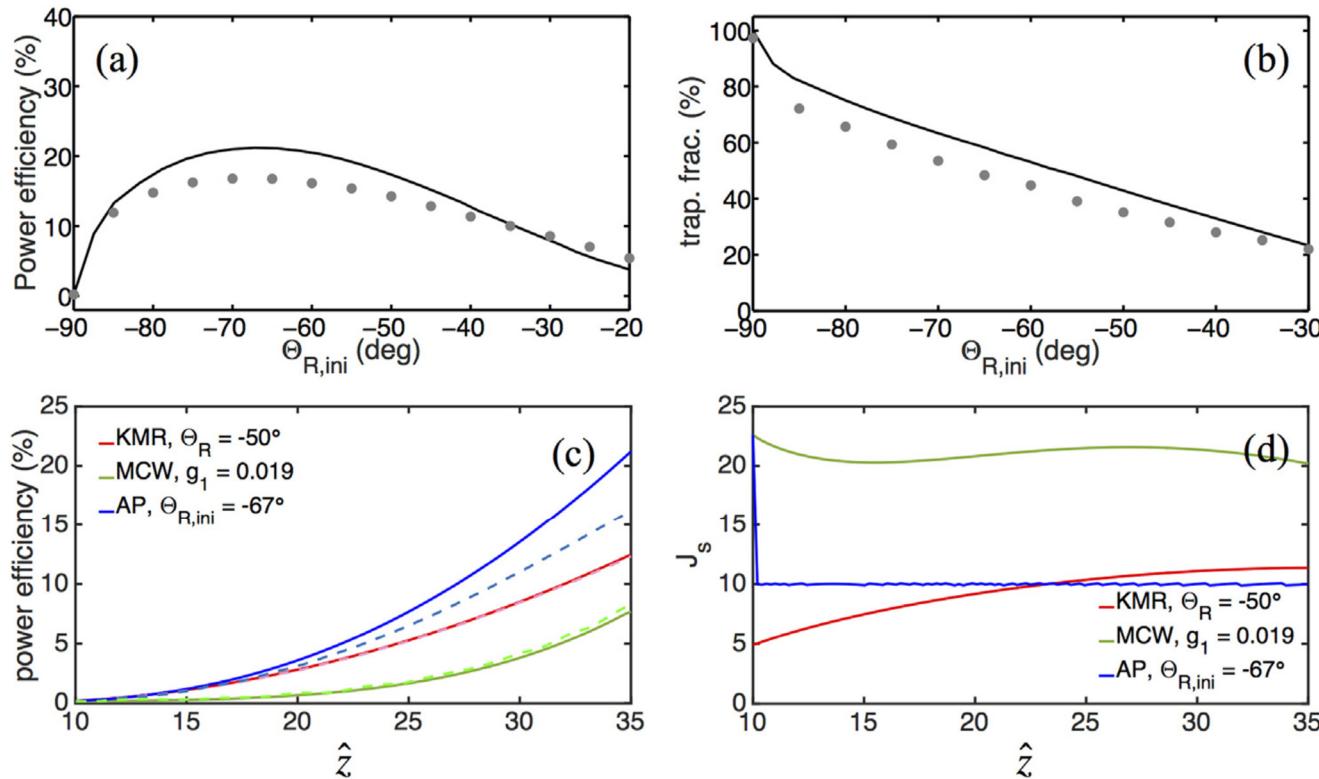
Linear- Θ_R taper scheme

- Mak, Curbis, and Werin, PRAB **18**, 040702 (2015) $\Theta_R(\hat{z}) = g_1(\hat{z} - \hat{z}_b) - \pi/2$
- Linear- Θ_R scheme takes care of initial particle detrapping, but the (unnecessary) bucket area remains increasing in the deep saturation regime
- The optimum efficiency ranges from 10% and 35%, depending on the undulator length



