

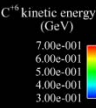
“Towards GeV laser-driven ion acceleration”

Björn Manuel Hegelich

**Los Alamos National Laboratory & Ludwig Maximilian
Universität München**

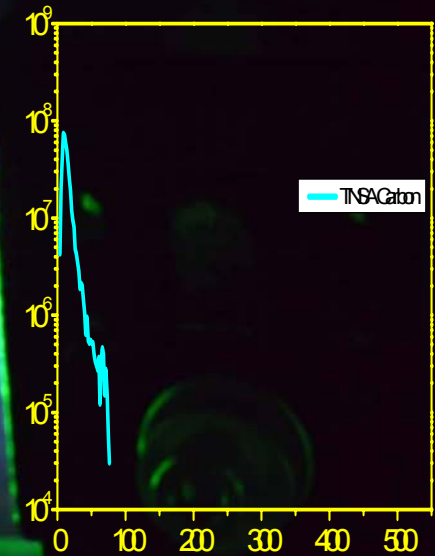
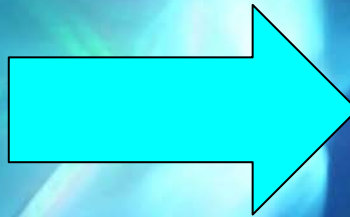
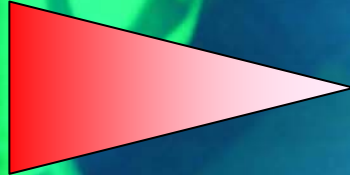
**International Conference on Heavy Ion Accelerator
Technology, Venice, Italy, June 8-12, 2009**

hegelich@lanl.gov



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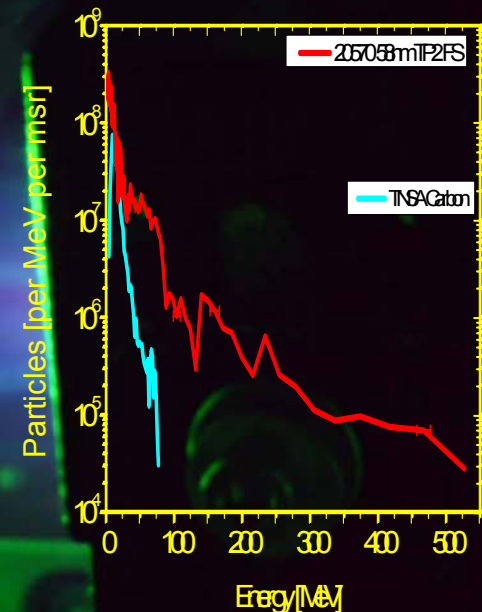
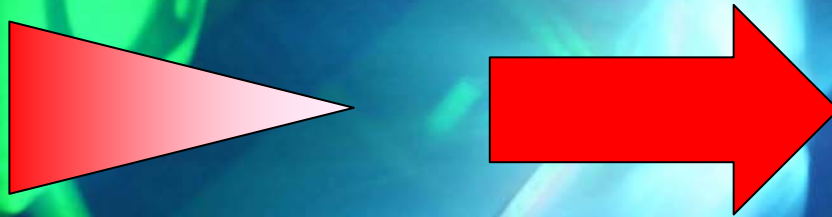
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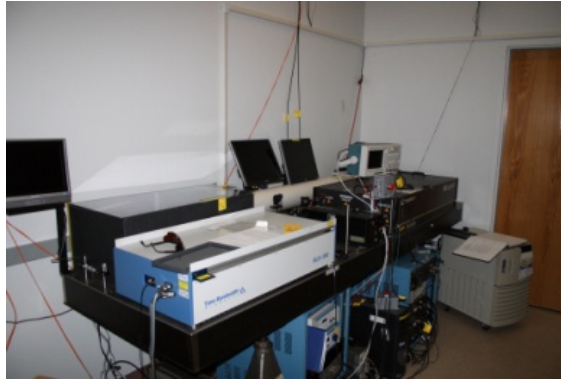


Outline:

- Laser-driven ion acceleration: Motivation & Current status
- Paradigm shift:
ultrahigh contrast enables use of ultrathin targets
⇒ ultrathin targets enable new acceleration mechanisms
- A new acceleration mechanisms: Break-Out Afterburner Acceleration (BOA)
 - Theoretical Concept, Simulations
 - First experimental demonstration of BOA:
 - >0.5 GeV carbon at ~100J Trident laser, Los Alamos
 - >70 MeV carbon at 0.7J Ti:Saph laser at MBI, Berlin
 - Reduced Analytical Model
- Summary

The Los Alamos Trident Laser Facility

200 TW, 100J, 500fs, 1 shot/h shortpulse + 2x 500J, 1ns longpulse beams



3 beamlines, 3 target areas:

A + B: 100ps – 6 μ s, 80-1000J (532nm)

- Full temporal pulse shaping

- C-Beam: 500fs, 125J, 250 TW (1054nm)

Intensity: 5×10^{20} W/cm²

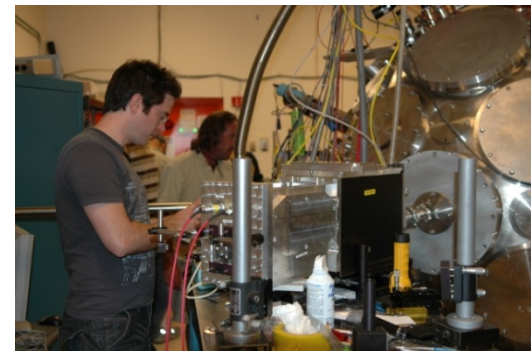
- Rep. rate: 1 shot / 45 min.

- AODF (spectral control), adaptive optics

- Complete suite of laser diagnostics on each shot (Energy, pulse length, pre-pulse, spectrum, far field, near field)

- Contrast: Old frontend: $\sim 10^{-7}$

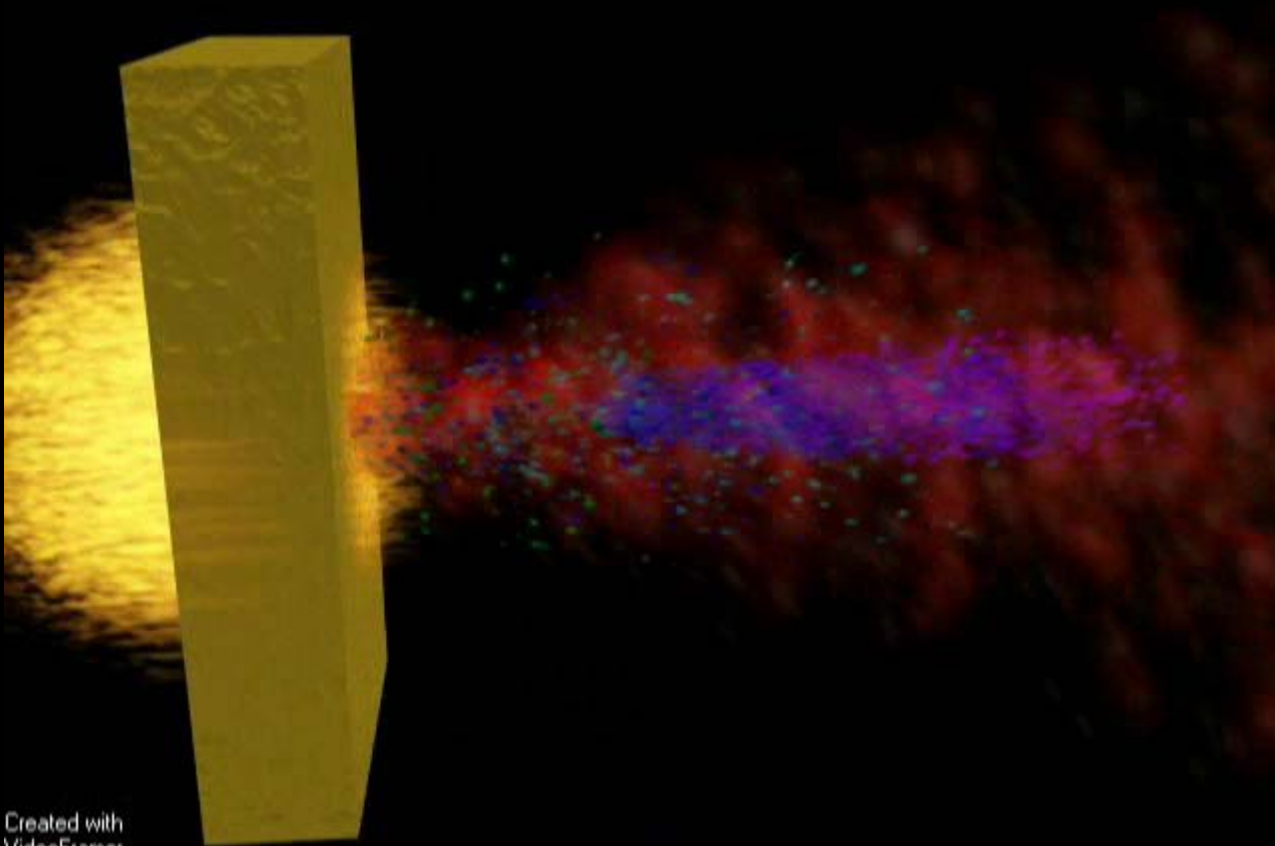
New frontend: $< 5 \times 10^{-10}$ (prepulse)
 $< 2 \times 10^{-12}$ (pedestal)



Current status of laser-ion acceleration

A laser pulse accelerates e^- through the target. The e^- set up a TV/m E-field at the rear surface, ionizing and accelerating atoms to MeV/u :

Target Normal Sheath Acceleration (TNSA):



Legend:

Created with
VideoFramer
shareware version

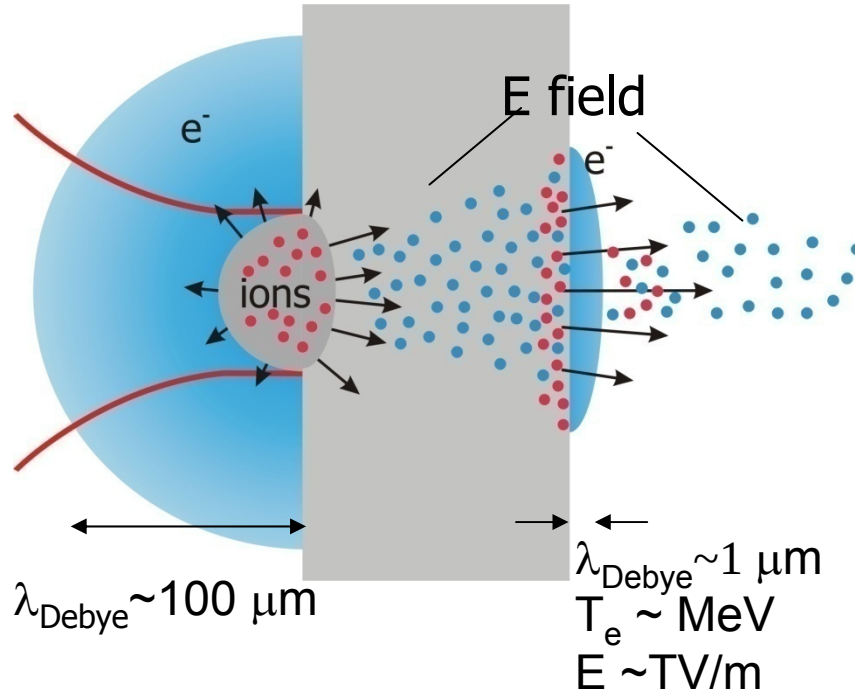
e^- , C1+, C2+, C3+, C4+

Target Normal Sheath Acceleration (TNSA):

Accelerates ions from the rear surface of $\sim\mu\text{m}$ foils in laser directions

The TNSA mechanism:

laser electron acceleration $\rightarrow$ charge separation $\rightarrow$ quasi static electric field $\rightarrow$ ion acceleration



Advantages of laser-driven ion beams:

- Shorter pulse duration ¹
 $< \text{ps}$ vs. $> \text{ns}$
- Smaller longitudinal emittance ¹
 10^{-6} eVs vs. 1 eVs (CERN SPS)
- Smaller transverse emittance ²
 $< 0.001 \pi \text{ mm-mrad}$ vs. $1 \pi \text{ mm-mrad}$ (CERN SPS)
- High beam currents ¹
 $\text{kA} - \text{MA}$ vs. $\mu\text{A} - \text{mA}$

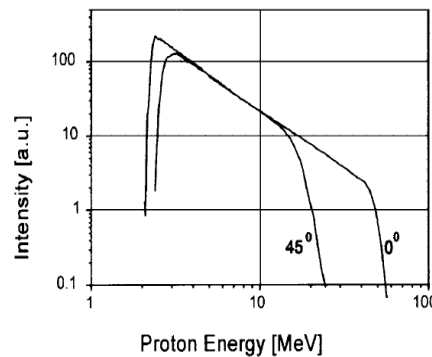
¹ Hegelich et al., Nature **439** (2006) p441

² Cowan et al., PRL **92** (2004) 204801

TNSA ion acceleration:

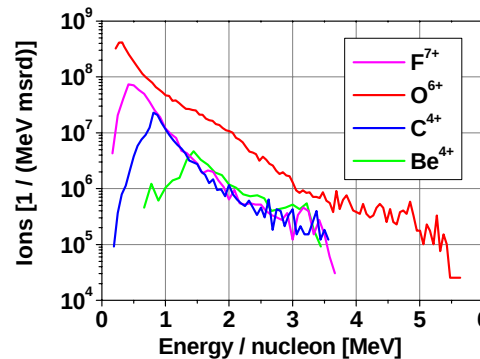
No significant increase in particle energies since first demonstrations.

Protons with $E \leq 60$ MeV.

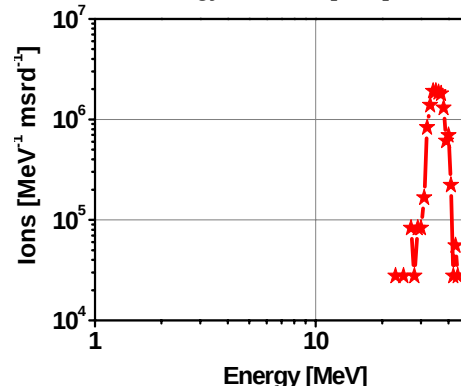


Snavely et al. PRL 2000

Light ions ($Z \leq 10$) with $E \leq 5$ MeV/amu.



Mid-Z ions ($10 \leq Z \leq 46$) with $E \geq 2$ MeV/amu.



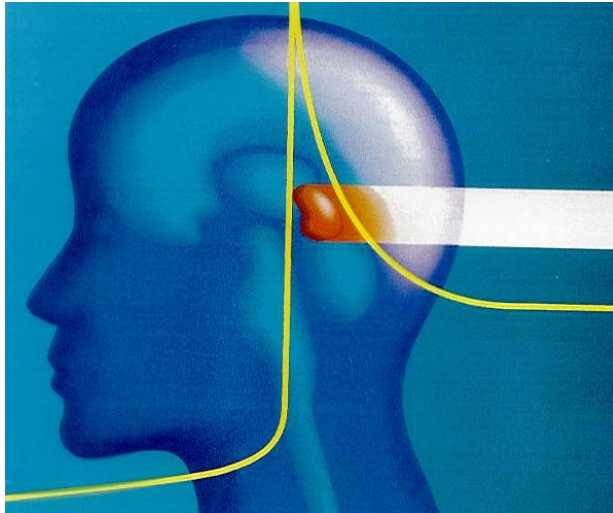
Mono-energetic ions (carbon)
3 MeV/amu



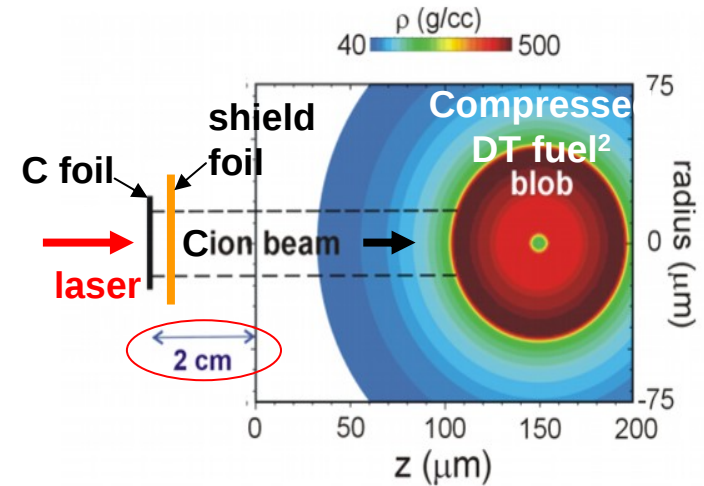
Potential Applications of Laser-driven Ions:

Hadron Therapy and Ion-driven Fast Ignition require GeV-class particle energies

Hadron therapy



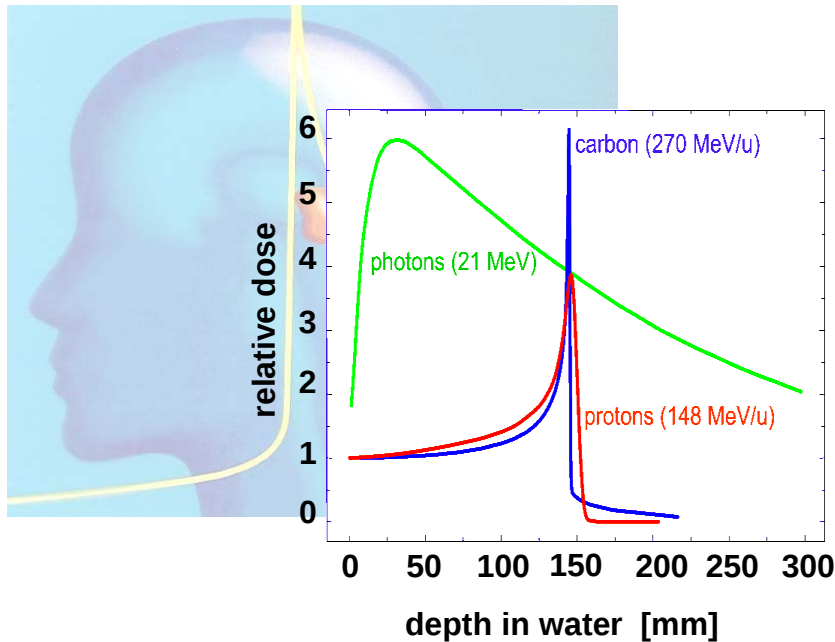
Ion-driven Fast Ignition (IFI)



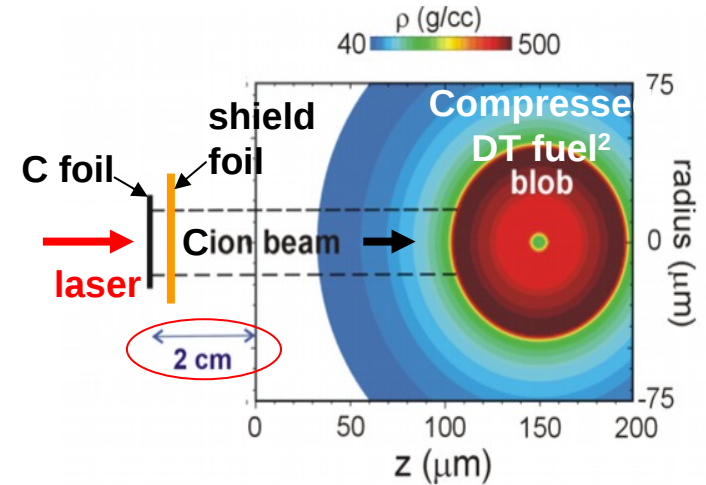
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Hadron therapy