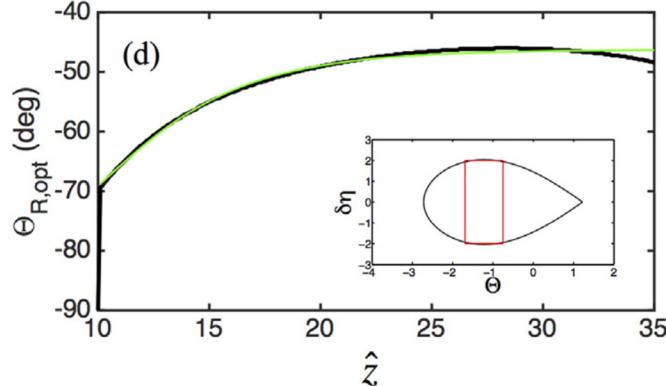
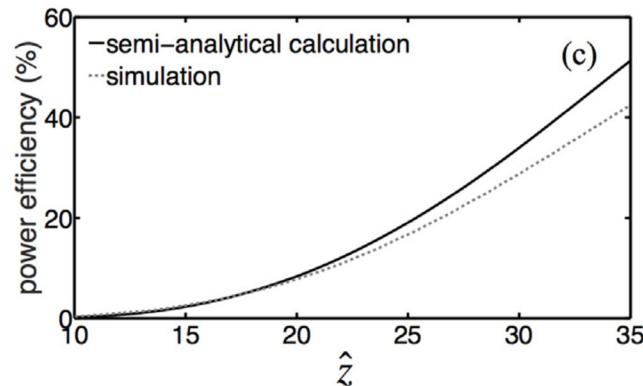
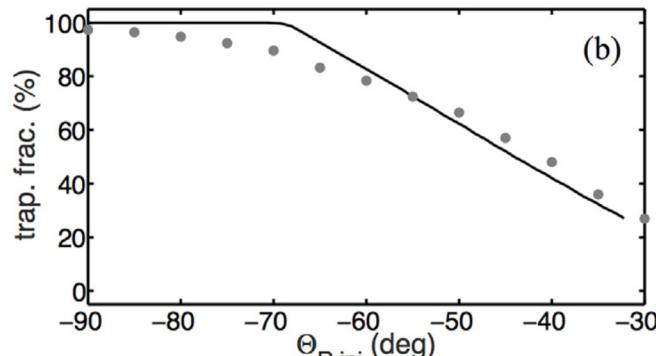
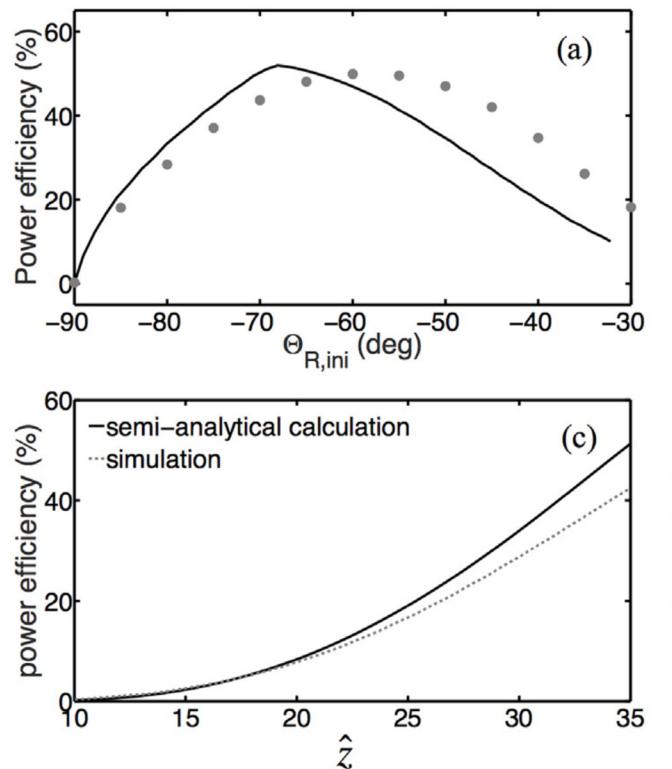
Area-preserving taper scheme

- Bucket deceleration and particle detrapping are both taken care
- The phase space area remains constant, as a result of balance between the growing radiation field and the effect of increasing Θ_R
- The optimum efficiency can be close to 20% (coasting beam)



Area-preserving taper scheme

- Bucket deceleration and particle detrapping are both taken care
- The phase space area remains constant, as a result of balance between the growing radiation field and the effect of increasing Θ_R
- The optimum efficiency can be close to 50% (prebunched beam)

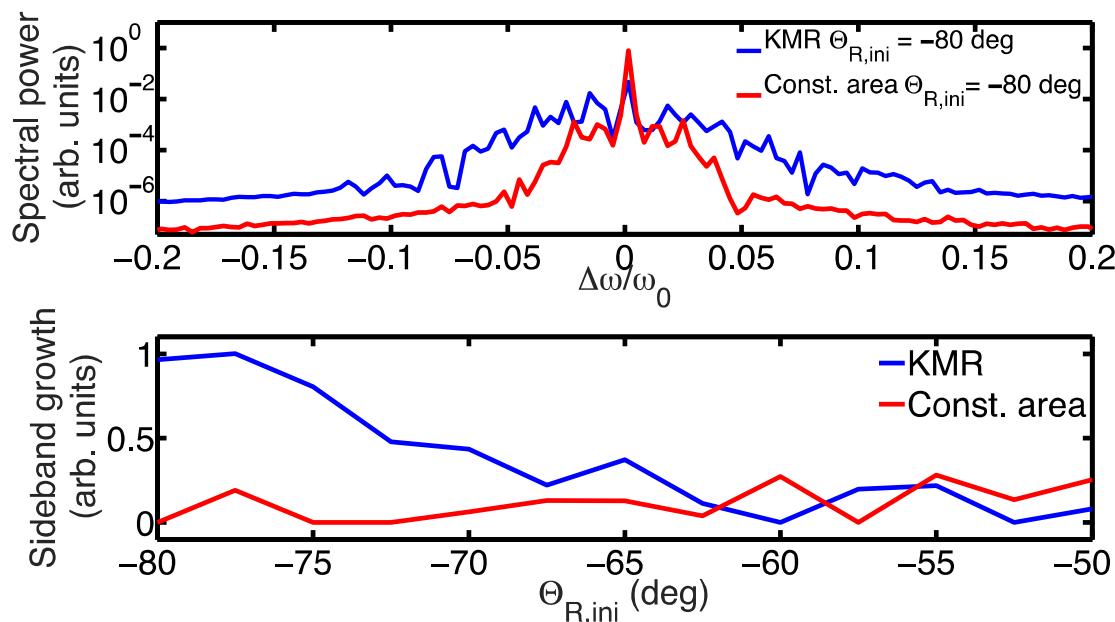


semi-analytical
expression of
taper profile

Numerical simulation

- Use perave [C. Emma, https://github.com/cemma1/FEL_code_PBPL]

Name	Value	Unit
Electron beam energy	4.5	GeV
RMS relative energy spread	3.3×10^{-4}	
Peak current	4	kA
Undulator period	2	cm
Undulator parameter (rms)	3	
Resonant wavelength	12.4/1	Å/keV
Pierce FEL parameter	2×10^{-3}	