Ion-driven Fast Ignition (IFI)

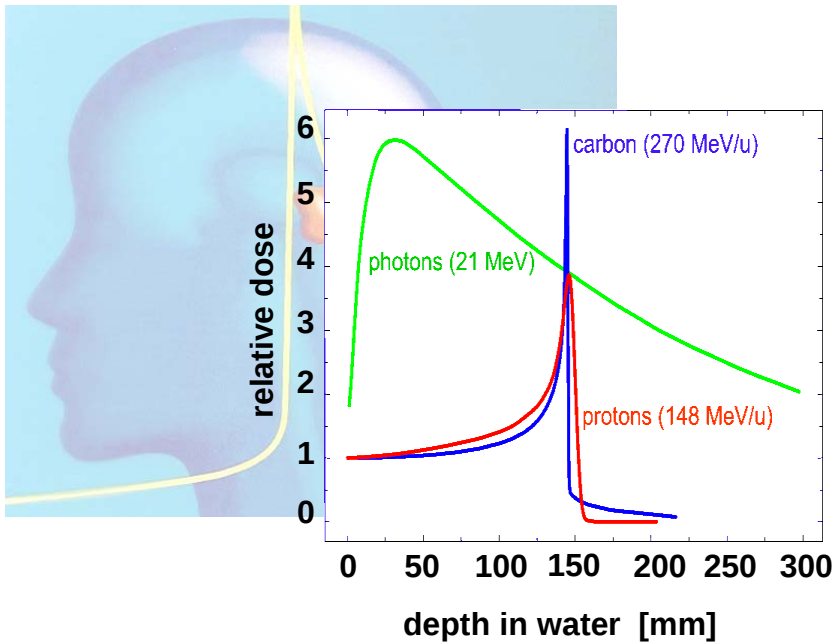


- Hadron therapy
- requires:
 - 150 – 250 MeV protons
 - 2-4 GeV carbon ions

Potential Applications of Laser-driven Ions:

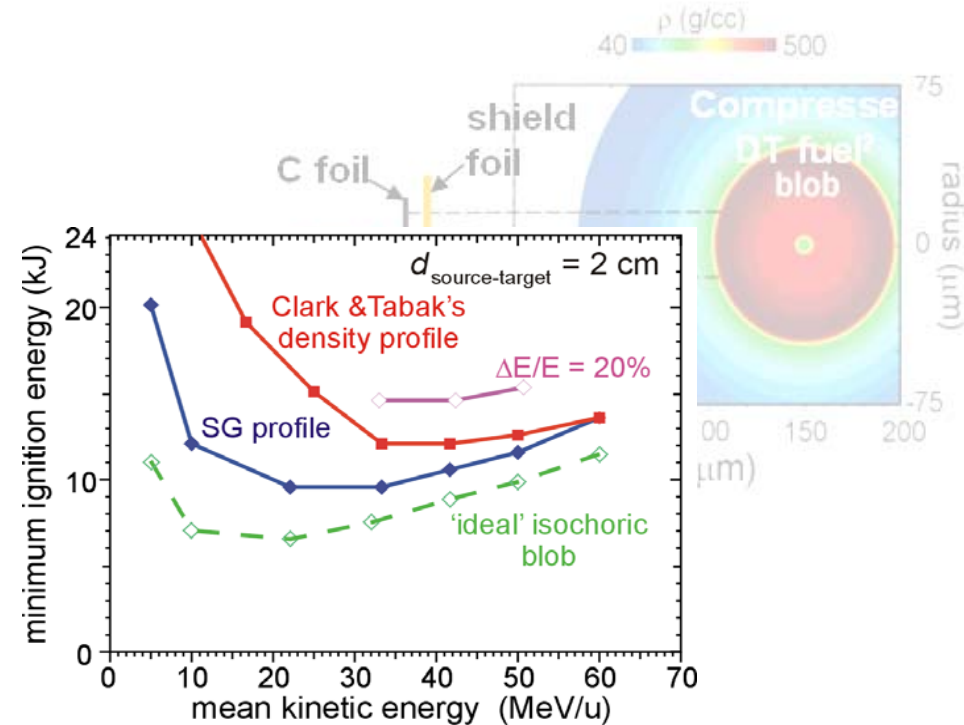
Hadron Therapy and Ion-driven Fast Ignition require GeV-class particle energies

Hadron therapy



- Hadron therapy
- requires:
- 150 – 250 MeV protons
- 2-4 GeV carbon ions

Ion-driven Fast Ignition (IFI)



Beam Ion	Energy (MeV)	Number of Ions	Laser Irrad. (W/cm ²)
Protons	7 – 19	10^{16}	$\sim 10^{20}$
C^{6+}	400-480	10^{14}	$\sim 10^{21}$

Potential Applications of Laser-driven Ions:

Advanced Accelerators: Injecting into SIS-18?



To inject into SIS-18 or similar:*

* I. Hofmann, priv. comm.

- 10^{12} ions / sec
- 30-70 MeV/amu
- $\Delta E \sim 1-2\%$

Not promising with Phelix type system at 1 shot per hour

BUT

@ 100Hz: 10^{10} ions per shot

@ 50MeV: 80mJ per bunch

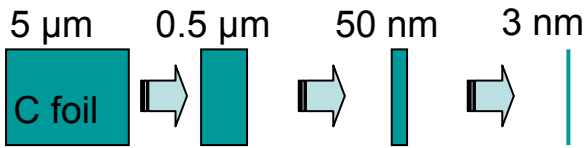
@ 1% CE: 8J laser

FEASIBLE



Nanoscale targets

Enable GeV ion energies at achievable laser intensities of $I \sim 10^{21} \text{ W/cm}^2$

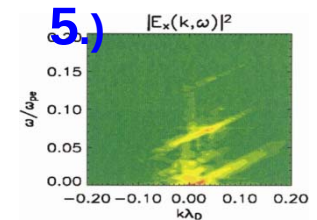
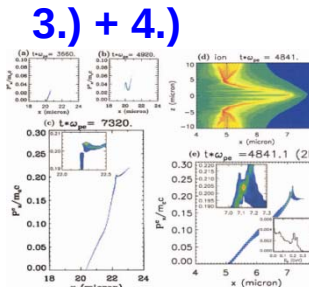
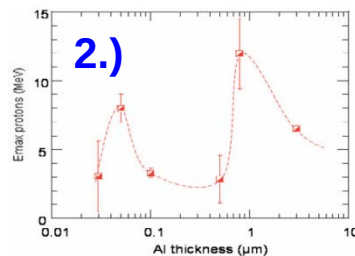
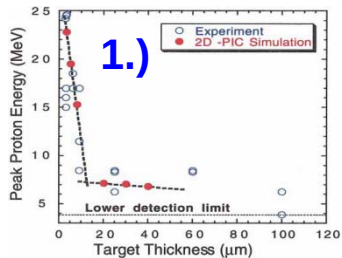


Enhanced TNSA: Thinner targets enable higher ion energies:

1. LLNL: Enhancement of Proton Acceleration by Hot-Electron Recirculation in Thin Foils Irradiated by Ultraintense Laser Pulses. A. MacKinnon, et al., **PRL 88**, (2002)
2. LULI: Ion acceleration using high-contrast ultra-intense lasers, J. Fuchs et al., **J. Phys. IV France 133** (2006) 1151–1153

Break-Out Afterburner (BOA): Matching of laser and target parameters enables additional energy transfer via relativistic Buneman instability:

3. LANL: GeV laser ion acceleration from ultrathin targets: The laser break-out afterburner, L. Yin, et al., **Laser and Particle Beams 24** (2006), 1–8
4. LANL: Monoenergetic and GeV ion acceleration from the laser break-out afterburner using ultrathin targets, L. Yin, et al., **PoP 14**, 056706, (2007).
5. LANL: Relativistic Buneman instability in the laser breakout afterburner, B. J. Albright, et al., **PoP 14**, 094502, (2007)

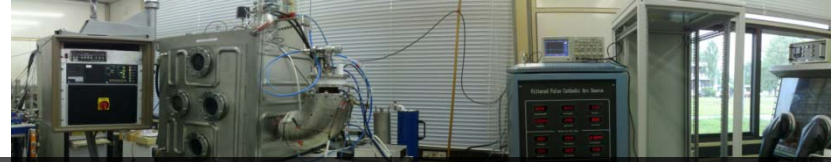


Experimental Realization

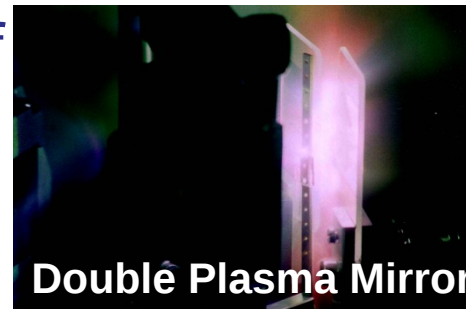
Ultrathin, nm-scale, robust, free standing targets & ultrahigh contrast

The experimental use of ultrathin targets required two major developments:

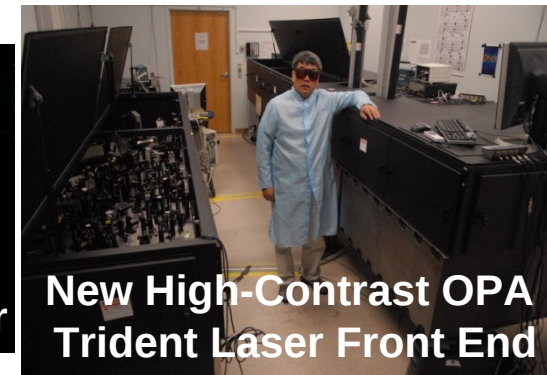
- Robust, free standing (mm), ultrathin (nm) targets
- Improvement of laser contrast by 4 - 6 orders of magnitude from 10^{-6} to $\sim 10^{-11}$



	LMU
Thickness	3 to 60 nm
Bulk density	$2.7 \pm 0.3 \text{ g/cm}^3$
sp^3 content	>75%
Roughness	$\sim 2 \text{ nm}$
Damage Threshold	$10^{11} \text{ W/cm}^2 @ 500 \text{ fs}$ $10^8 \text{ W/cm}^2 @ 1.2 \text{ ns}$
Atomic composition	<10% protons (bulk), proton layer on top



Double Plasma Mirror



New High-Contrast OPA
Trident Laser Front End

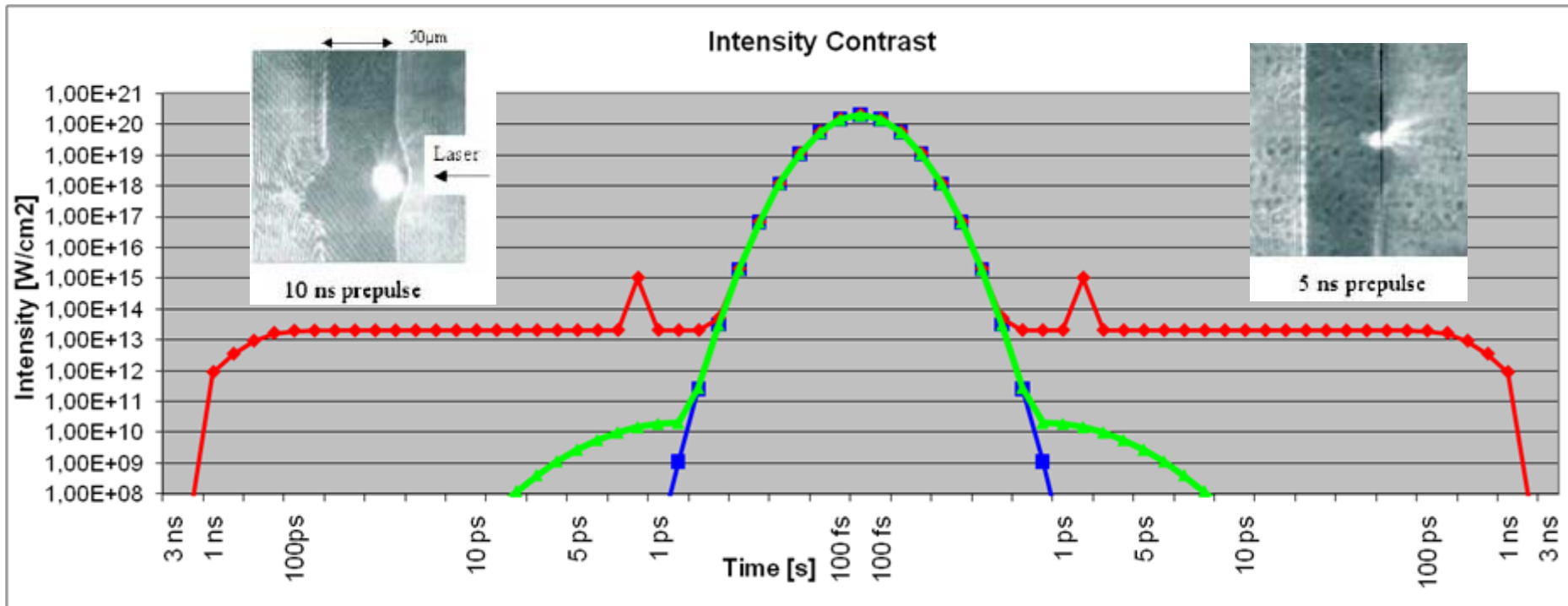
High-contrast ($<10^{-10}$ @ 5ps) is needed to shoot $\sim 40\text{nm}$ targets without shot breakout before the main pulse:

Starting point:

- Current contrast: $<10^{-7}$ @ 1ns
- $V_s \sim 7 \text{ nm/ps} \Rightarrow 40\text{nm}/5.7\text{ps}$

Goals:

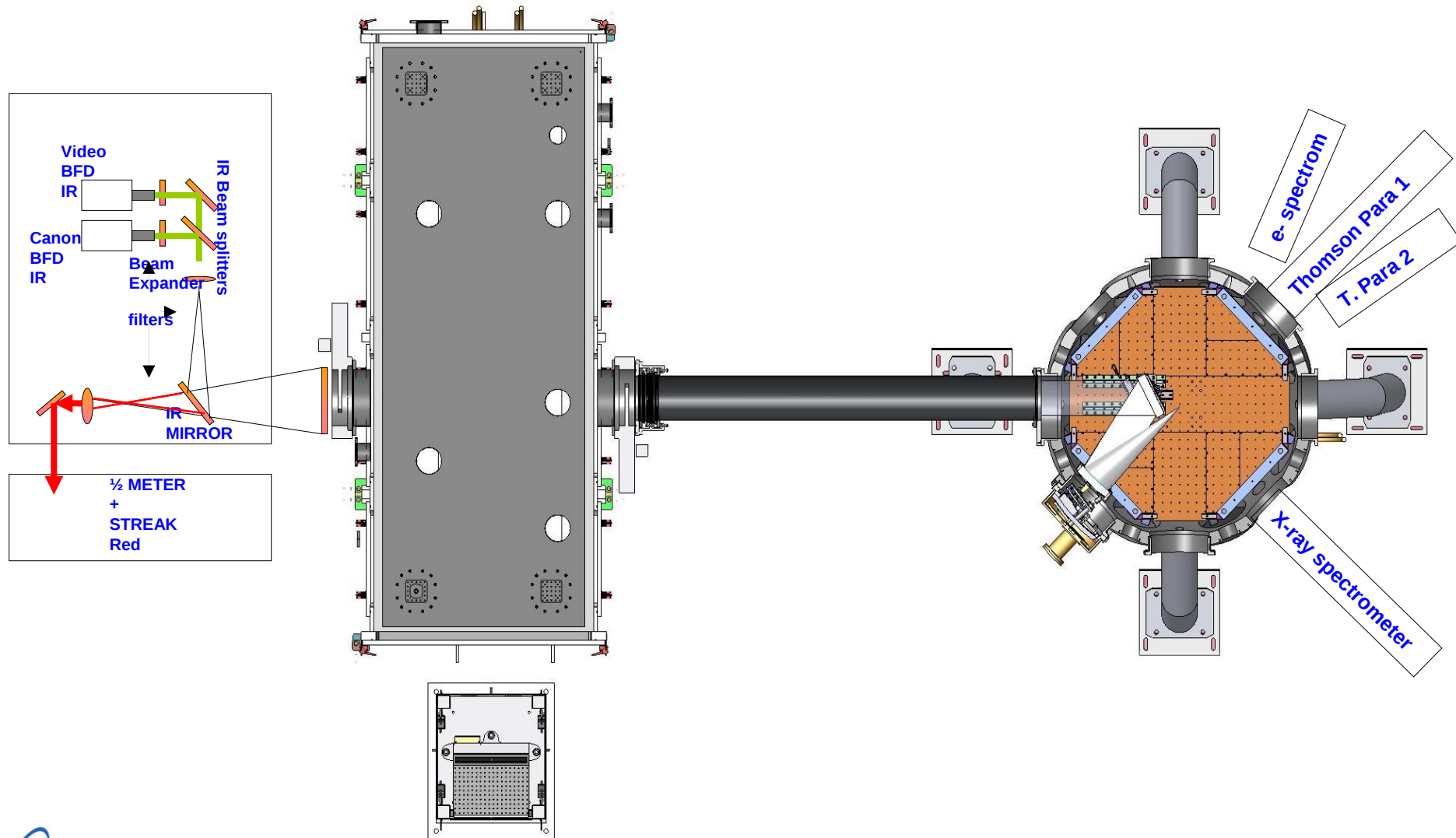
Intensity contrast of $<10^{-10}$ @ 5ps on target



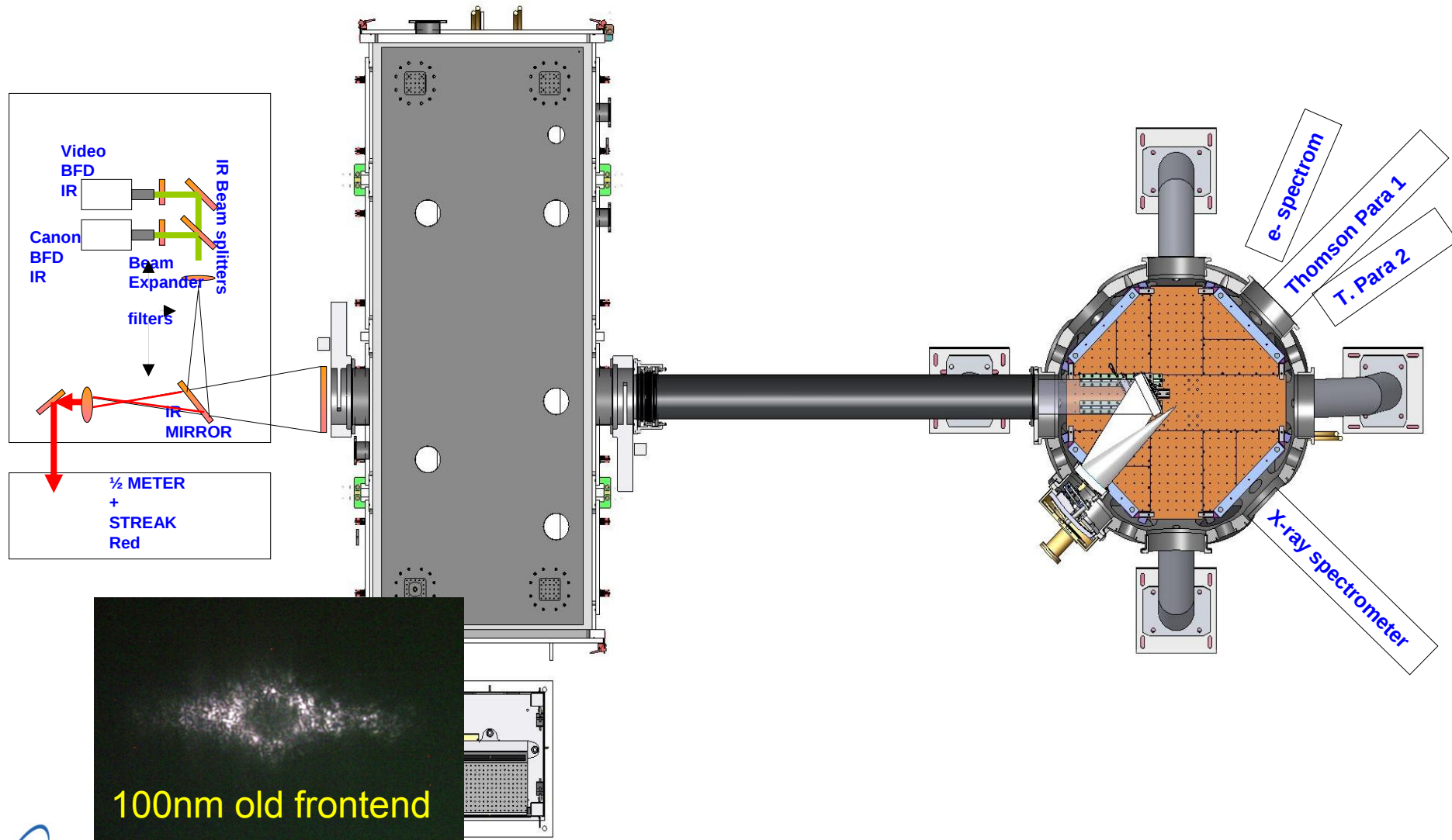
Energetic ions generated by laser pulses: A detailed study on target properties; M. Roth, M. Hegelich, et al.
PRST – AB, Vol. 5, 061301, 2002

High-temporal contrast using low-gain optical parametric amplification; R. Shah, M. Hegelich, et al.
Accepted for publication, Opt. Lett. 2009

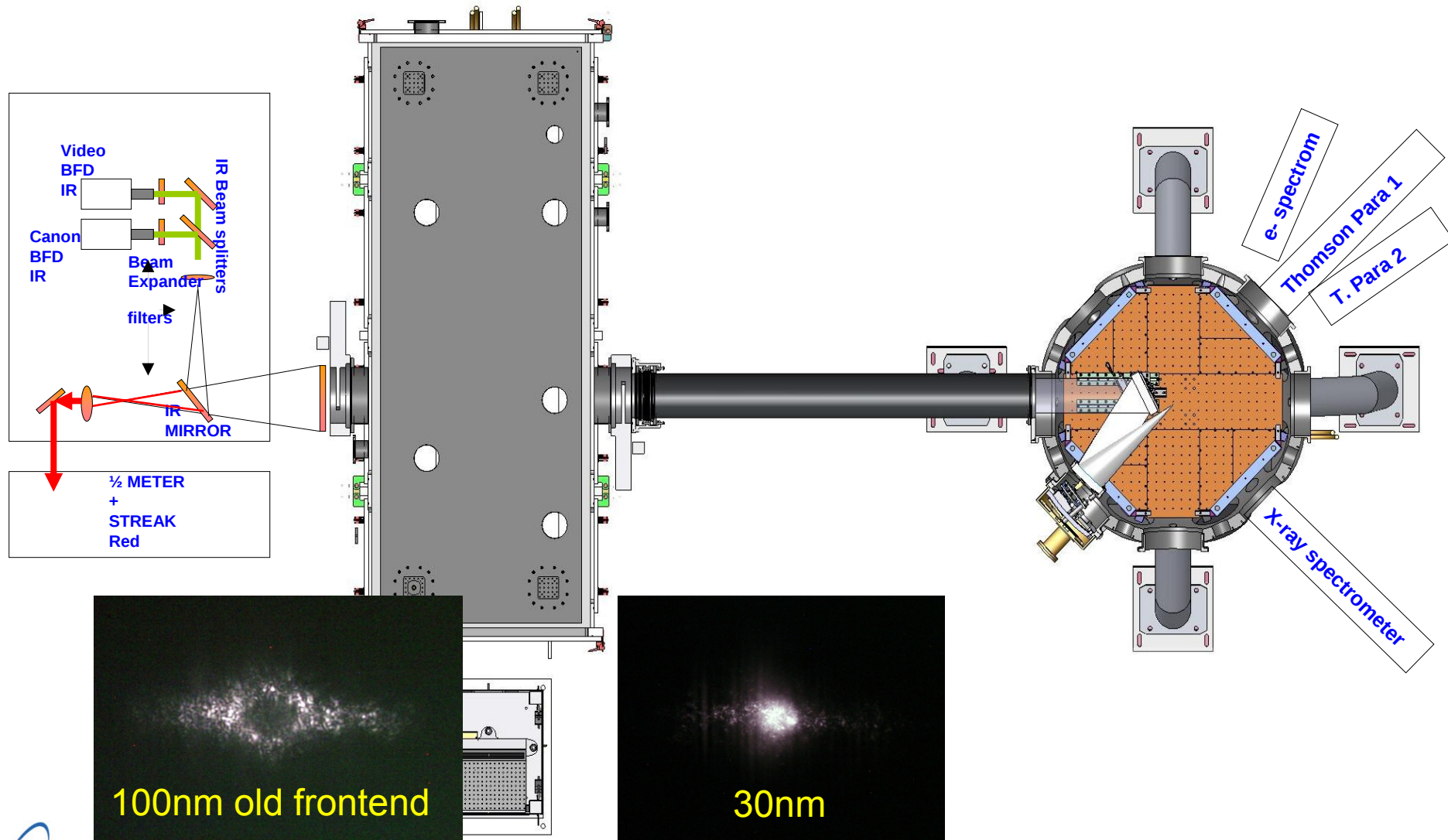
Experimental Setup: F/3 OAP, 2 Thomson parabola ion spectr., e-spectr., Full-Aperture Backscatter (FABS), x-ray spectrom.



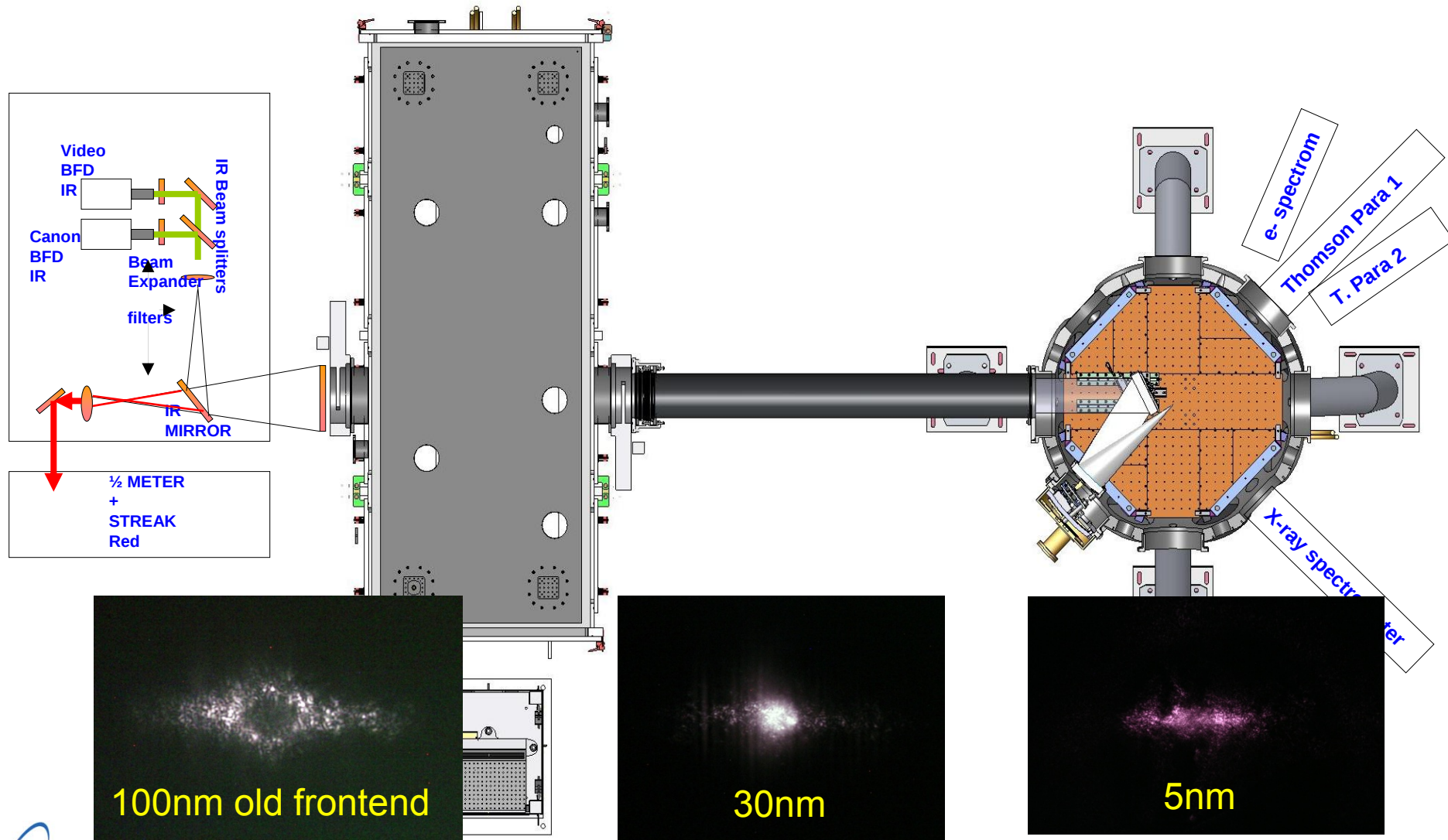
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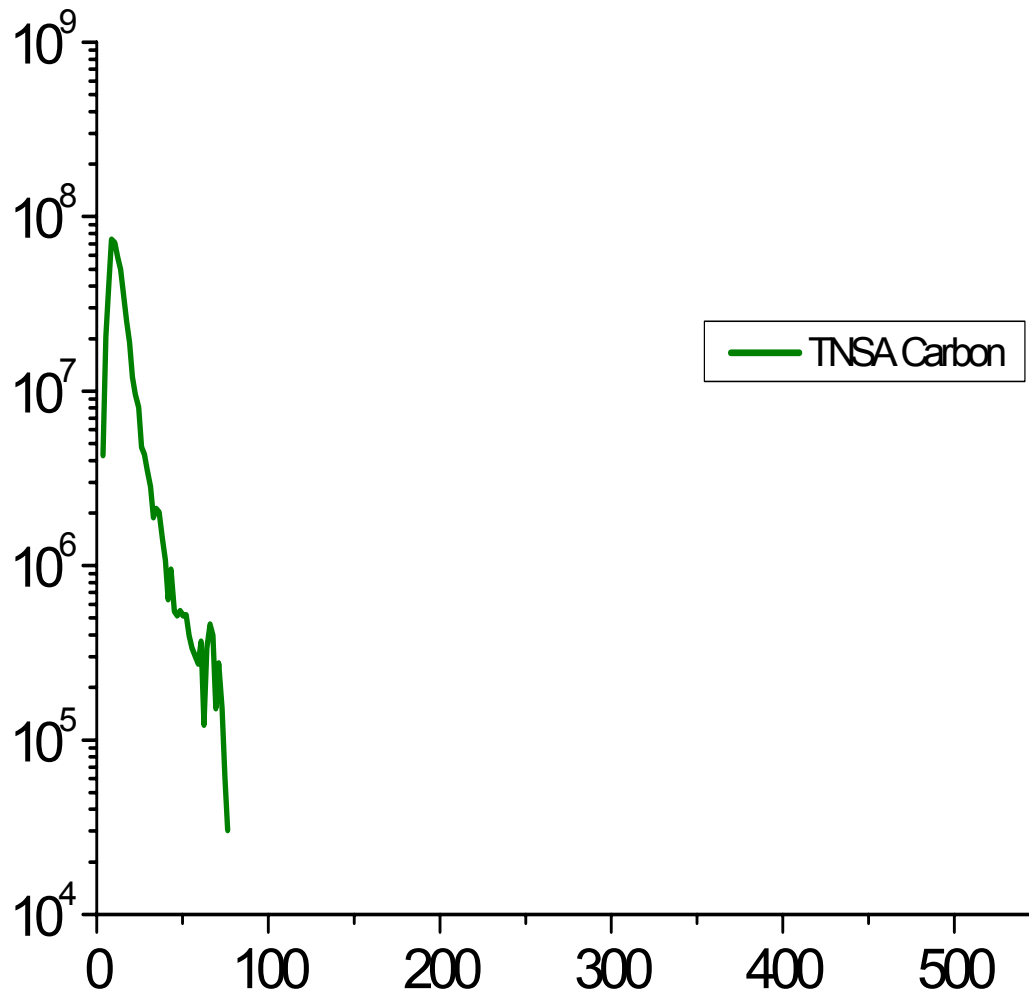


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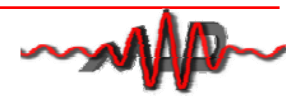


1st Demonstration of Break-Out Afterburner:

Shot #20570, 58nm DLC foil, $E_{\text{target}} = 90.1\text{J}$, $t=540\text{fs}$, $I = 2 \times 10^{20} \text{ W/cm}^2$

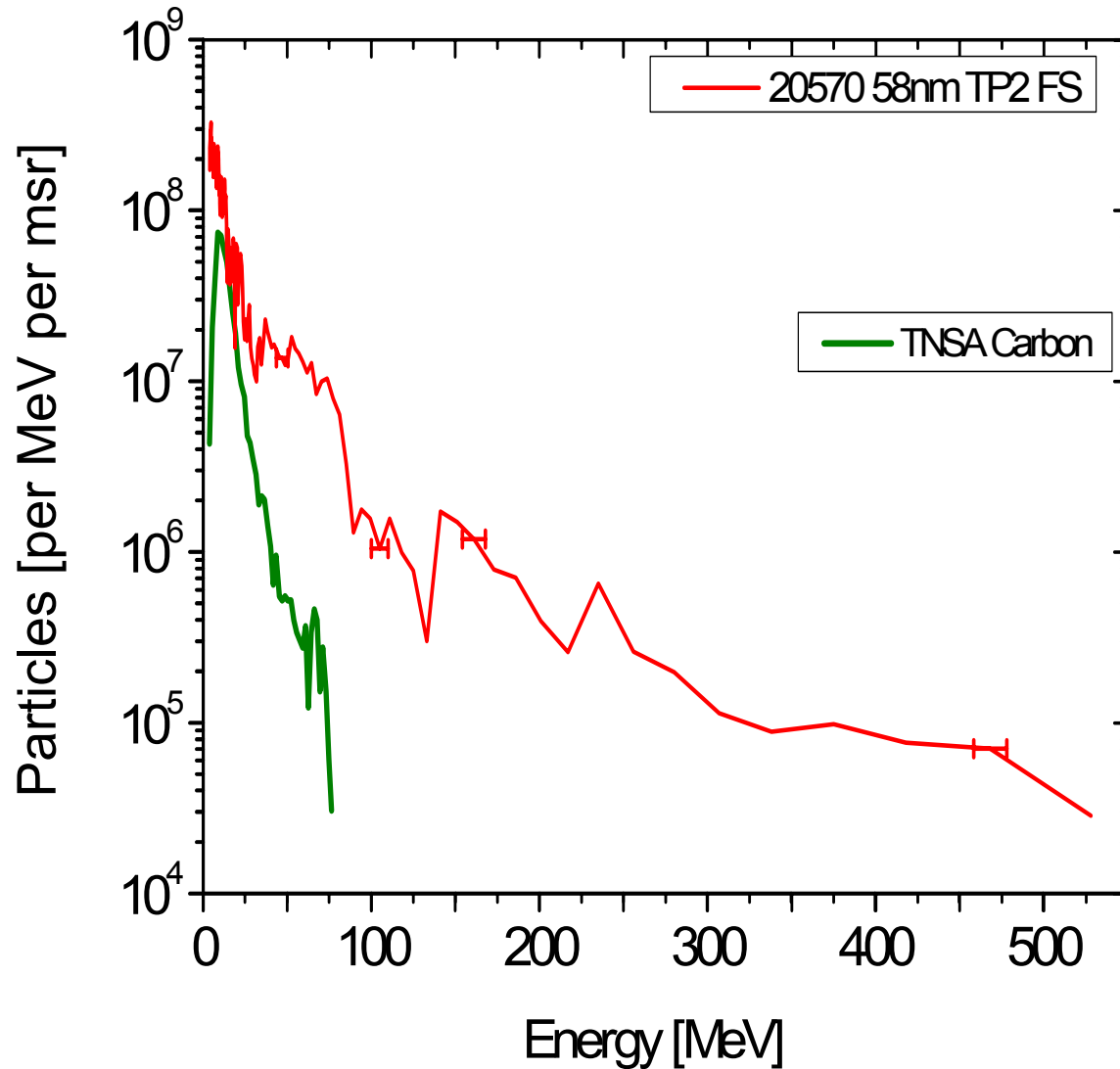


- Compared to 75 MeV from TNSA (scaling a measured 30J spectra with [Hegelich, M. et al., Phys. Plasmas, 12, 056314 (2005).])