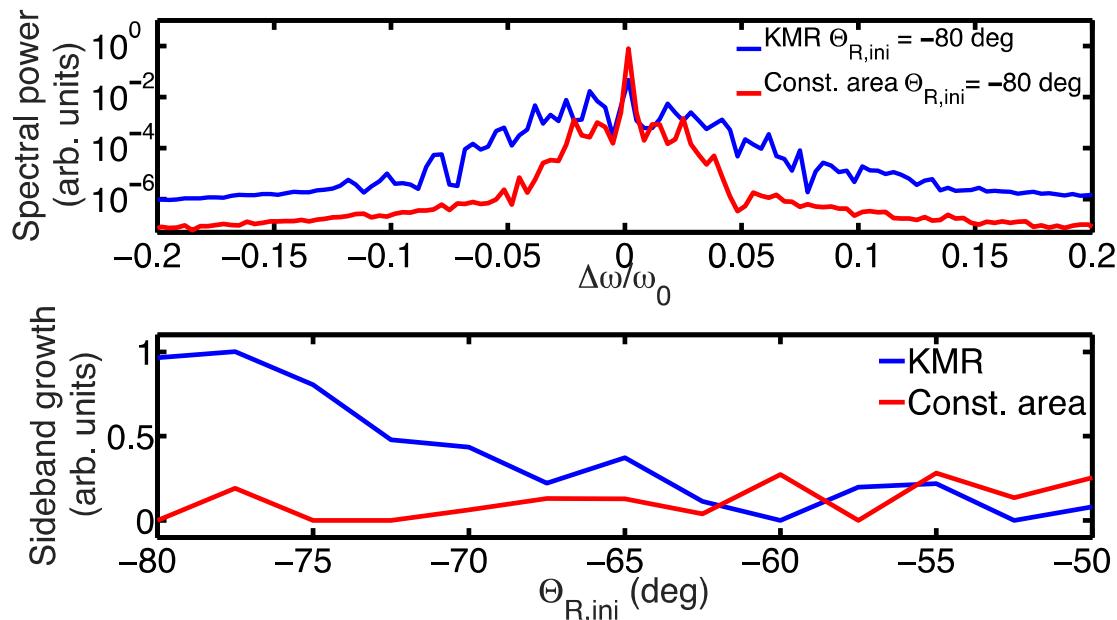


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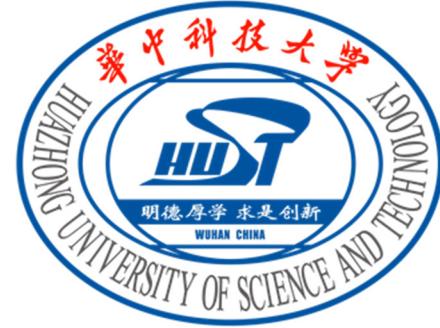
Effective suppression of FEL sideband instability over wide range of Θ_R !



Part III: Summary and Discussion

- By including two trade-off mechanisms in post-saturation tapered FEL (**bucket deceleration** and **particle detrapping**), in the semi-analytical analysis, the area-preserving taper scheme takes **both** effects into consideration for evaluation of FEL output power performance
- 1-D time-dependent simulations indicate that such a taper scheme can also **effectively suppress FEL sideband instability**
- Other remaining issues for the theoretical model
 - include transverse diffraction (and finite-emittance electron beam) into the analysis, which will lead to additional particle detrapping
 - analyze the sideband instability in such a Θ_R -varying case
- *Work in progress:* combined analyses of the aforementioned three issues

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 - **Guanqun Zhou** (IHEP), **Xiaofan Wang** (SINAP), **Chuan Yang** (ShanghaiTech)
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References

- In this presentation I must have missed the references. We refer the interested reader to the papers below (and references therein)

Part I

- Cheng-Ying Tsai, Juhao Wu, Chuan Yang, Moohyun Yoon, and Guanqun Zhou, Sideband instability analysis based on a one-dimensional high-gain free-electron laser model, PRAB **20**, 120702 (2017)

Part II

- Cheng-Ying Tsai, Juhao Wu, Chuan Yang, Moohyun Yoon, and Guanqun Zhou, Single-pass high-gain tapered free-electron laser with transverse diffraction in the postsaturation regime, PRAB **21**, 060702 (2018)

Part III

- Cheng-Ying Tsai, Claudio Emma, Juhao Wu, Moohyun Yoon, Xiaofan Wang, Chuan Yang, and Guanqun Zhou, Area-preserving scheme for efficiency enhancement in single-pass tapered free electron lasers, NIMA **913**, 107-119 (2019)

Thank you for your attention