1st Demonstration of Break-Out Afterburner:

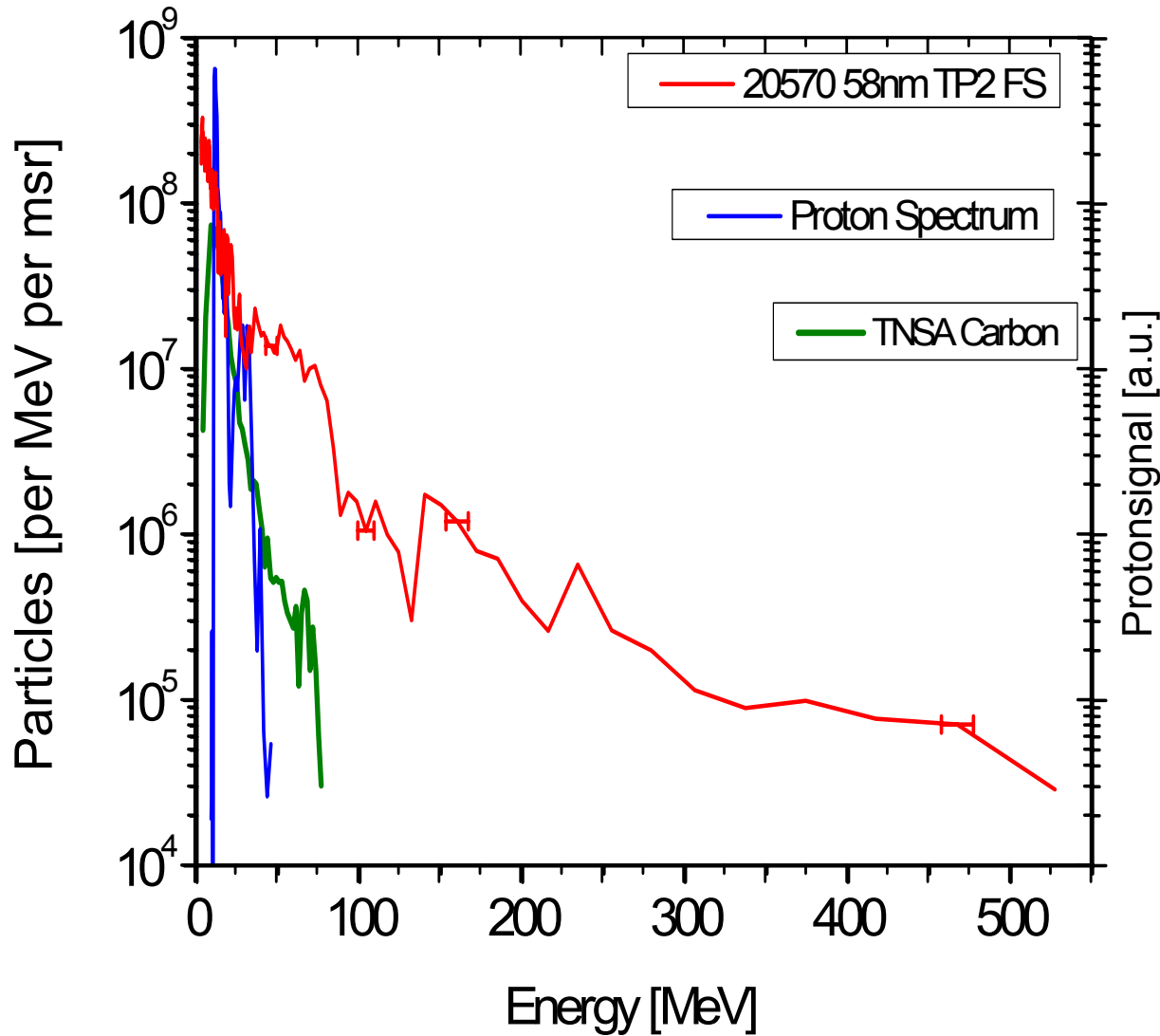
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- >500 MeV Carbon 6+

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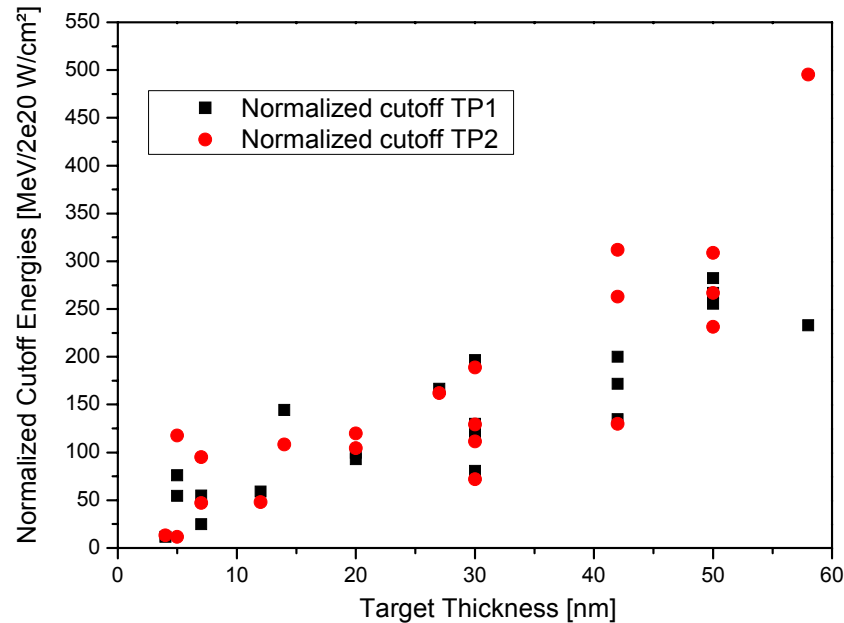
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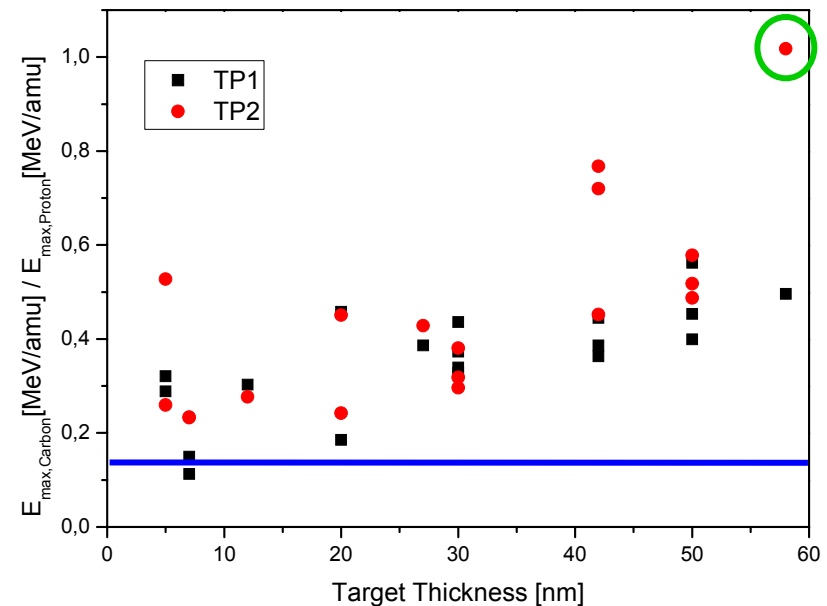
- Compared to 75 MeV from TNSA (scaling a measured 30J spectra with [Hegelich, M. et al., Phys. Plasmas, 12, 056314 (2005).])
- >500 MeV Carbon 6+
- Protons on shot have same velocity
- **First demonstration of BOA acceleration**

Experimental Results: Cutoff energies

Carbon ion reach same velocity as protons



Best shot at 58nm:
0.525 GeV C6+ cutoff energy



Theoretical C/p limit for TNSA is 0.5
best observed TNSA ratio 0.16

Simulation prediction for BOA is 1.0

Hegelich et al., PRL 89, 85002 (2002)



Ion acceleration from nm-targets:

MPQ/LMU – MBI collaboration

Max-Born-Institut

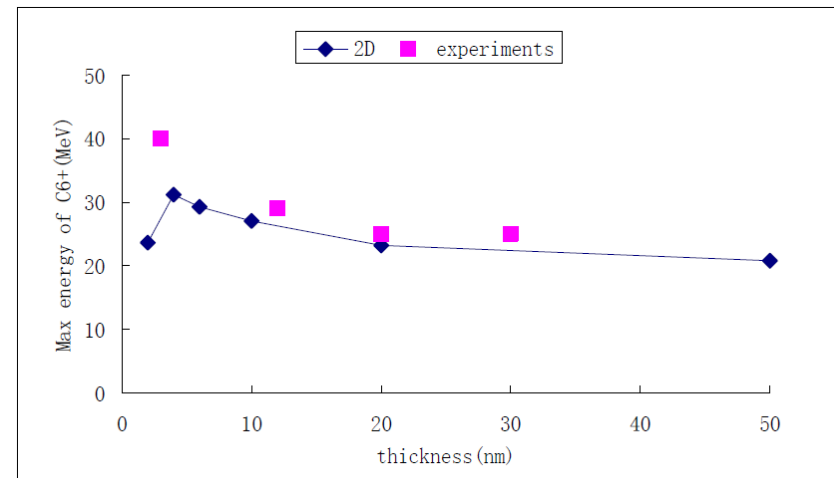
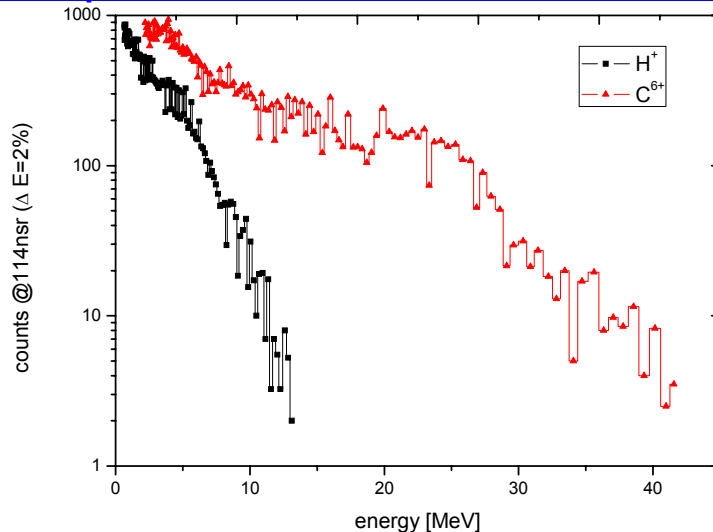
2-weeks experiment in November 2008:

A. Henig, D. Kiefer, D. Jung, X. Yan, D. Habs, M. Hegelich (LMU)

S. Steinke, T. Sokollik, M. Schnürer, P. Nickles (MBI)

- 10Hz Ti:Sapphire laser system: 700 mJ, 45 fs, 3×10^{19} W/cm²
- double plasma mirror for contrast enhancement
- DLC-foils of thickness 50nm down to sub-5nm
(shot at normal incidence)

Ion spectra observed from sub-5nm target at linear polarization:



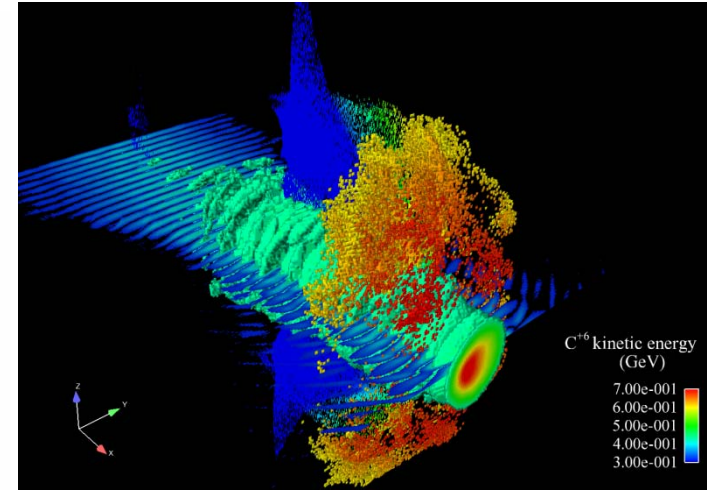
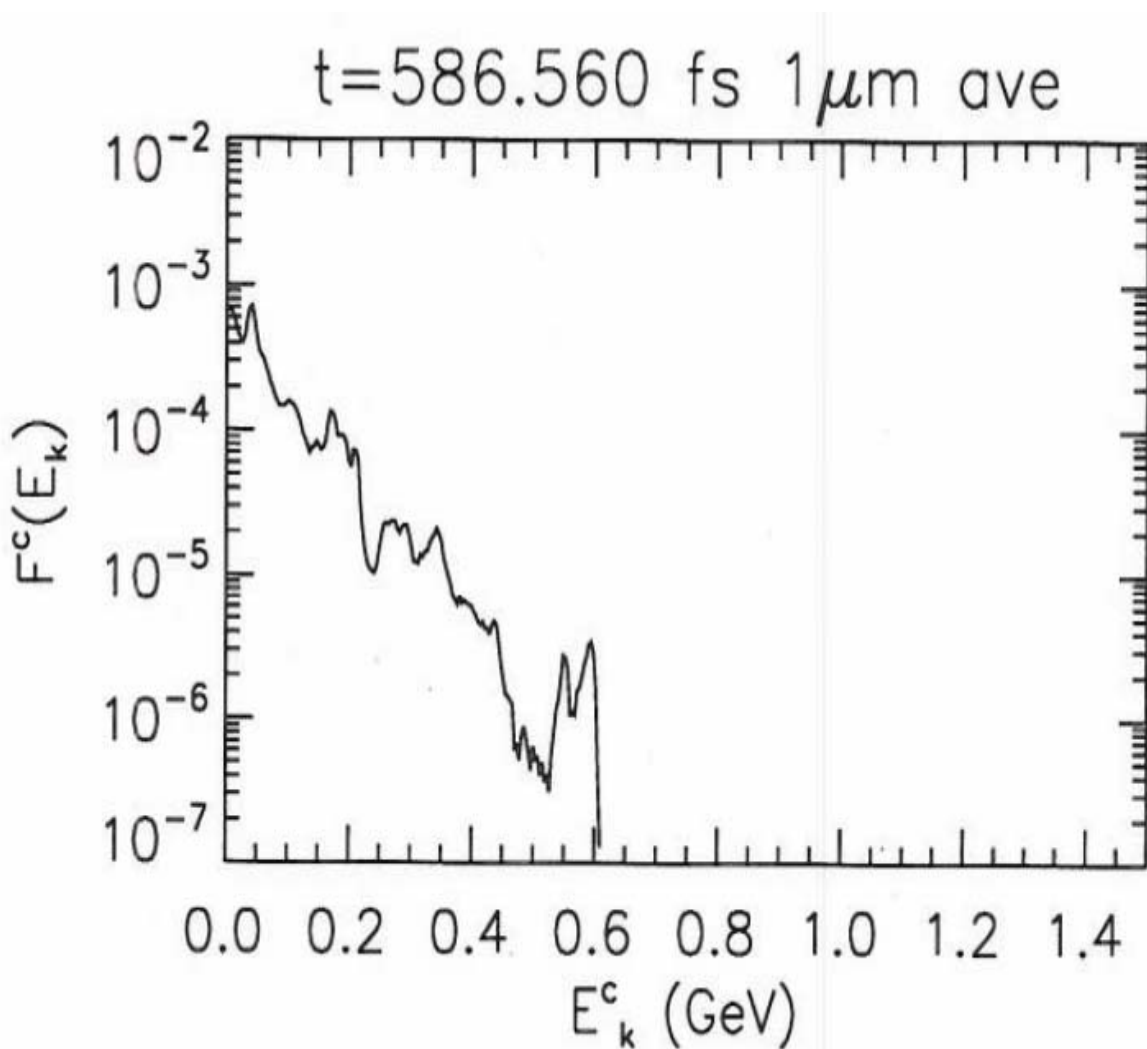
Last experiments in March/April 09 got >70 MeV carbon

Simulations

- Ion energy and spectra qualitatively and quantitatively well reproduced
- Angular anisotropy reproduced: 2D and 3D effects!
- Main acceleration is due to co-moving (with carbon ions) electric field and happens between the times of relativistic and classic transparency (BOA)
- Plasma frequency analysis suggest kinetic instability (Buneman-like) as cause of the E-field
- ~80% of the energy gain happens in BOA phase

VPIC Simulation:

2D simulation of 58nm target shows good agreement



Roadrunner base system

$25 \times 25 \times 20 \mu\text{m}$

Target: 58nm DLC

$n = 821n_{\text{cr}}$ (2.8 g/cc)

$I = 5 \times 10^{20} \text{ W/cm}^2$, $t = 540 \text{ fs}$

FWHM

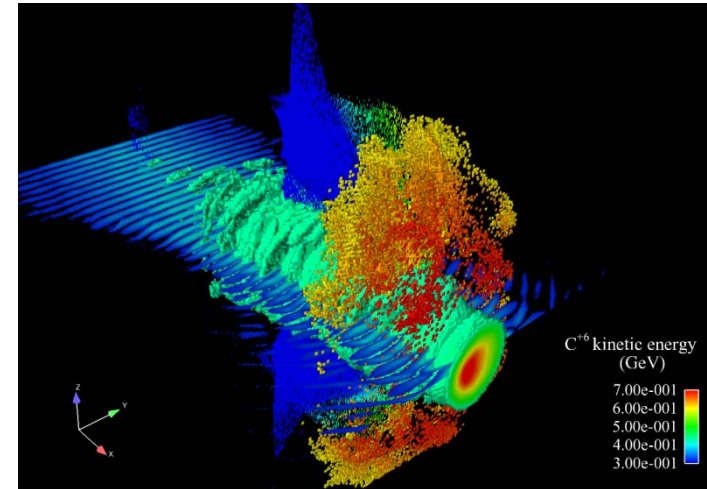
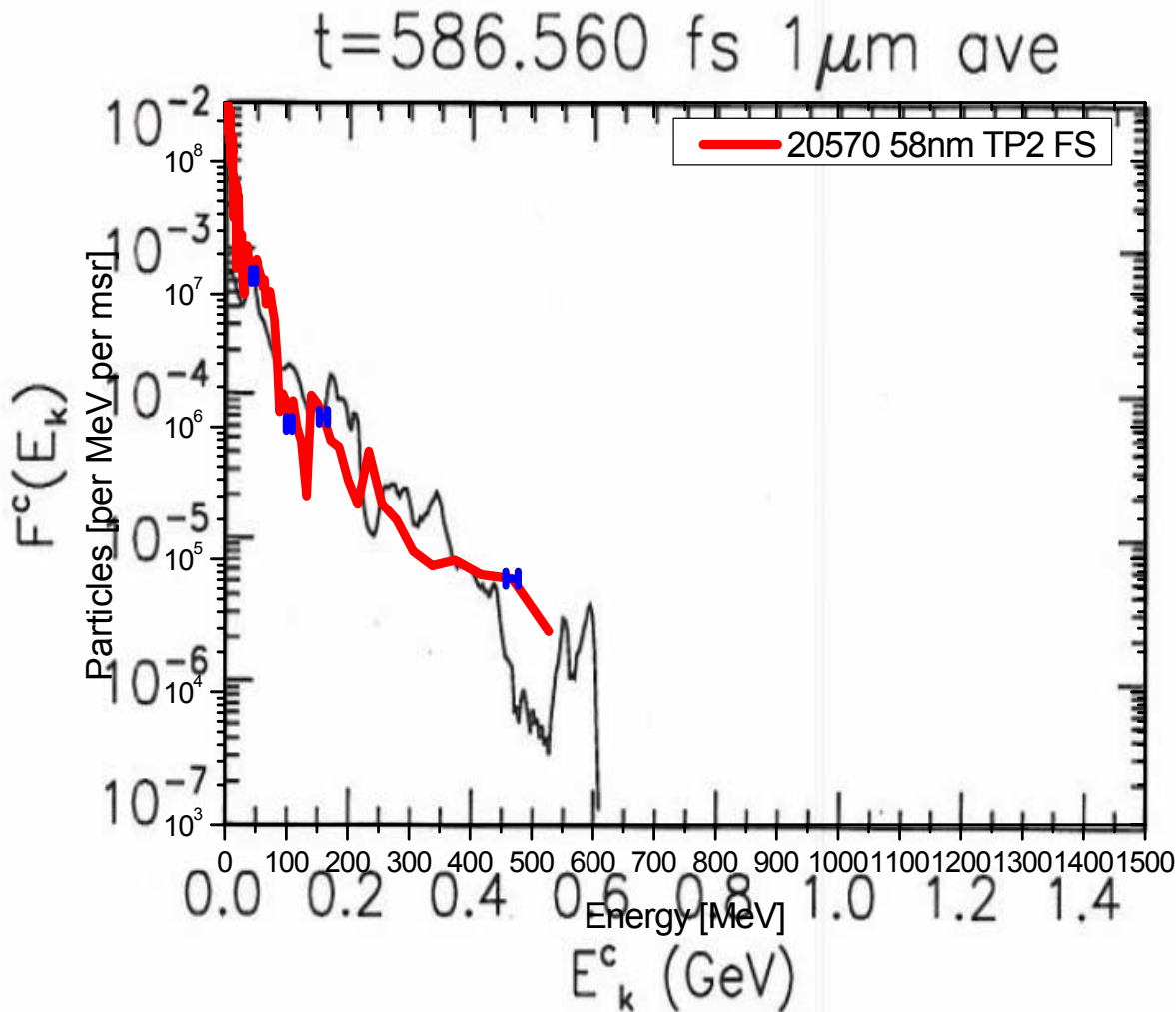
14×10^9 cells

21×10^9 particles

4096 processors

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25x25x20 μm

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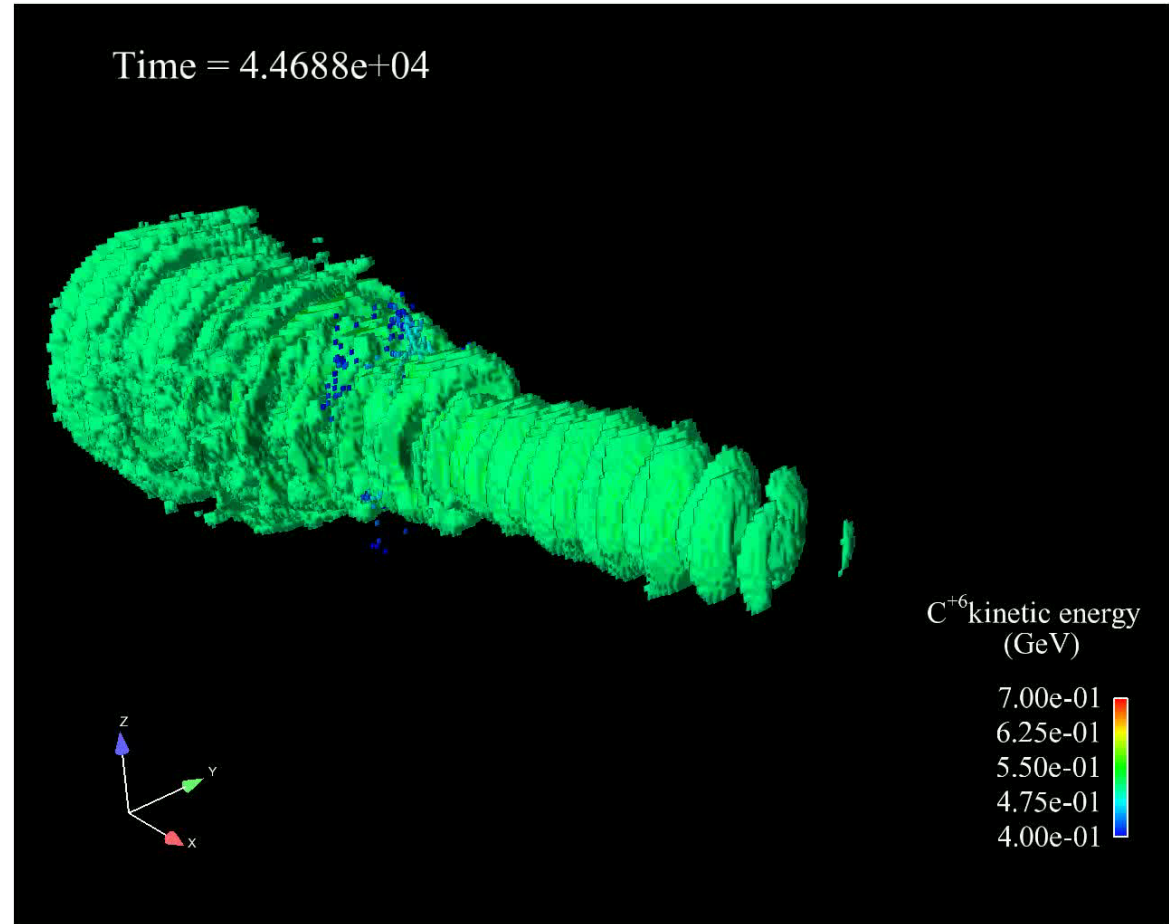
3D VPIC: simulation of the BOA

highest energies are observed out of polarization plane, slightly off-axis

Horizontal Polarization, 60nm C, $I_0 = 6 \times 10^{20}$ W/cm², 540 fs pulse

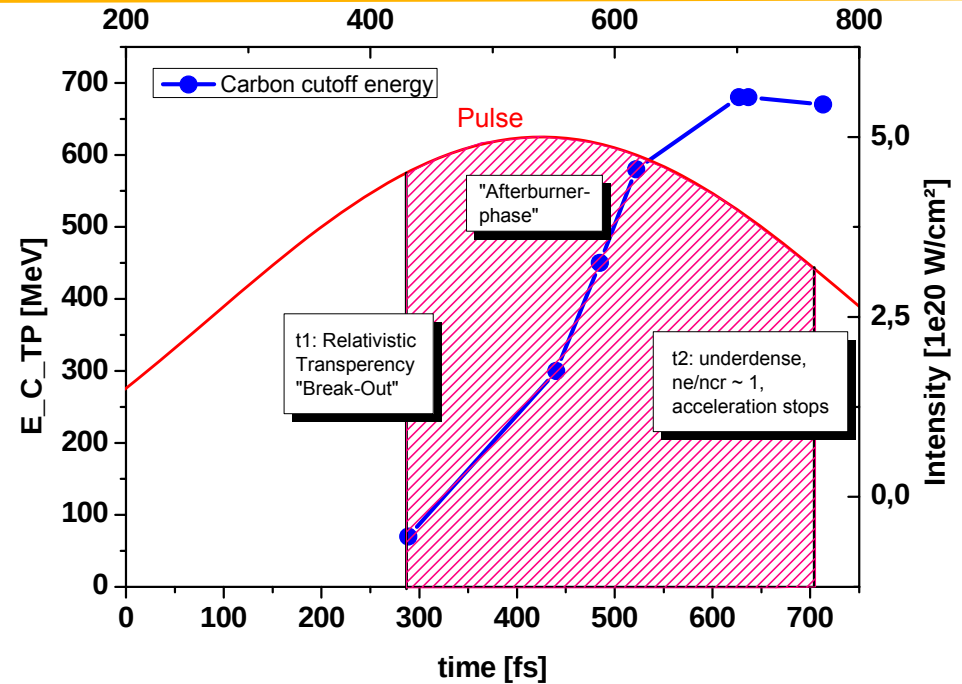
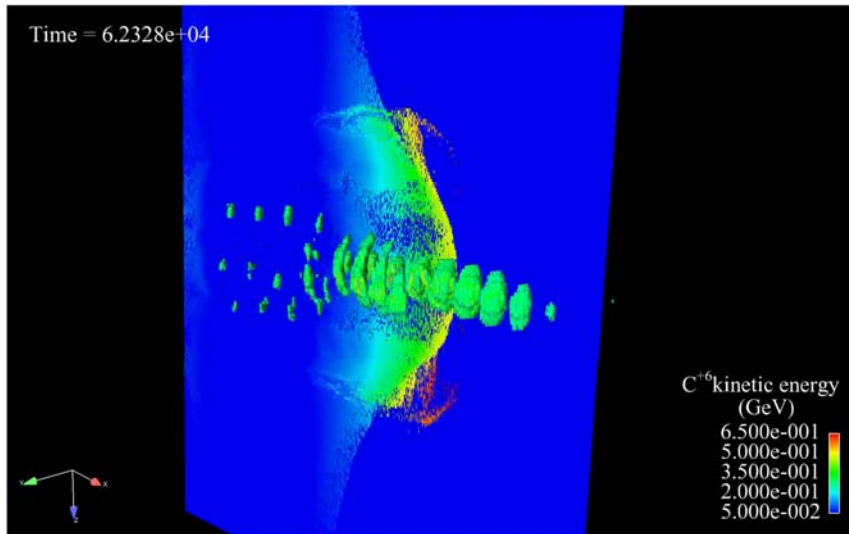
Our largest simulation to date on ion acceleration (run on Roadrunner base system):

- Physical domain 25x25x20 μm w. solid target density
14x10⁹ cells, 21 x 10⁹ particles, 4096 processors
- Contrasting with sim. size at the time of the proposal:
0.5x10⁹ cells, 2.2x10⁹ particles, 510 processors
- 3D visualization using EnSight server-of-servers mode enables viewing, analysis of very large (multiple-TB) data sets.



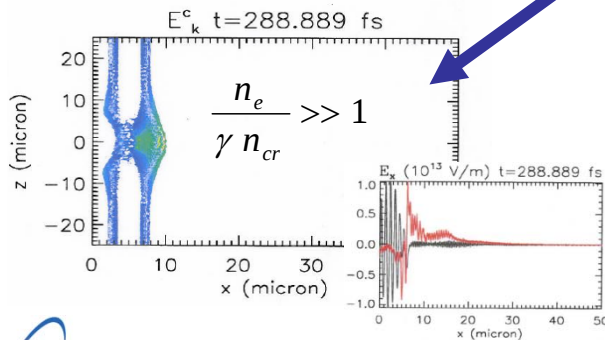
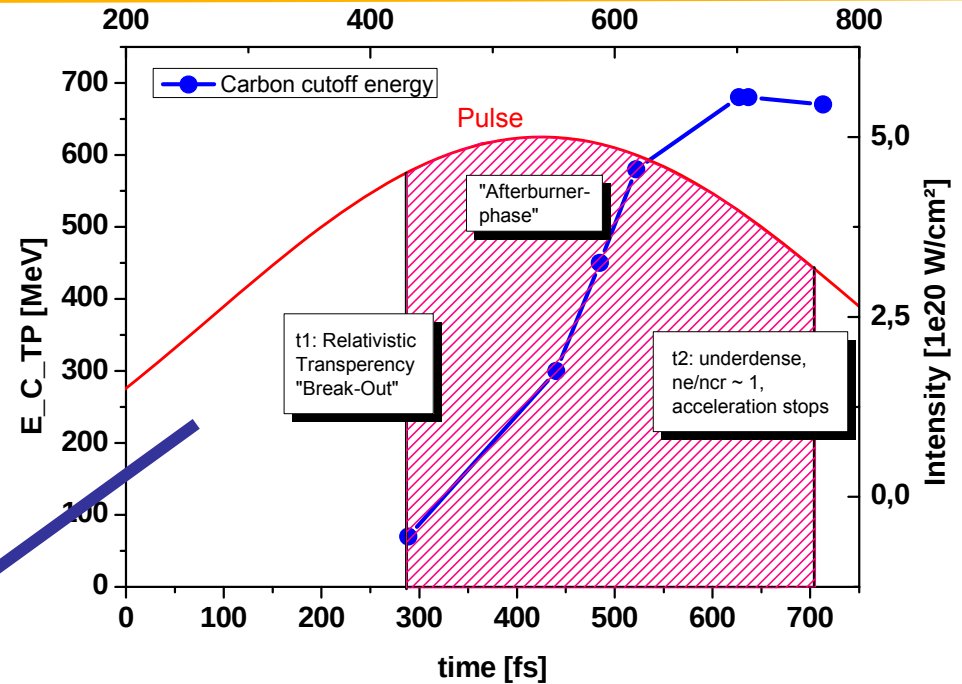
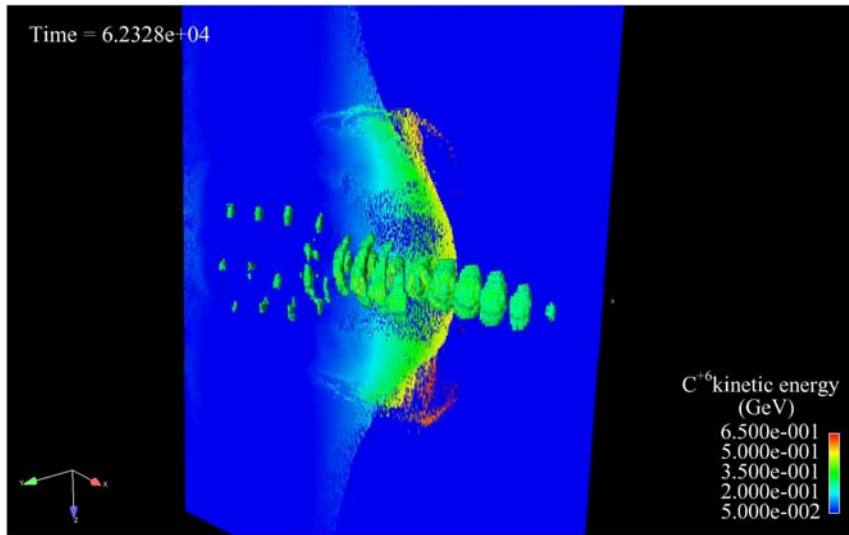
Simulation Results: Acceleration Dynamic

~80% of the carbon acceleration happens during BOA phase



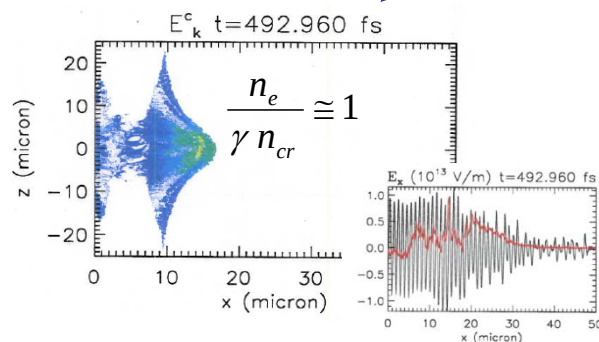
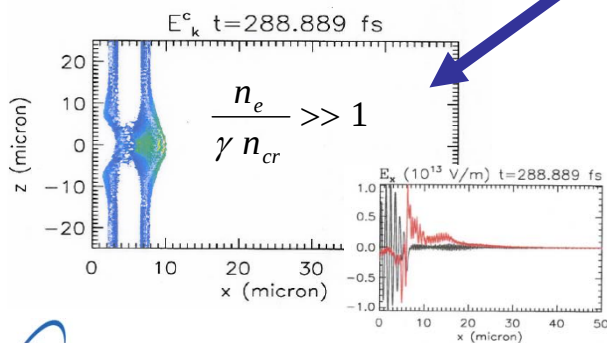
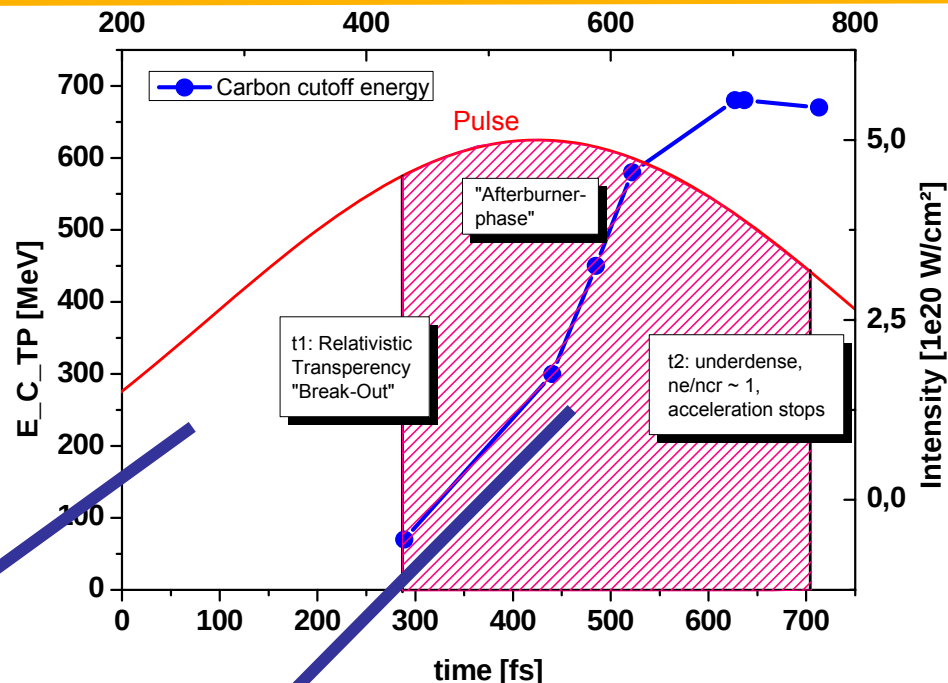
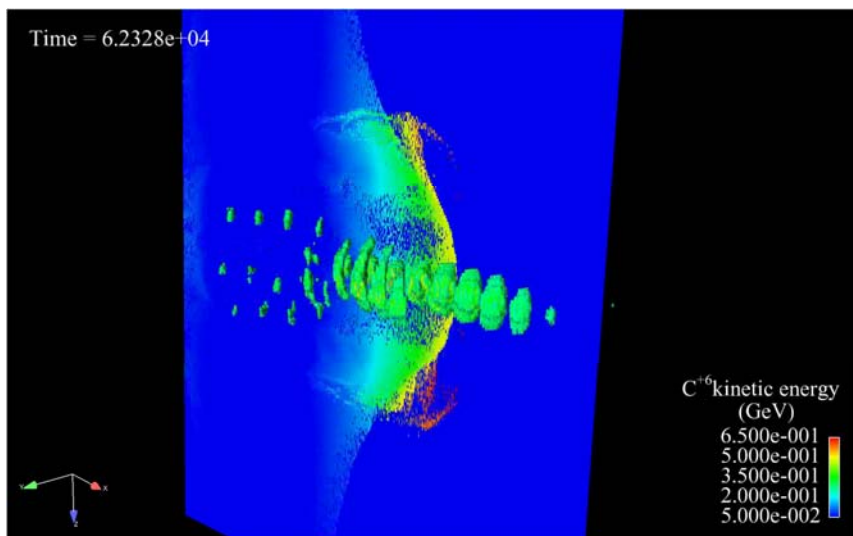
Simulation Results: Acceleration Dynamic

~80% of the carbon acceleration happens during BOA phase



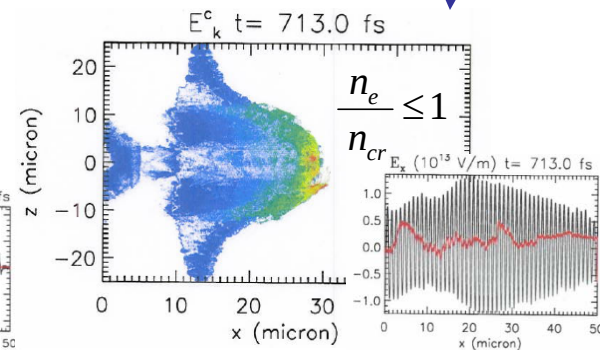
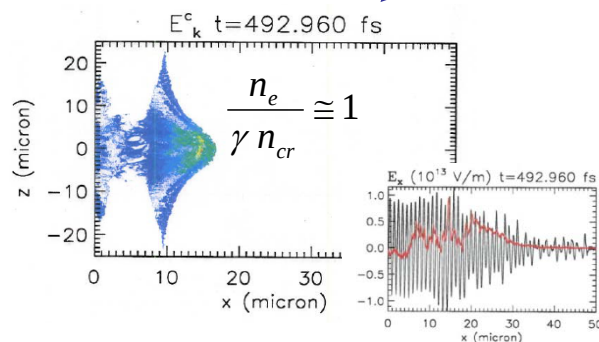
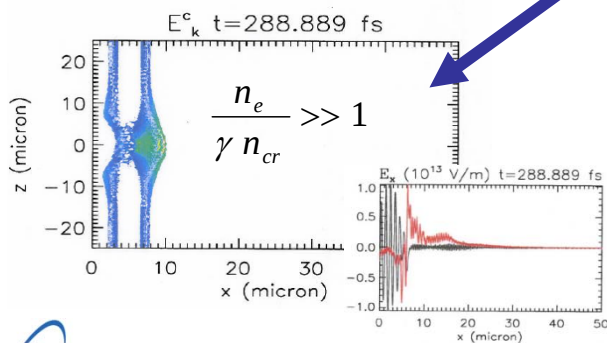
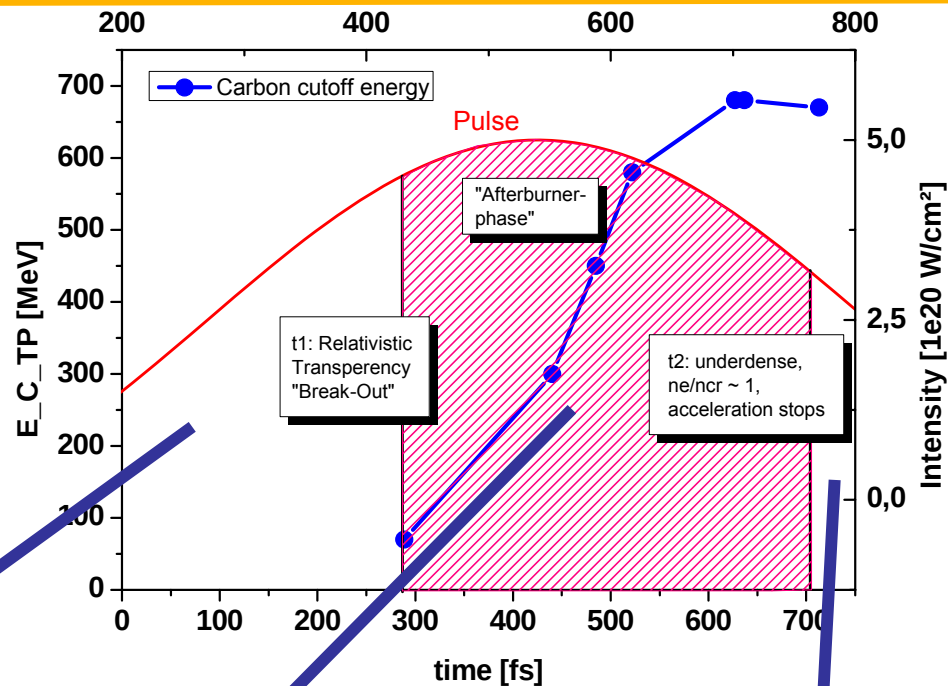
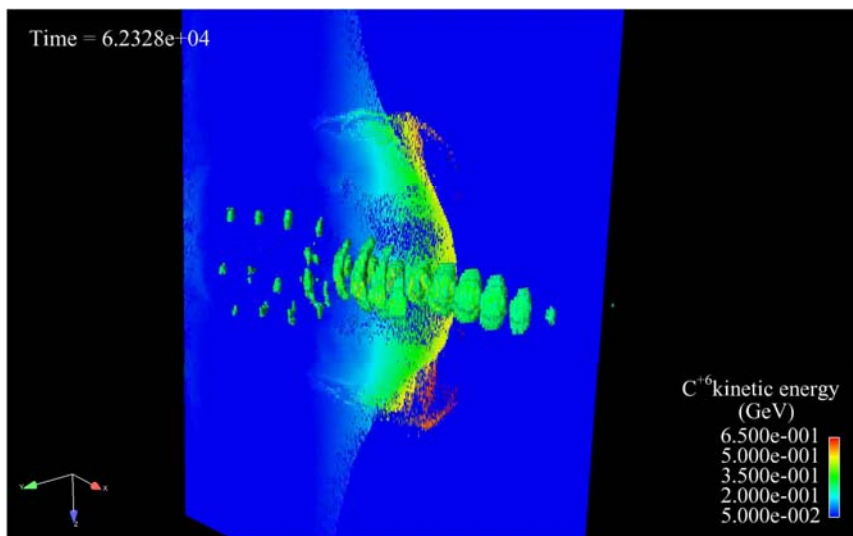
Simulation Results: Acceleration Dynamic

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Simulation Results: Acceleration Dynamic

~80% of the carbon acceleration happens during BOA phase



Theory

- Analytical model* reproduces existing data
- Analytical model showed predictive capability
- Allows design of experiments w/o having to rely on massive parallel simulations

* Yan, Tashima, Hegelich (Subm. to New Journ. Physics (arXiv:0904.1466))

Theory:

HYT- model (Subm. to New Journ. Physics (arXiv:0904.1466))

$$\mathcal{E}_{\text{sum}} = \mathcal{E}_{\text{max},i} + \mathcal{E}_{\text{max},\text{BOA}}$$

$$\mathcal{E}_{\text{max},i}(t_1) = (2\alpha + 1)Q\bar{E}_0(t_1)((1 + \omega t_1)^{1/2\alpha+1} - 1)$$

$$\bar{E}_0(t_1) = m_e c^2 \int_0^{t_1} (\sqrt{T(t')a^2(t') + 1} - 1) \frac{dt'}{t_1}$$

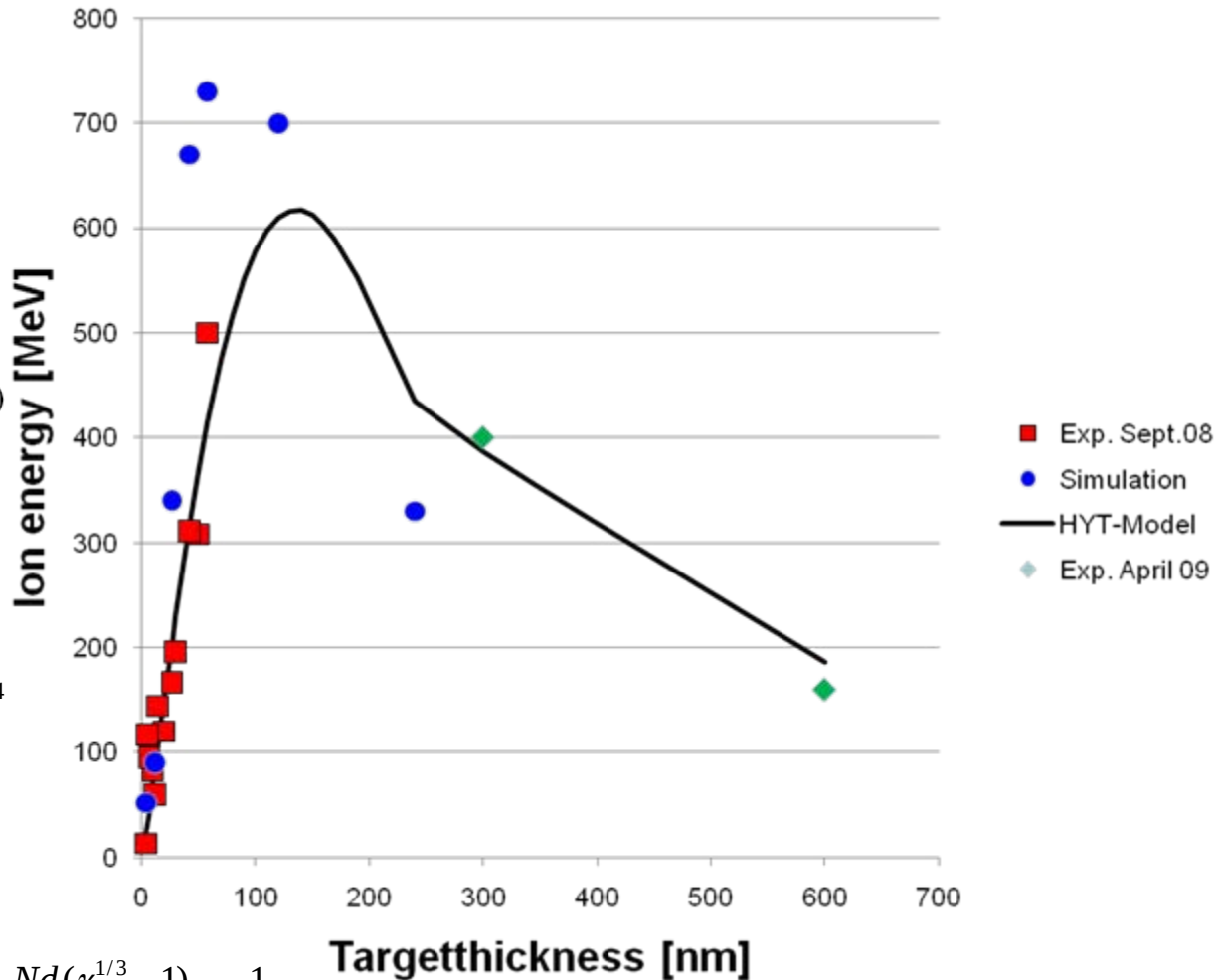
$$\mathcal{E}_{\text{max},i,\text{BOA}} = (2\alpha + 1)Q\bar{E}_0((1 + \omega(t_2 - t_1))^{1/2\alpha+1} - 1)$$

$$t_1 : n_e / \gamma n_{\text{cr}} \sim 1$$

$$t_1 = \left(\frac{M}{m} \frac{3N^2 d^2}{q_i \omega^2 c^2 a_0^3} \right)^{1/4} = \left(\frac{12}{q_i \pi^2} \frac{M}{m} \frac{N^2 d^2}{a_0^3} \frac{\tau^2}{c^2} \right)^{1/4}$$

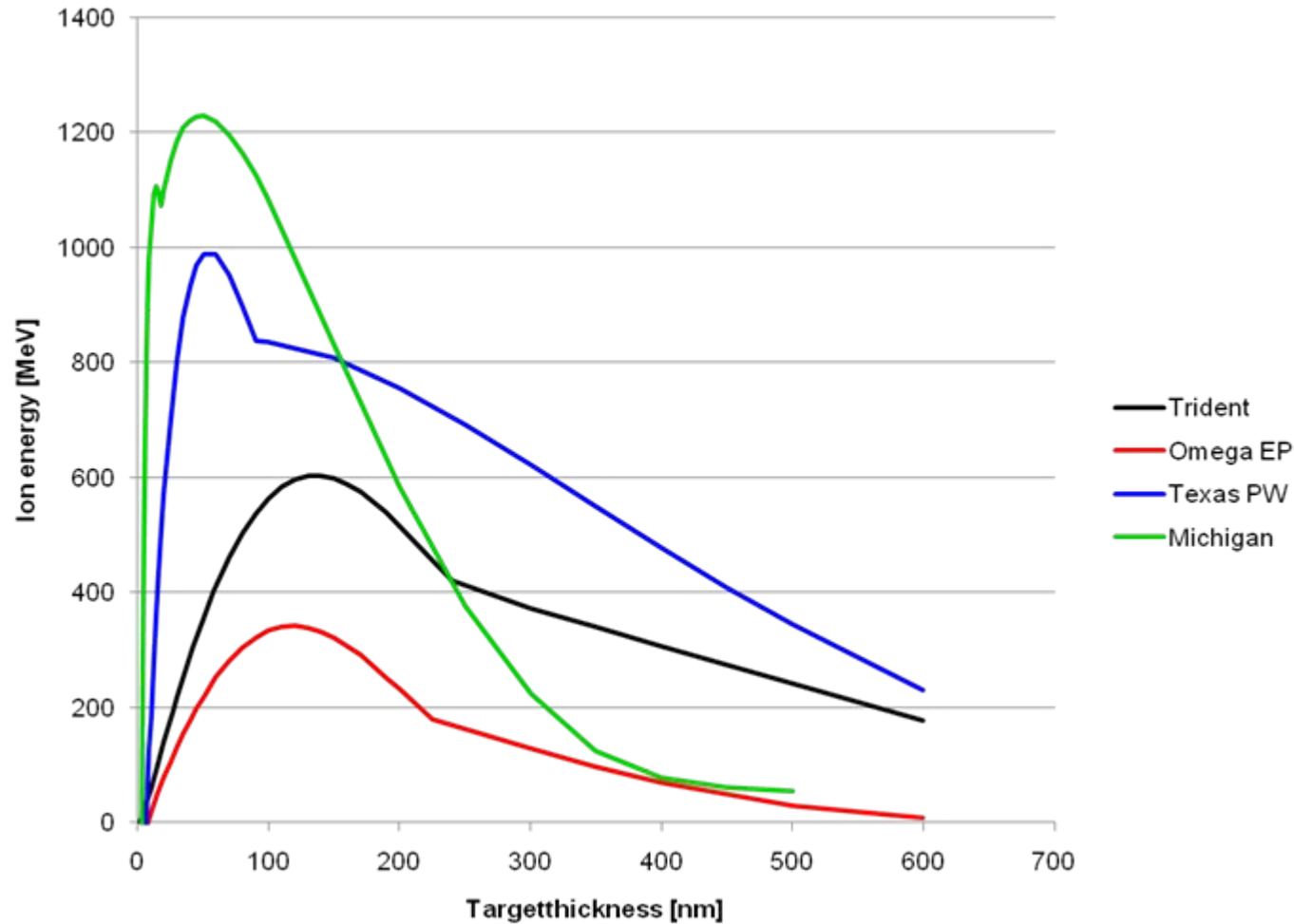
$$t_2 = t_1 + \Delta t : n_e / n_{\text{cr}} \sim 1$$

$$\Delta t = \frac{x_2 - x_1}{C_{s,\text{max}}} \frac{1}{\sin(\omega t_1)} = \frac{x_1(\gamma^{1/3} - 1)}{C_s} \frac{1}{\sin(\omega t_1)} = \frac{Nd(\gamma^{1/3} - 1)}{\gamma C_s} \frac{1}{\sin(\omega t_1)}$$



Outlook

new lasersystems will reach $> \text{GeV}$



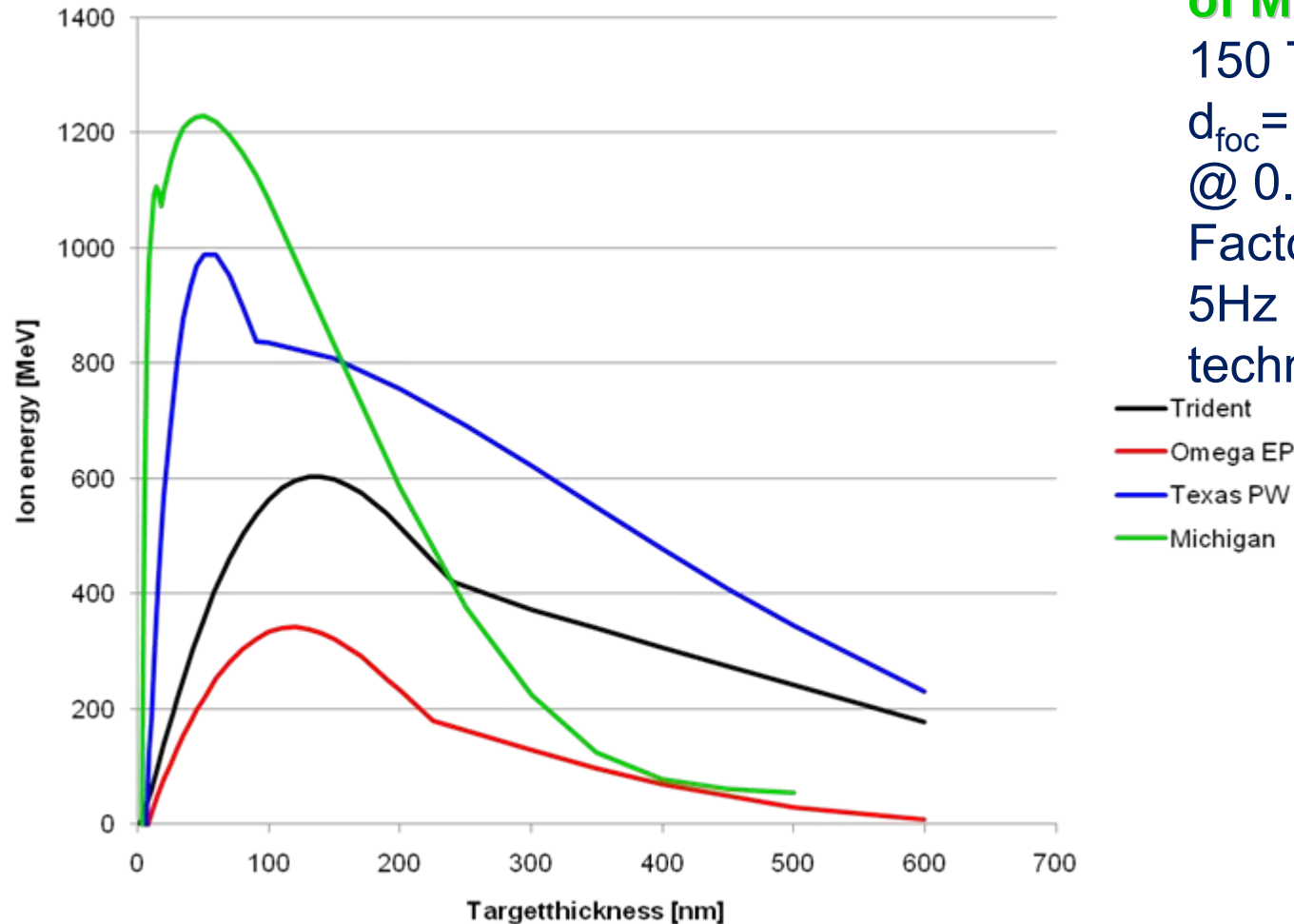
Outlook

new lasersystems will reach > GeV

Hercules Laser @ Univ. of Michigan:

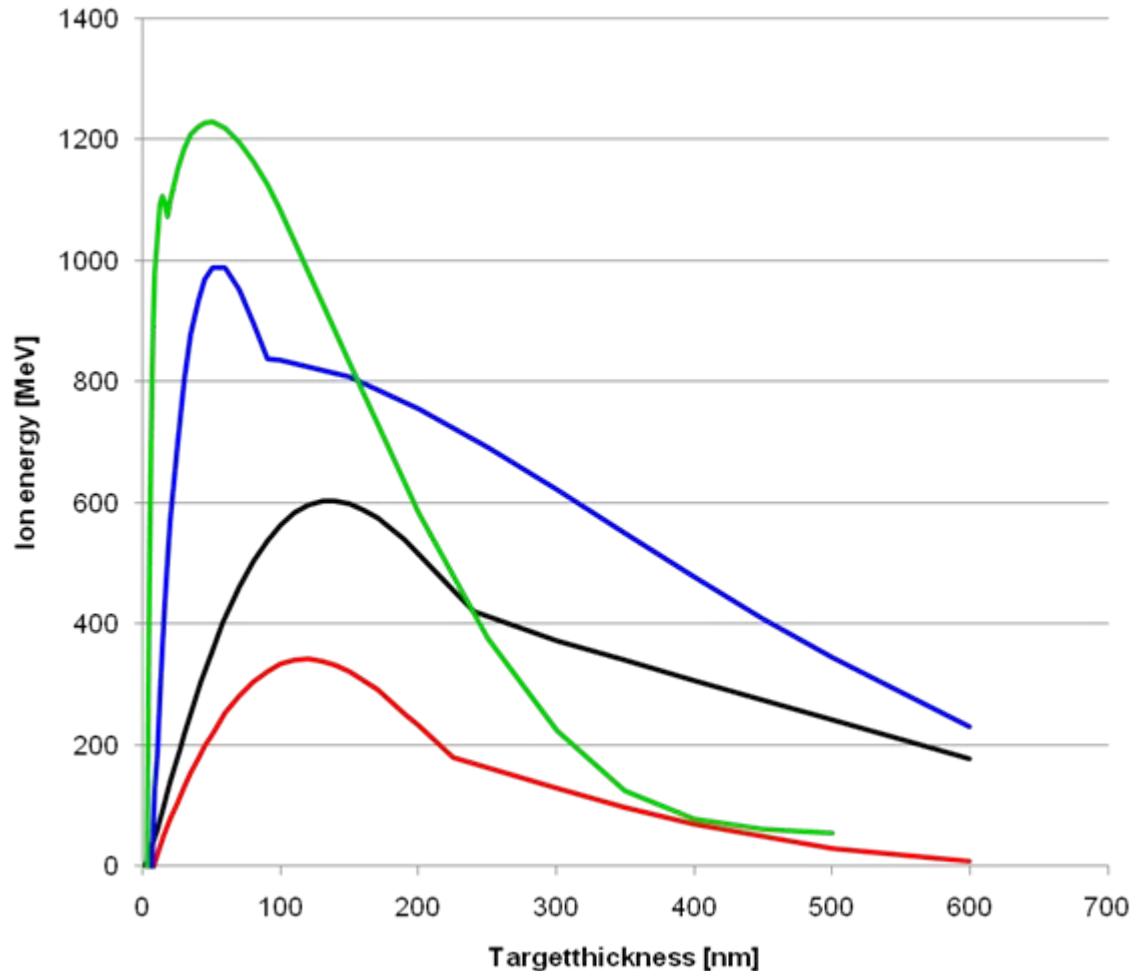
150 TW, 30fs, 5J,
 $d_{\text{foc}} = 1\mu\text{m}$, $1 \times 10^{22} \text{W/cm}^2$,
@ 0.1 Hz

Factor 5 larger system at
5Hz possible with current
technology for ~\$10M



Outlook

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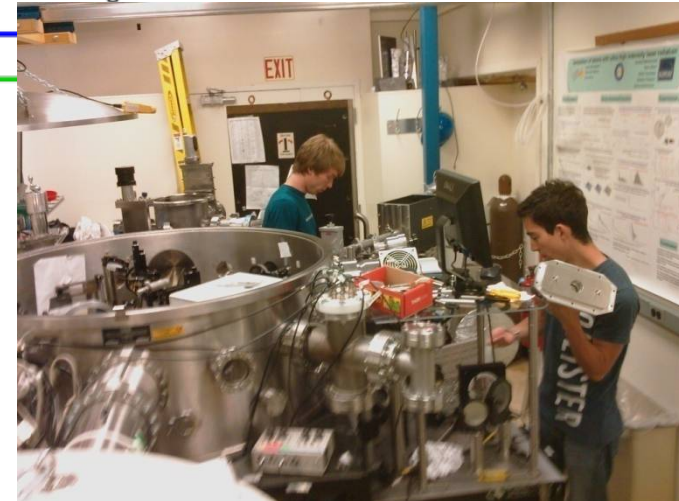


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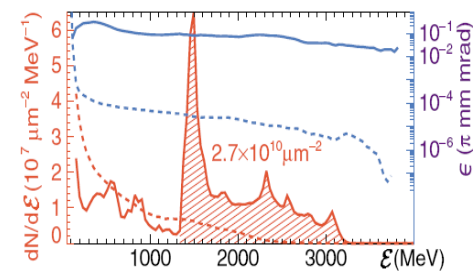
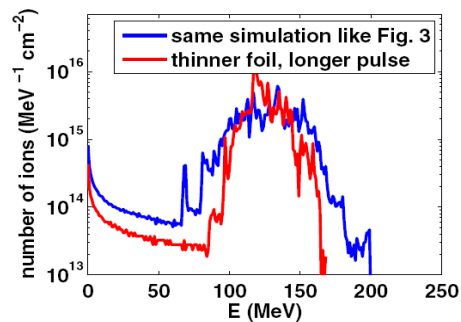
— Trident
— Omega EP
— Hercules



Challenges – Spectral Shape:

Fast rise time of laser pulse ($\sim 15\text{fs}$) enables lower $\Delta E/E$

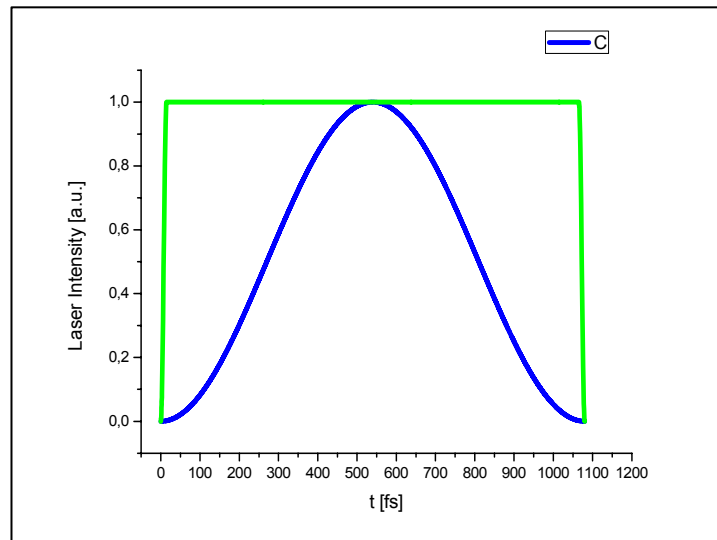
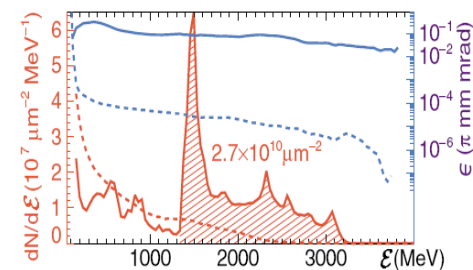
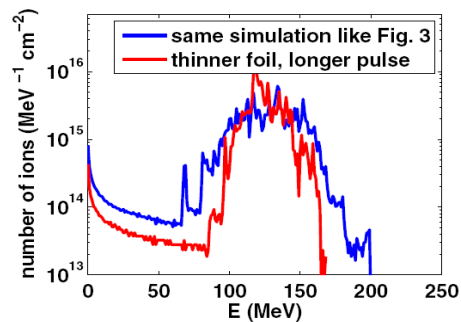
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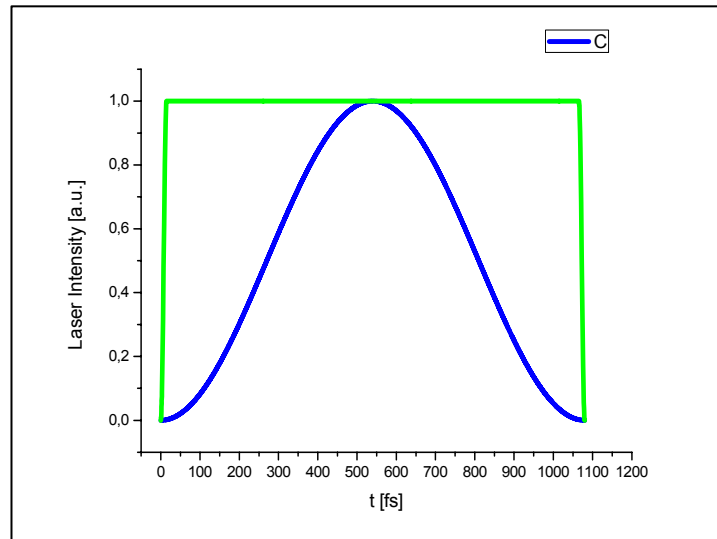
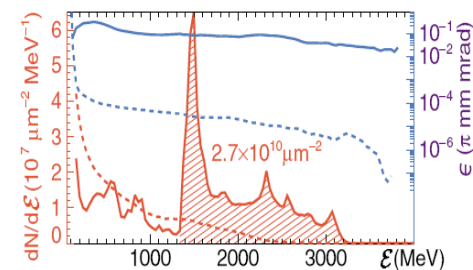
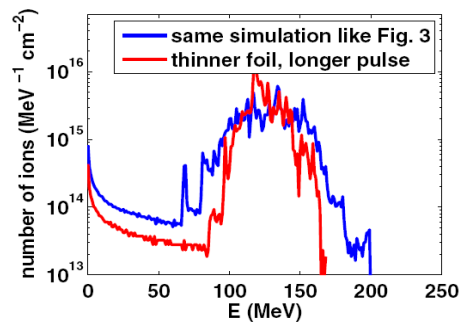
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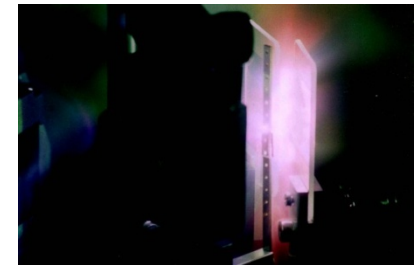
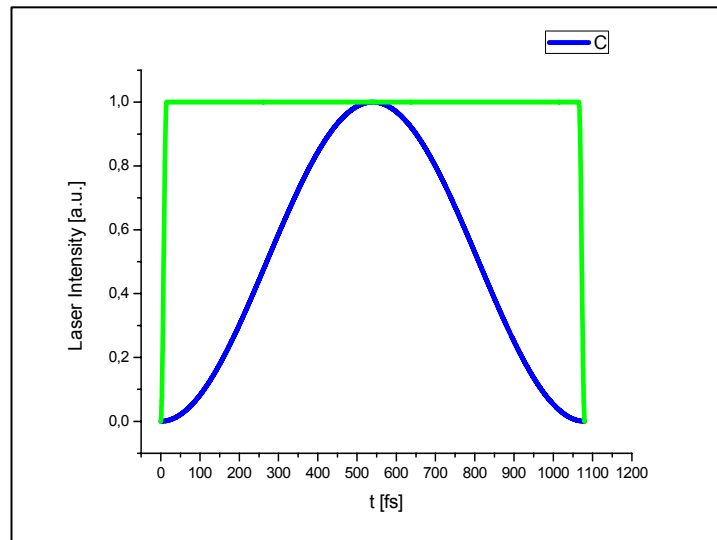
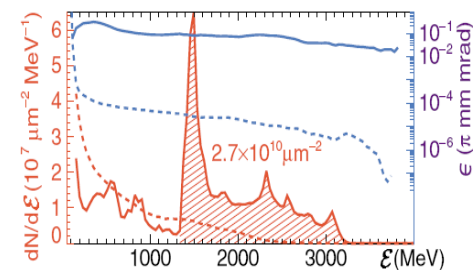
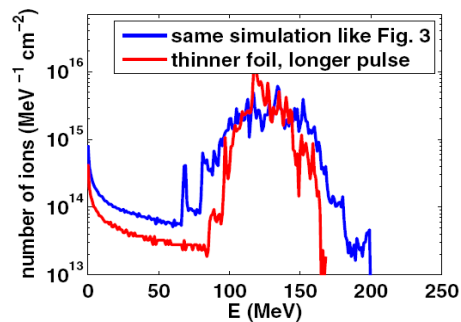
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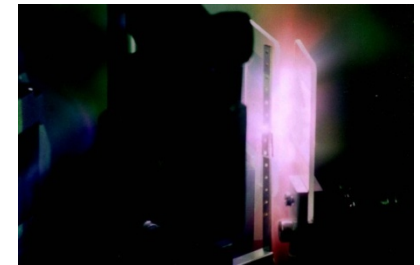
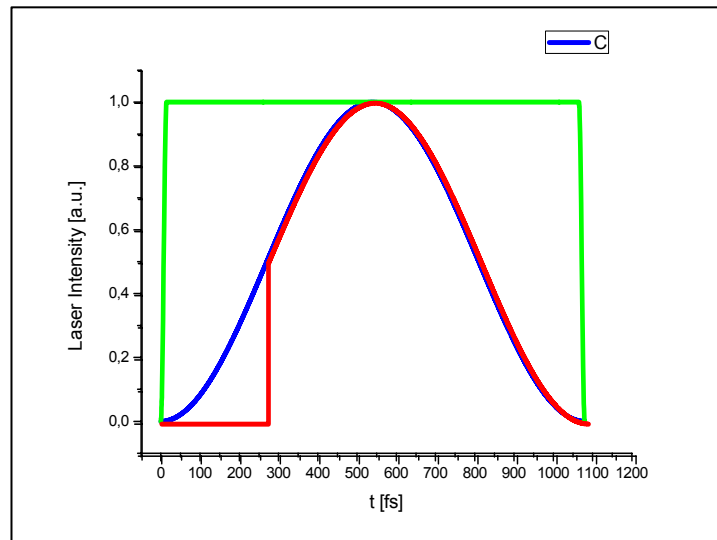
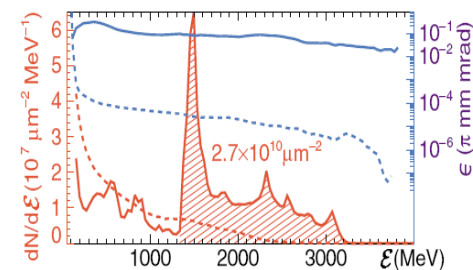
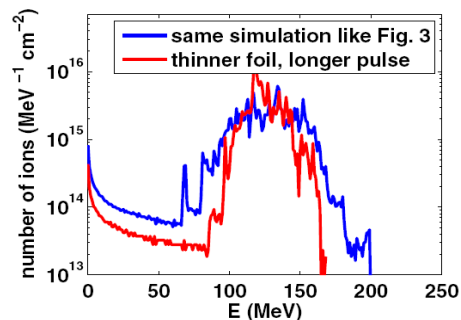
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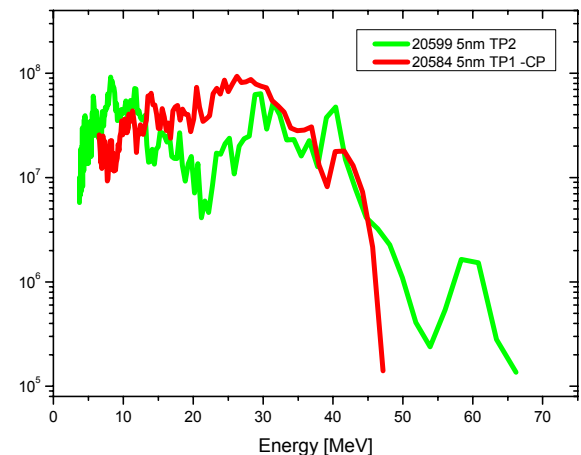
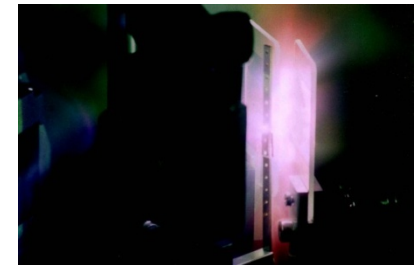
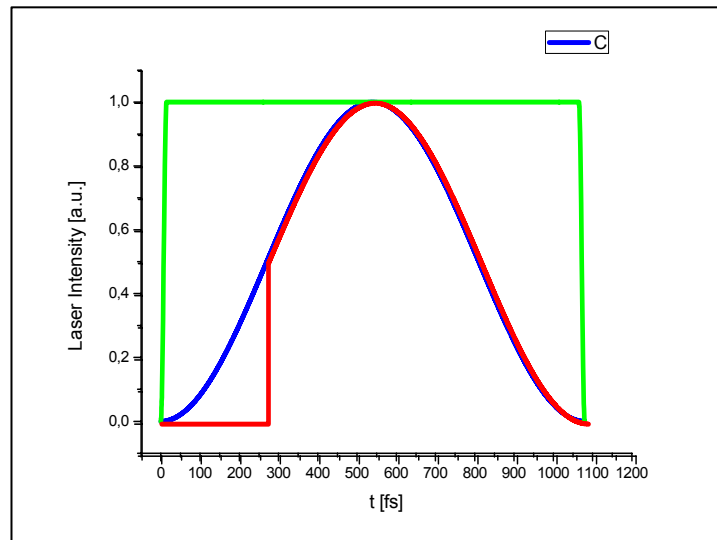
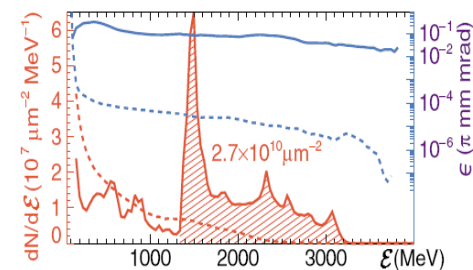
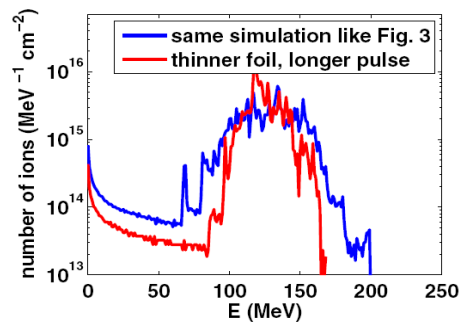
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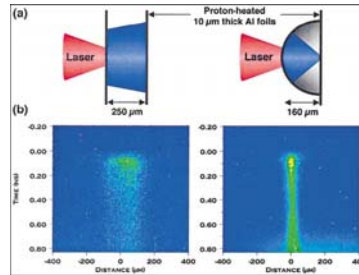
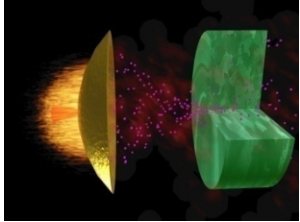
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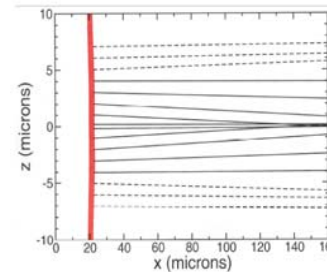
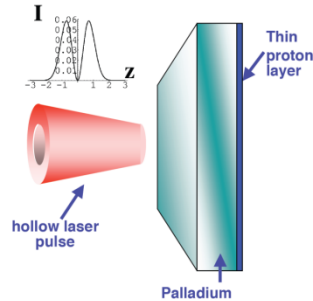
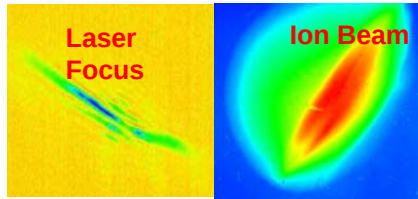
Challenges – Beam Divergence:

A lot of progress has been made in understanding and control

By shaped targets:



By shaped laser focus:



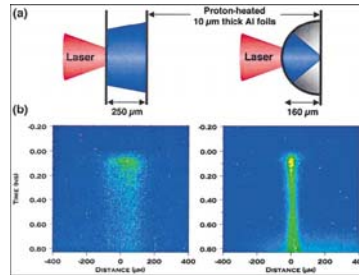
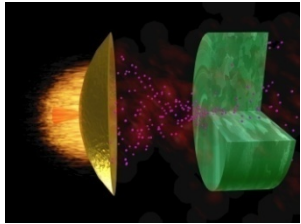
LANL, Yin, Hegelich et al. (2005)



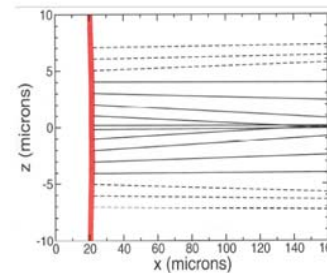
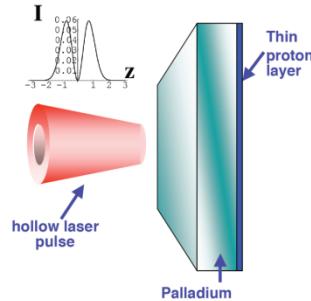
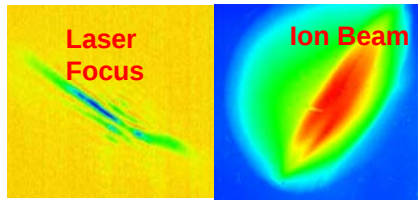
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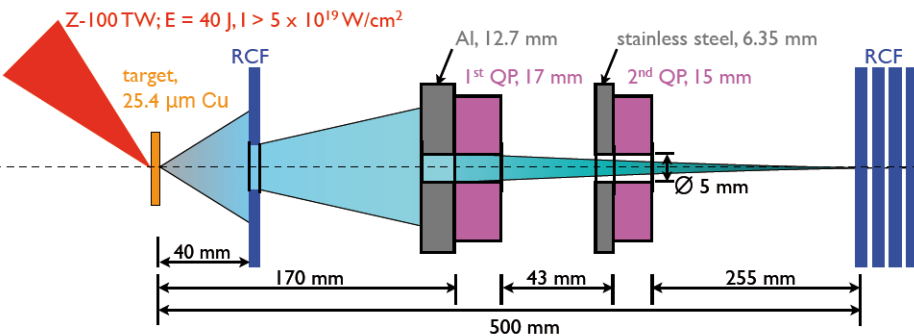
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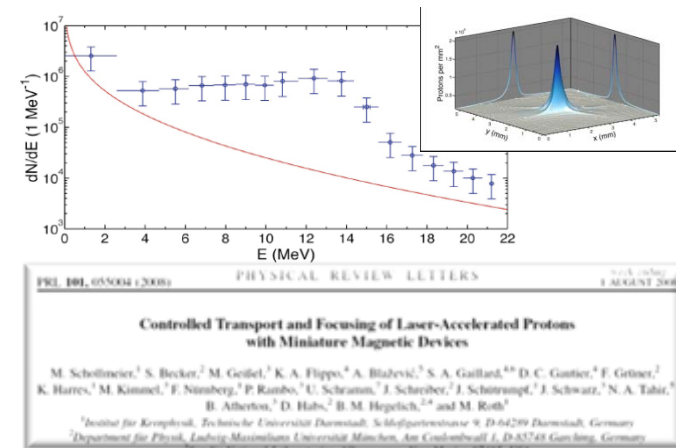
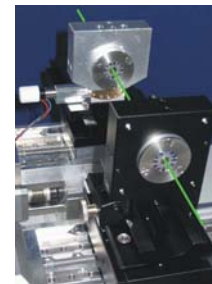
LANL, Yin, Hegelich et al. (2005)



By magnetic lenses:



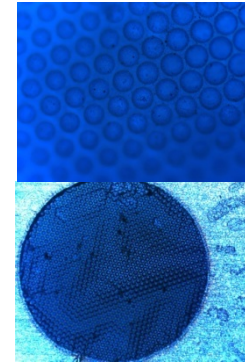
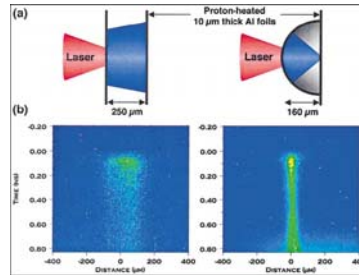
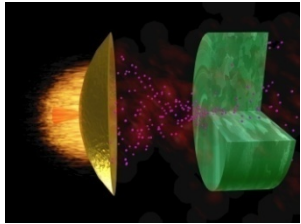
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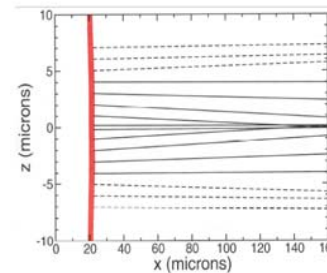
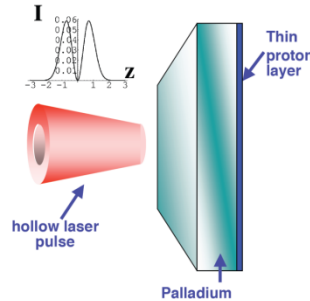
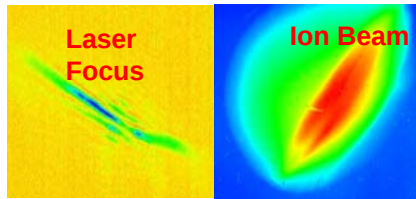
A lot of progress has been made in understanding and control

By shaped targets:



15nm DLC target with micro-hemis:
 $R=42\mu\text{m}$, $d=20\mu\text{m}$
 Mounted over 1mm hole

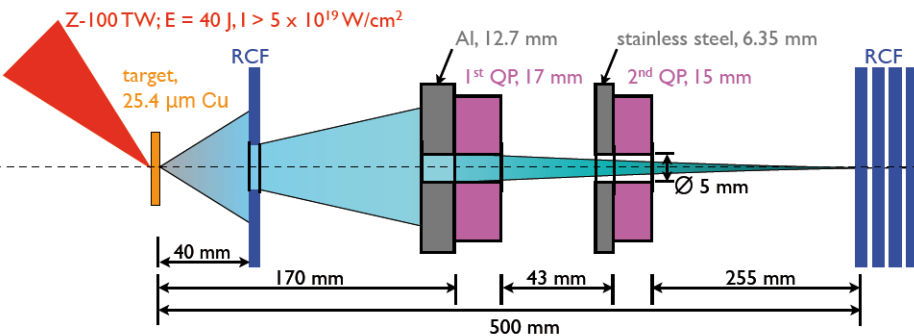
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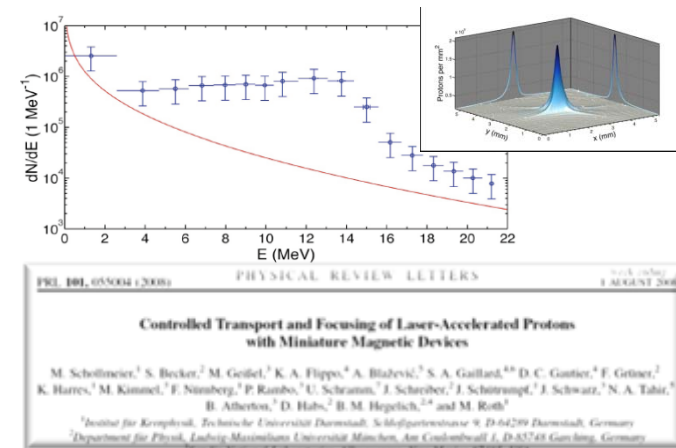
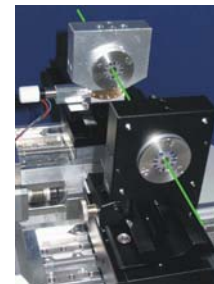
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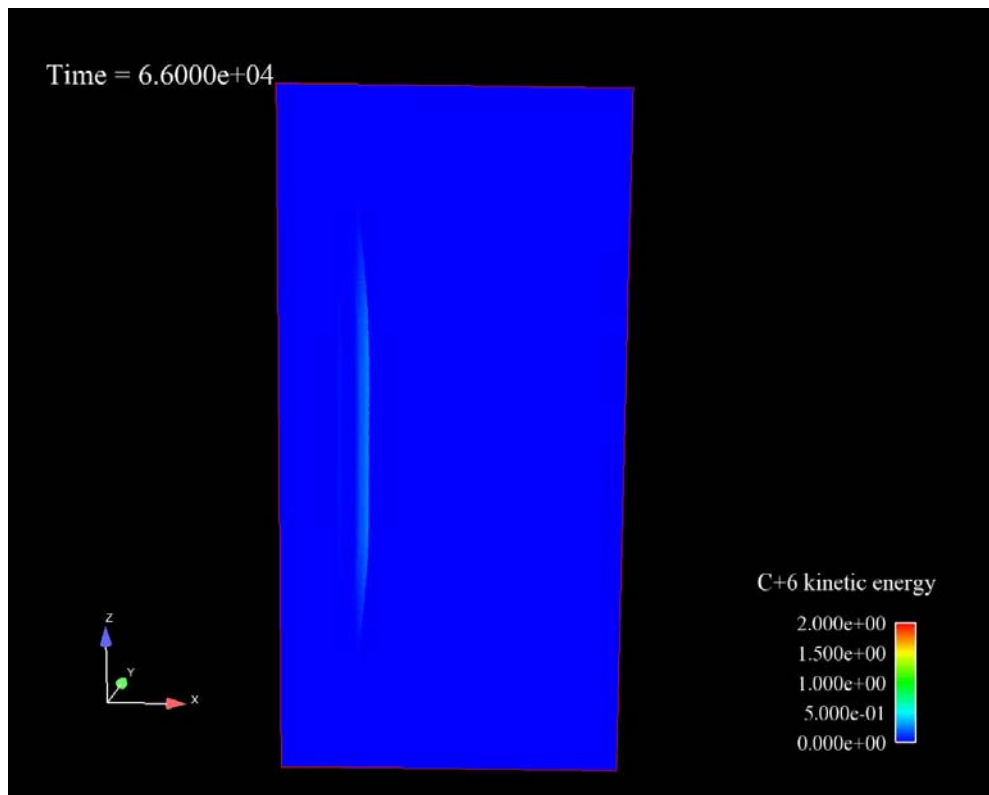
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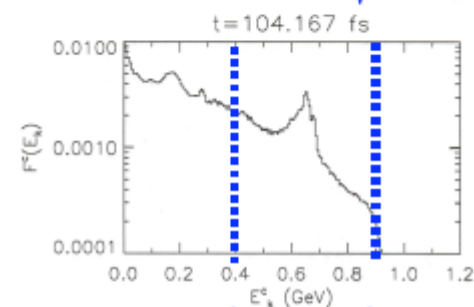
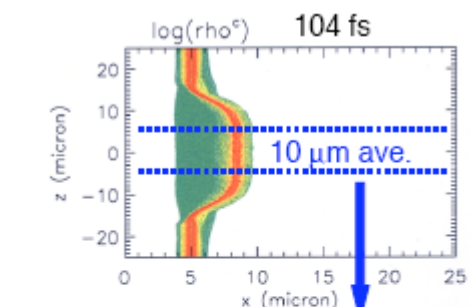
BOA: Laser Pulse Shaping

enables spectral and directional control and higher conversion efficiency

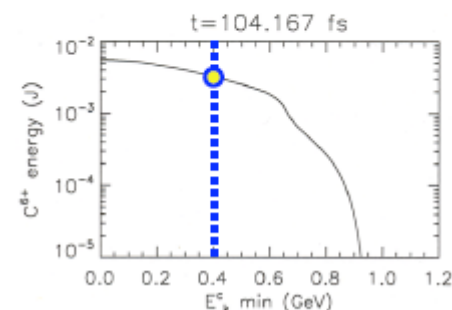
- $I(t) = I_0(t)\exp[-(r^2/2w^2)^6]$
- $w = 10$ microns (spot size larger)
- $I_0(t)$ short rise to 10^{21} W/cm²
- $n_e/n_{cr} = 939$



- Collimated C+6 ion beam
- GeV carbon ions
- Quasi-monoenergetic C6+ > 600 MeV
- 10 μ m ave: 0.003 J in ions > 400 MeV, conversion efficiency ~ 5.5 %
- 50 μ m ave: 0.006 J in ions > 400 MeV, conversion efficiency ~ 11 %



C⁶⁺ energy ~ 0.003 J
efficiency ~ 5.5 %



Summary

- Combination of nm-scale targets and ultrahigh contrast pulses leads to a paradigm shift in relativistic laser-matter interaction.
- We have demonstrated the production and integration of nm-scale targets and ultraclean pulses.
- They enable new particle acceleration mechanisms (BOA, RPA).
- First demonstration of BOA with carbon energies up to 0.5 GeV is promising for applications like IFI and hadron therapy:
- IFI energies reached with modest laser, much smaller than a real FI laser
- Experiments at small Ti:Sa laser at MBL also show enhanced acceleration
- Full 3D PIC simulation on Roadrunner are in excellent agreement and allow design of future experiments

Thank you for your attention!

Colleagues and Collaborators:

LANL:

B. J. Albright
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K. A. Flippo
D. C. Gautier
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B.M. Hegelich
T. Hurry
R. Johnson
S. Letzring
S.-M. Reid
R. Shah
T. Shimada
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LMU München:

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D. Frischke
D. Habs
B. M. Hegelich
A. Henig
R. Hörlein
C. Huebsch
D. Jung
D. Kiefer
H.-J. Meier
J. Schreiber
J. Szerypo
T. Tashima
X. Yan

Kurchatov Institute:

T. Ivkova
V. Liechtenstein
E. Olshanski
A. Spitsin

Support by LANL LDRD
Program Office,
Office of Fusion Energy
Sciences, and LMU
Excellent.

Theory:

Hegelich-Yan-Tashima model: calculating times t_1 and t_2

t_1 is 1D until $x \sim r_0$:

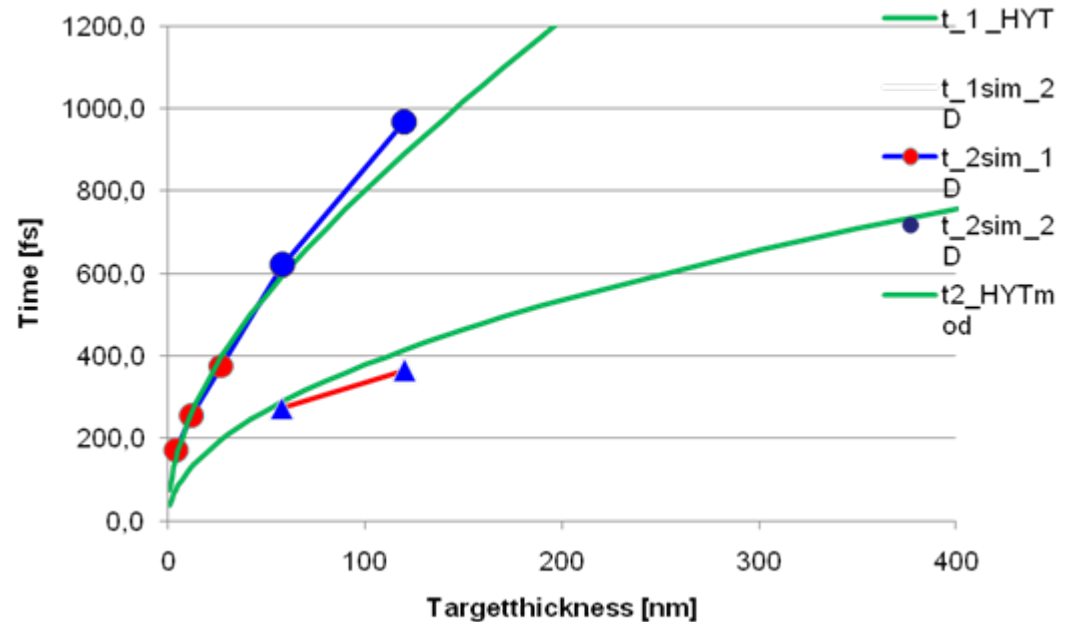
$$\frac{dp}{dt} = \frac{\phi}{r_0} = \frac{\phi_0 \sqrt{a_0^2 + 1}}{r_0} \sin^2(\omega_0 t)$$

$$x dx = \frac{q_i \phi_0 \sqrt{a_0^2 + 1}}{M} \left(t - \frac{1}{2\omega_0} \sin(2\omega_0 t) \right)$$

$$x_1^2 - d^2 = \frac{m}{M} \frac{q_i c^2 \sqrt{a_0^2 + 1}}{3} \omega_0^2 t_1^4$$

$$x_1 = Nd / \gamma = Nd / \sqrt{a_0^2 + 1}, x_1 \gg d$$

$$t_1 = \left(\frac{M}{m} \frac{3N^2 d^2}{q_i \omega_0^2 c^2 a_0^3} \right)^{1/4} = \left(\frac{12}{q_i \pi^2} \frac{M}{m} \frac{N^2 d^2}{a_0^3} \frac{\tau^2}{c^2} \right)^{1/4}$$



$t_2 = t_1 + \Delta t$: 3D sphere isotropic expansion:

$$dt = \frac{dx}{C_s(t)} = \frac{dx}{C_{s,max} \sin(\omega t)}$$

$$\Delta t = \frac{x_2 - x_1}{C_{s,max} \sin(\omega t_1)} = \frac{x_1(\gamma^{1/3} - 1)}{C_s \sin(\omega t_1)} = \frac{Nd(\gamma^{1/3} - 1)}{\gamma C_s \sin(\omega t_1)}$$

Theory:

HYT-model: calculating the maximum energy

$$E_{\max} = (2\alpha(t_1) + 1)\phi_{e-}(t_1)\left((1 + \omega t_1)^{1/2\alpha(t_1)+1} - 1\right) \\ + (2\alpha(t_1) + 1)\phi_{Pt}(t_1)\left((1 + \omega t_1)^{1/2\alpha(t_1)+1} - 1\right) \\ + (2\alpha(t_2) + 1)\phi_{BOA}(t_{2-1})\left((1 + \omega t_{2-1})^{1/2\alpha(t_{2-1})+1} - 1\right)$$

$$\phi_{e-} = m_e c^2 \sqrt{(1 - T(t_1)) \sqrt{2} \langle a(t_1) \rangle + 1}$$

$$\phi_{Pt} = m_e c^2 \sqrt{(T(t_1)) a(t_1)^2 + 1}$$

$$\phi_{BOA} = m_e c^2 \sqrt{(1 - T(t_2)) \langle a(t_2 - t_1) \rangle^2 + 1}$$

$t_{e-} = t_1$ until relativistic transparency

$t_{Pt} = t_1$ until relativistic transparency

$t_{BOA} = t_2 - t_1$

$$a_0^2 = \frac{I_0 \lambda^2}{1.37 \times 10^{18}}$$

$$\sigma = \frac{n_e}{n_{cr}} \frac{d}{\lambda} \quad T = \frac{1}{1 + \pi^2 \frac{\sigma^2}{a(t)^2}}$$